

Appendices

Statistical tables

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Appendix 1

Standard normal distribution areas

| z | $P(Z < z)$ | $P(Z > z)$ | $P(-z < Z < z)$ | $P(Z < -z \text{ or } Z > z)$ |
|------|------------|------------|-----------------|-------------------------------|
| 0.00 | 0.50000 | 0.50000 | 0.00000 | 1.00000 |
| 0.01 | 0.50399 | 0.49601 | 0.00798 | 0.99202 |
| 0.02 | 0.50798 | 0.49202 | 0.01596 | 0.98404 |
| 0.03 | 0.51197 | 0.48803 | 0.02393 | 0.97607 |
| 0.04 | 0.51595 | 0.48405 | 0.03191 | 0.96809 |
| 0.05 | 0.51994 | 0.48006 | 0.03988 | 0.96012 |
| 0.06 | 0.52392 | 0.47608 | 0.04784 | 0.95216 |
| 0.07 | 0.52790 | 0.47210 | 0.05581 | 0.94419 |
| 0.08 | 0.53188 | 0.46812 | 0.06376 | 0.93624 |
| 0.09 | 0.53586 | 0.46414 | 0.07171 | 0.92829 |
| 0.10 | 0.53983 | 0.46017 | 0.07966 | 0.92034 |
| 0.11 | 0.54380 | 0.45620 | 0.08759 | 0.91241 |
| 0.12 | 0.54776 | 0.45224 | 0.09552 | 0.90448 |
| 0.13 | 0.55172 | 0.44828 | 0.10343 | 0.89657 |
| 0.14 | 0.55567 | 0.44433 | 0.11134 | 0.88866 |
| 0.15 | 0.55962 | 0.44038 | 0.11924 | 0.88076 |
| 0.16 | 0.56356 | 0.43644 | 0.12712 | 0.87288 |
| 0.17 | 0.56749 | 0.43251 | 0.13499 | 0.86501 |
| 0.18 | 0.57142 | 0.42858 | 0.14285 | 0.85715 |
| 0.19 | 0.57535 | 0.42465 | 0.15069 | 0.84931 |
| 0.20 | 0.57926 | 0.42074 | 0.15852 | 0.84148 |
| 0.21 | 0.58317 | 0.41683 | 0.16633 | 0.83367 |
| 0.22 | 0.58706 | 0.41294 | 0.17413 | 0.82587 |
| 0.23 | 0.59095 | 0.40905 | 0.18191 | 0.81809 |
| 0.24 | 0.59483 | 0.40517 | 0.18967 | 0.81033 |
| 0.25 | 0.59871 | 0.40129 | 0.19741 | 0.80259 |
| 0.26 | 0.60257 | 0.39743 | 0.20514 | 0.79486 |
| 0.27 | 0.60642 | 0.39358 | 0.21284 | 0.78716 |
| 0.28 | 0.61026 | 0.38974 | 0.22052 | 0.77948 |
| 0.29 | 0.61409 | 0.38591 | 0.22818 | 0.77182 |
| 0.30 | 0.61791 | 0.38209 | 0.23582 | 0.76418 |
| 0.31 | 0.62172 | 0.37828 | 0.24344 | 0.75656 |
| 0.32 | 0.62552 | 0.37448 | 0.25103 | 0.74897 |
| 0.33 | 0.62930 | 0.37070 | 0.25860 | 0.74140 |
| 0.34 | 0.63307 | 0.36693 | 0.26614 | 0.73386 |
| 0.35 | 0.63683 | 0.36317 | 0.27366 | 0.72634 |
| 0.36 | 0.64058 | 0.35942 | 0.28115 | 0.71885 |
| 0.37 | 0.64431 | 0.35569 | 0.28862 | 0.71138 |
| 0.38 | 0.64803 | 0.35197 | 0.29605 | 0.70395 |

| z | $P(Z < z)$ | $P(Z > z)$ | $P(-z < Z < z)$ | $P(Z < -z \text{ or } Z > z)$ |
|------|------------|------------|-----------------|-------------------------------|
| 0.39 | 0.65173 | 0.34827 | 0.30346 | 0.69654 |
| 0.40 | 0.65542 | 0.34458 | 0.31084 | 0.68916 |
| 0.41 | 0.65910 | 0.34090 | 0.31819 | 0.68181 |
| 0.42 | 0.66276 | 0.33724 | 0.32551 | 0.67449 |
| 0.43 | 0.66640 | 0.33360 | 0.33280 | 0.66720 |
| 0.44 | 0.67003 | 0.32997 | 0.34006 | 0.65994 |
| 0.45 | 0.67364 | 0.32636 | 0.34729 | 0.65271 |
| 0.46 | 0.67724 | 0.32276 | 0.35448 | 0.64552 |
| 0.47 | 0.68082 | 0.31918 | 0.36164 | 0.63836 |
| 0.48 | 0.68439 | 0.31561 | 0.36877 | 0.63123 |
| 0.49 | 0.68793 | 0.31207 | 0.37587 | 0.62413 |
| 0.50 | 0.69146 | 0.30854 | 0.38292 | 0.61708 |
| 0.51 | 0.69497 | 0.30503 | 0.38995 | 0.61005 |
| 0.52 | 0.69847 | 0.30153 | 0.39694 | 0.60306 |
| 0.53 | 0.70194 | 0.29806 | 0.40389 | 0.59611 |
| 0.54 | 0.70540 | 0.29460 | 0.41080 | 0.58920 |
| 0.55 | 0.70884 | 0.29116 | 0.41768 | 0.58232 |
| 0.56 | 0.71226 | 0.28774 | 0.42452 | 0.57548 |
| 0.57 | 0.71566 | 0.28434 | 0.43132 | 0.56868 |
| 0.58 | 0.71904 | 0.28096 | 0.43809 | 0.56191 |
| 0.59 | 0.72240 | 0.27760 | 0.44481 | 0.55519 |
| 0.60 | 0.72575 | 0.27425 | 0.45149 | 0.54851 |
| 0.61 | 0.72907 | 0.27093 | 0.45814 | 0.54186 |
| 0.62 | 0.73237 | 0.26763 | 0.46474 | 0.53526 |
| 0.63 | 0.73565 | 0.26435 | 0.47131 | 0.52869 |
| 0.64 | 0.73891 | 0.26109 | 0.47783 | 0.52217 |
| 0.65 | 0.74215 | 0.25785 | 0.48431 | 0.51569 |
| 0.66 | 0.74537 | 0.25463 | 0.49075 | 0.50925 |
| 0.67 | 0.74857 | 0.25143 | 0.49714 | 0.50286 |
| 0.68 | 0.75175 | 0.24825 | 0.50350 | 0.49650 |
| 0.69 | 0.75490 | 0.24510 | 0.50981 | 0.49019 |
| 0.70 | 0.75804 | 0.24196 | 0.51607 | 0.48393 |
| 0.71 | 0.76115 | 0.23885 | 0.52230 | 0.47770 |
| 0.72 | 0.76424 | 0.23576 | 0.52848 | 0.47152 |
| 0.73 | 0.76730 | 0.23270 | 0.53461 | 0.46539 |
| 0.74 | 0.77035 | 0.22965 | 0.54070 | 0.45930 |
| 0.75 | 0.77337 | 0.22663 | 0.54675 | 0.45325 |
| 0.76 | 0.77637 | 0.22363 | 0.55275 | 0.44725 |
| 0.77 | 0.77935 | 0.22065 | 0.55870 | 0.44130 |
| 0.78 | 0.78230 | 0.21770 | 0.56461 | 0.43539 |
| 0.79 | 0.78524 | 0.21476 | 0.57047 | 0.42953 |
| 0.80 | 0.78814 | 0.21186 | 0.57629 | 0.42371 |
| 0.81 | 0.79103 | 0.20897 | 0.58206 | 0.41794 |
| 0.82 | 0.79389 | 0.20611 | 0.58778 | 0.41222 |
| 0.83 | 0.79673 | 0.20327 | 0.59346 | 0.40654 |
| 0.84 | 0.79955 | 0.20045 | 0.59909 | 0.40091 |
| 0.85 | 0.80234 | 0.19766 | 0.60467 | 0.39533 |
| 0.86 | 0.80511 | 0.19489 | 0.61021 | 0.38979 |
| 0.87 | 0.80785 | 0.19215 | 0.61570 | 0.38430 |

| z | $P(Z < z)$ | $P(Z > z)$ | $P(-z < Z < z)$ | $P(Z < -z \text{ or } Z > z)$ |
|------|------------|------------|-----------------|-------------------------------|
| 0.88 | 0.81057 | 0.18943 | 0.62114 | 0.37886 |
| 0.89 | 0.81327 | 0.18673 | 0.62653 | 0.37347 |
| 0.90 | 0.81594 | 0.18406 | 0.63188 | 0.36812 |
| 0.91 | 0.81859 | 0.18141 | 0.63718 | 0.36282 |
| 0.92 | 0.82121 | 0.17879 | 0.64243 | 0.35757 |
| 0.93 | 0.82381 | 0.17619 | 0.64763 | 0.35237 |
| 0.94 | 0.82639 | 0.17361 | 0.65278 | 0.34722 |
| 0.95 | 0.82894 | 0.17106 | 0.65789 | 0.34211 |
| 0.96 | 0.83147 | 0.16853 | 0.66294 | 0.33706 |
| 0.97 | 0.83398 | 0.16602 | 0.66795 | 0.33205 |
| 0.98 | 0.83646 | 0.16354 | 0.67291 | 0.32709 |
| 0.99 | 0.83891 | 0.16109 | 0.67783 | 0.32217 |
| 1.00 | 0.84134 | 0.15866 | 0.68269 | 0.31731 |
| 1.01 | 0.84375 | 0.15625 | 0.68750 | 0.31250 |
| 1.02 | 0.84614 | 0.15386 | 0.69227 | 0.30773 |
| 1.03 | 0.84849 | 0.15151 | 0.69699 | 0.30301 |
| 1.04 | 0.85083 | 0.14917 | 0.70166 | 0.29834 |
| 1.05 | 0.85314 | 0.14686 | 0.70628 | 0.29372 |
| 1.06 | 0.85543 | 0.14457 | 0.71086 | 0.28914 |
| 1.07 | 0.85769 | 0.14231 | 0.71538 | 0.28462 |
| 1.08 | 0.85993 | 0.14007 | 0.71986 | 0.28014 |
| 1.09 | 0.86214 | 0.13786 | 0.72429 | 0.27571 |
| 1.10 | 0.86433 | 0.13567 | 0.72867 | 0.27133 |
| 1.11 | 0.86650 | 0.13350 | 0.73300 | 0.26700 |
| 1.12 | 0.86864 | 0.13136 | 0.73729 | 0.26271 |
| 1.13 | 0.87076 | 0.12924 | 0.74152 | 0.25848 |
| 1.14 | 0.87286 | 0.12714 | 0.74571 | 0.25429 |
| 1.15 | 0.87493 | 0.12507 | 0.74986 | 0.25014 |
| 1.16 | 0.87698 | 0.12302 | 0.75395 | 0.24605 |
| 1.17 | 0.87900 | 0.12100 | 0.75800 | 0.24200 |
| 1.18 | 0.88100 | 0.11900 | 0.76200 | 0.23800 |
| 1.19 | 0.88298 | 0.11702 | 0.76595 | 0.23405 |
| 1.20 | 0.88493 | 0.11507 | 0.76986 | 0.23014 |
| 1.21 | 0.88686 | 0.11314 | 0.77372 | 0.22628 |
| 1.22 | 0.88877 | 0.11123 | 0.77754 | 0.22246 |
| 1.23 | 0.89065 | 0.10935 | 0.78130 | 0.21870 |
| 1.24 | 0.89251 | 0.10749 | 0.78502 | 0.21498 |
| 1.25 | 0.89435 | 0.10565 | 0.78870 | 0.21130 |
| 1.26 | 0.89617 | 0.10383 | 0.79233 | 0.20767 |
| 1.27 | 0.89796 | 0.10204 | 0.79592 | 0.20408 |
| 1.28 | 0.89973 | 0.10027 | 0.79945 | 0.20055 |
| 1.29 | 0.90147 | 0.09853 | 0.80295 | 0.19705 |
| 1.30 | 0.90320 | 0.09680 | 0.80640 | 0.19360 |
| 1.31 | 0.90490 | 0.09510 | 0.80980 | 0.19020 |
| 1.32 | 0.90658 | 0.09342 | 0.81316 | 0.18684 |
| 1.33 | 0.90824 | 0.09176 | 0.81648 | 0.18352 |
| 1.34 | 0.90988 | 0.09012 | 0.81975 | 0.18025 |
| 1.35 | 0.91149 | 0.08851 | 0.82298 | 0.17702 |
| 1.36 | 0.91309 | 0.08691 | 0.82617 | 0.17383 |

| z | $P(Z < z)$ | $P(Z > z)$ | $P(-z < Z < z)$ | $P(Z < -z \text{ or } Z > z)$ |
|------|------------|------------|-----------------|-------------------------------|
| 1.37 | 0.91466 | 0.08534 | 0.82931 | 0.17069 |
| 1.38 | 0.91621 | 0.08379 | 0.83241 | 0.16759 |
| 1.39 | 0.91774 | 0.08226 | 0.83547 | 0.16453 |
| 1.40 | 0.91924 | 0.08076 | 0.83849 | 0.16151 |
| 1.41 | 0.92073 | 0.07927 | 0.84146 | 0.15854 |
| 1.42 | 0.92220 | 0.07780 | 0.84439 | 0.15561 |
| 1.43 | 0.92364 | 0.07636 | 0.84728 | 0.15272 |
| 1.44 | 0.92507 | 0.07493 | 0.85013 | 0.14987 |
| 1.45 | 0.92647 | 0.07353 | 0.85294 | 0.14706 |
| 1.46 | 0.92785 | 0.07215 | 0.85571 | 0.14429 |
| 1.47 | 0.92922 | 0.07078 | 0.85844 | 0.14156 |
| 1.48 | 0.93056 | 0.06944 | 0.86113 | 0.13887 |
| 1.49 | 0.93189 | 0.06811 | 0.86378 | 0.13622 |
| 1.50 | 0.93319 | 0.06681 | 0.86639 | 0.13361 |
| 1.51 | 0.93448 | 0.06552 | 0.86896 | 0.13104 |
| 1.52 | 0.93574 | 0.06426 | 0.87149 | 0.12851 |
| 1.53 | 0.93699 | 0.06301 | 0.87398 | 0.12602 |
| 1.54 | 0.93822 | 0.06178 | 0.87644 | 0.12356 |
| 1.55 | 0.93943 | 0.06057 | 0.87886 | 0.12114 |
| 1.56 | 0.94062 | 0.05938 | 0.88124 | 0.11876 |
| 1.57 | 0.94179 | 0.05821 | 0.88358 | 0.11642 |
| 1.58 | 0.94295 | 0.05705 | 0.88589 | 0.11411 |
| 1.59 | 0.94408 | 0.05592 | 0.88817 | 0.11183 |
| 1.60 | 0.94520 | 0.05480 | 0.89040 | 0.10960 |
| 1.61 | 0.94630 | 0.05370 | 0.89260 | 0.10740 |
| 1.62 | 0.94738 | 0.05262 | 0.89477 | 0.10523 |
| 1.63 | 0.94845 | 0.05155 | 0.89690 | 0.10310 |
| 1.64 | 0.94950 | 0.05050 | 0.89899 | 0.10101 |
| 1.65 | 0.95053 | 0.04947 | 0.90106 | 0.09894 |
| 1.66 | 0.95154 | 0.04846 | 0.90309 | 0.09691 |
| 1.67 | 0.95254 | 0.04746 | 0.90508 | 0.09492 |
| 1.68 | 0.95352 | 0.04648 | 0.90704 | 0.09296 |
| 1.69 | 0.95449 | 0.04551 | 0.90897 | 0.09103 |
| 1.70 | 0.95543 | 0.04457 | 0.91087 | 0.08913 |
| 1.71 | 0.95637 | 0.04363 | 0.91273 | 0.08727 |
| 1.72 | 0.95728 | 0.04272 | 0.91457 | 0.08543 |
| 1.73 | 0.95818 | 0.04182 | 0.91637 | 0.08363 |
| 1.74 | 0.95907 | 0.04093 | 0.91814 | 0.08186 |
| 1.75 | 0.95994 | 0.04006 | 0.91988 | 0.08012 |
| 1.76 | 0.96080 | 0.03920 | 0.92159 | 0.07841 |
| 1.77 | 0.96164 | 0.03836 | 0.92327 | 0.07673 |
| 1.78 | 0.96246 | 0.03754 | 0.92492 | 0.07508 |
| 1.79 | 0.96327 | 0.03673 | 0.92655 | 0.07345 |
| 1.80 | 0.96407 | 0.03593 | 0.92814 | 0.07186 |
| 1.81 | 0.96485 | 0.03515 | 0.92970 | 0.07030 |
| 1.82 | 0.96562 | 0.03438 | 0.93124 | 0.06876 |
| 1.83 | 0.96638 | 0.03362 | 0.93275 | 0.06725 |
| 1.84 | 0.96712 | 0.03288 | 0.93423 | 0.06577 |
| 1.85 | 0.96784 | 0.03216 | 0.93569 | 0.06431 |

| z | $P(Z < z)$ | $P(Z > z)$ | $P(-z < Z < z)$ | $P(Z < -z \text{ or } Z > z)$ |
|------|------------|------------|-----------------|-------------------------------|
| 1.86 | 0.96856 | 0.03144 | 0.93711 | 0.06289 |
| 1.87 | 0.96926 | 0.03074 | 0.93852 | 0.06148 |
| 1.88 | 0.96995 | 0.03005 | 0.93989 | 0.06011 |
| 1.89 | 0.97062 | 0.02938 | 0.94124 | 0.05876 |
| 1.90 | 0.97128 | 0.02872 | 0.94257 | 0.05743 |
| 1.91 | 0.97193 | 0.02807 | 0.94387 | 0.05613 |
| 1.92 | 0.97257 | 0.02743 | 0.94514 | 0.05486 |
| 1.93 | 0.97320 | 0.02680 | 0.94639 | 0.05361 |
| 1.94 | 0.97381 | 0.02619 | 0.94762 | 0.05238 |
| 1.95 | 0.97441 | 0.02559 | 0.94882 | 0.05118 |
| 1.96 | 0.97500 | 0.02500 | 0.95000 | 0.05000 |
| 1.97 | 0.97558 | 0.02442 | 0.95116 | 0.04884 |
| 1.98 | 0.97615 | 0.02385 | 0.95230 | 0.04770 |
| 1.99 | 0.97670 | 0.02330 | 0.95341 | 0.04659 |
| 2.00 | 0.97725 | 0.02275 | 0.95450 | 0.04550 |
| 2.01 | 0.97778 | 0.02222 | 0.95557 | 0.04443 |
| 2.02 | 0.97831 | 0.02169 | 0.95662 | 0.04338 |
| 2.03 | 0.97882 | 0.02118 | 0.95764 | 0.04236 |
| 2.04 | 0.97932 | 0.02068 | 0.95865 | 0.04135 |
| 2.05 | 0.97982 | 0.02018 | 0.95964 | 0.04036 |
| 2.06 | 0.98030 | 0.01970 | 0.96060 | 0.03940 |
| 2.07 | 0.98077 | 0.01923 | 0.96155 | 0.03845 |
| 2.08 | 0.98124 | 0.01876 | 0.96247 | 0.03753 |
| 2.09 | 0.98169 | 0.01831 | 0.96338 | 0.03662 |
| 2.10 | 0.98214 | 0.01786 | 0.96427 | 0.03573 |
| 2.11 | 0.98257 | 0.01743 | 0.96514 | 0.03486 |
| 2.12 | 0.98300 | 0.01700 | 0.96599 | 0.03401 |
| 2.13 | 0.98341 | 0.01659 | 0.96683 | 0.03317 |
| 2.14 | 0.98382 | 0.01618 | 0.96765 | 0.03235 |
| 2.15 | 0.98422 | 0.01578 | 0.96844 | 0.03156 |
| 2.16 | 0.98461 | 0.01539 | 0.96923 | 0.03077 |
| 2.17 | 0.98500 | 0.01500 | 0.96999 | 0.03001 |
| 2.18 | 0.98537 | 0.01463 | 0.97074 | 0.02926 |
| 2.19 | 0.98574 | 0.01426 | 0.97148 | 0.02852 |
| 2.20 | 0.98610 | 0.01390 | 0.97219 | 0.02781 |
| 2.21 | 0.98645 | 0.01355 | 0.97289 | 0.02711 |
| 2.22 | 0.98679 | 0.01321 | 0.97358 | 0.02642 |
| 2.23 | 0.98713 | 0.01287 | 0.97425 | 0.02575 |
| 2.24 | 0.98745 | 0.01255 | 0.97491 | 0.02509 |
| 2.25 | 0.98778 | 0.01222 | 0.97555 | 0.02445 |
| 2.26 | 0.98809 | 0.01191 | 0.97618 | 0.02382 |
| 2.27 | 0.98840 | 0.01160 | 0.97679 | 0.02321 |
| 2.28 | 0.98870 | 0.01130 | 0.97739 | 0.02261 |
| 2.29 | 0.98899 | 0.01101 | 0.97798 | 0.02202 |
| 2.30 | 0.98928 | 0.01072 | 0.97855 | 0.02145 |
| 2.31 | 0.98956 | 0.01044 | 0.97911 | 0.02089 |
| 2.32 | 0.98983 | 0.01017 | 0.97966 | 0.02034 |
| 2.33 | 0.99010 | 0.00990 | 0.98019 | 0.01981 |
| 2.34 | 0.99036 | 0.00964 | 0.98072 | 0.01928 |

| z | $P(Z < z)$ | $P(Z > z)$ | $P(-z < Z < z)$ | $P(Z < -z \text{ or } Z > z)$ |
|------|------------|------------|-----------------|-------------------------------|
| 2.35 | 0.99061 | 0.00939 | 0.98123 | 0.01877 |
| 2.36 | 0.99086 | 0.00914 | 0.98173 | 0.01827 |
| 2.37 | 0.99111 | 0.00889 | 0.98221 | 0.01779 |
| 2.38 | 0.99134 | 0.00866 | 0.98269 | 0.01731 |
| 2.39 | 0.99158 | 0.00842 | 0.98315 | 0.01685 |
| 2.40 | 0.99180 | 0.00820 | 0.98360 | 0.01640 |
| 2.41 | 0.99202 | 0.00798 | 0.98405 | 0.01595 |
| 2.42 | 0.99224 | 0.00776 | 0.98448 | 0.01552 |
| 2.43 | 0.99245 | 0.00755 | 0.98490 | 0.01510 |
| 2.44 | 0.99266 | 0.00734 | 0.98531 | 0.01469 |
| 2.45 | 0.99286 | 0.00714 | 0.98571 | 0.01429 |
| 2.46 | 0.99305 | 0.00695 | 0.98611 | 0.01389 |
| 2.47 | 0.99324 | 0.00676 | 0.98649 | 0.01351 |
| 2.48 | 0.99343 | 0.00657 | 0.98686 | 0.01314 |
| 2.49 | 0.99361 | 0.00639 | 0.98723 | 0.01277 |
| 2.50 | 0.99379 | 0.00621 | 0.98758 | 0.01242 |
| 2.51 | 0.99396 | 0.00604 | 0.98793 | 0.01207 |
| 2.52 | 0.99413 | 0.00587 | 0.98826 | 0.01174 |
| 2.53 | 0.99430 | 0.00570 | 0.98859 | 0.01141 |
| 2.54 | 0.99446 | 0.00554 | 0.98891 | 0.01109 |
| 2.55 | 0.99461 | 0.00539 | 0.98923 | 0.01077 |
| 2.56 | 0.99477 | 0.00523 | 0.98953 | 0.01047 |
| 2.57 | 0.99492 | 0.00508 | 0.98983 | 0.01017 |
| 2.58 | 0.99506 | 0.00494 | 0.99012 | 0.00988 |
| 2.59 | 0.99520 | 0.00480 | 0.99040 | 0.00960 |
| 2.60 | 0.99534 | 0.00466 | 0.99068 | 0.00932 |
| 2.61 | 0.99547 | 0.00453 | 0.99095 | 0.00905 |
| 2.62 | 0.99560 | 0.00440 | 0.99121 | 0.00879 |
| 2.63 | 0.99573 | 0.00427 | 0.99146 | 0.00854 |
| 2.64 | 0.99585 | 0.00415 | 0.99171 | 0.00829 |
| 2.65 | 0.99598 | 0.00402 | 0.99195 | 0.00805 |
| 2.66 | 0.99609 | 0.00391 | 0.99219 | 0.00781 |
| 2.67 | 0.99621 | 0.00379 | 0.99241 | 0.00759 |
| 2.68 | 0.99632 | 0.00368 | 0.99264 | 0.00736 |
| 2.69 | 0.99643 | 0.00357 | 0.99285 | 0.00715 |
| 2.70 | 0.99653 | 0.00347 | 0.99307 | 0.00693 |
| 2.71 | 0.99664 | 0.00336 | 0.99327 | 0.00673 |
| 2.72 | 0.99674 | 0.00326 | 0.99347 | 0.00653 |
| 2.73 | 0.99683 | 0.00317 | 0.99367 | 0.00633 |
| 2.74 | 0.99693 | 0.00307 | 0.99386 | 0.00614 |
| 2.75 | 0.99702 | 0.00298 | 0.99404 | 0.00596 |
| 2.76 | 0.99711 | 0.00289 | 0.99422 | 0.00578 |
| 2.77 | 0.99720 | 0.00280 | 0.99439 | 0.00561 |
| 2.78 | 0.99728 | 0.00272 | 0.99456 | 0.00544 |
| 2.79 | 0.99736 | 0.00264 | 0.99473 | 0.00527 |
| 2.80 | 0.99744 | 0.00256 | 0.99489 | 0.00511 |
| 2.81 | 0.99752 | 0.00248 | 0.99505 | 0.00495 |
| 2.82 | 0.99760 | 0.00240 | 0.99520 | 0.00480 |
| 2.83 | 0.99767 | 0.00233 | 0.99535 | 0.00465 |

| z | $P(Z < z)$ | $P(Z > z)$ | $P(-z < Z < z)$ | $P(Z < -z \text{ or } Z > z)$ |
|------|------------|------------|-----------------|-------------------------------|
| 2.84 | 0.99774 | 0.00226 | 0.99549 | 0.00451 |
| 2.85 | 0.99781 | 0.00219 | 0.99563 | 0.00437 |
| 2.86 | 0.99788 | 0.00212 | 0.99576 | 0.00424 |
| 2.87 | 0.99795 | 0.00205 | 0.99590 | 0.00410 |
| 2.88 | 0.99801 | 0.00199 | 0.99602 | 0.00398 |
| 2.89 | 0.99807 | 0.00193 | 0.99615 | 0.00385 |
| 2.90 | 0.99813 | 0.00187 | 0.99627 | 0.00373 |
| 2.91 | 0.99819 | 0.00181 | 0.99639 | 0.00361 |
| 2.92 | 0.99825 | 0.00175 | 0.99650 | 0.00350 |
| 2.93 | 0.99831 | 0.00169 | 0.99661 | 0.00339 |
| 2.94 | 0.99836 | 0.00164 | 0.99672 | 0.00328 |
| 2.95 | 0.99841 | 0.00159 | 0.99682 | 0.00318 |
| 2.96 | 0.99846 | 0.00154 | 0.99692 | 0.00308 |
| 2.97 | 0.99851 | 0.00149 | 0.99702 | 0.00298 |
| 2.98 | 0.99856 | 0.00144 | 0.99712 | 0.00288 |
| 2.99 | 0.99861 | 0.00139 | 0.99721 | 0.00279 |
| 3.00 | 0.99865 | 0.00135 | 0.99730 | 0.00270 |
| 3.01 | 0.99869 | 0.00131 | 0.99739 | 0.00261 |
| 3.02 | 0.99874 | 0.00126 | 0.99747 | 0.00253 |
| 3.03 | 0.99878 | 0.00122 | 0.99755 | 0.00245 |
| 3.04 | 0.99882 | 0.00118 | 0.99763 | 0.00237 |
| 3.05 | 0.99886 | 0.00114 | 0.99771 | 0.00229 |
| 3.06 | 0.99889 | 0.00111 | 0.99779 | 0.00221 |
| 3.07 | 0.99893 | 0.00107 | 0.99786 | 0.00214 |
| 3.08 | 0.99896 | 0.00104 | 0.99793 | 0.00207 |
| 3.09 | 0.99900 | 0.00100 | 0.99800 | 0.00200 |
| 3.10 | 0.99903 | 0.00097 | 0.99806 | 0.00194 |
| 3.11 | 0.99906 | 0.00094 | 0.99813 | 0.00187 |
| 3.12 | 0.99910 | 0.00090 | 0.99819 | 0.00181 |
| 3.13 | 0.99913 | 0.00087 | 0.99825 | 0.00175 |
| 3.14 | 0.99916 | 0.00084 | 0.99831 | 0.00169 |
| 3.15 | 0.99918 | 0.00082 | 0.99837 | 0.00163 |
| 3.16 | 0.99921 | 0.00079 | 0.99842 | 0.00158 |
| 3.17 | 0.99924 | 0.00076 | 0.99848 | 0.00152 |
| 3.18 | 0.99926 | 0.00074 | 0.99853 | 0.00147 |
| 3.19 | 0.99929 | 0.00071 | 0.99858 | 0.00142 |
| 3.20 | 0.99931 | 0.00069 | 0.99863 | 0.00137 |
| 3.21 | 0.99934 | 0.00066 | 0.99867 | 0.00133 |
| 3.22 | 0.99936 | 0.00064 | 0.99872 | 0.00128 |
| 3.23 | 0.99938 | 0.00062 | 0.99876 | 0.00124 |
| 3.24 | 0.99940 | 0.00060 | 0.99880 | 0.00120 |
| 3.25 | 0.99942 | 0.00058 | 0.99885 | 0.00115 |
| 3.26 | 0.99944 | 0.00056 | 0.99889 | 0.00111 |
| 3.27 | 0.99946 | 0.00054 | 0.99892 | 0.00108 |
| 3.28 | 0.99948 | 0.00052 | 0.99896 | 0.00104 |
| 3.29 | 0.99950 | 0.00050 | 0.99900 | 0.00100 |
| 3.30 | 0.99952 | 0.00048 | 0.99903 | 0.00097 |
| 3.31 | 0.99953 | 0.00047 | 0.99907 | 0.00093 |
| 3.32 | 0.99955 | 0.00045 | 0.99910 | 0.00090 |

| z | $P(Z < z)$ | $P(Z > z)$ | $P(-z < Z < z)$ | $P(Z < -z \text{ or } Z > z)$ |
|------|------------|------------|-----------------|-------------------------------|
| 3.33 | 0.99957 | 0.00043 | 0.99913 | 0.00087 |
| 3.34 | 0.99958 | 0.00042 | 0.99916 | 0.00084 |
| 3.35 | 0.99960 | 0.00040 | 0.99919 | 0.00081 |
| 3.36 | 0.99961 | 0.00039 | 0.99922 | 0.00078 |
| 3.37 | 0.99962 | 0.00038 | 0.99925 | 0.00075 |
| 3.38 | 0.99964 | 0.00036 | 0.99928 | 0.00072 |
| 3.39 | 0.99965 | 0.00035 | 0.99930 | 0.00070 |
| 3.40 | 0.99966 | 0.00034 | 0.99933 | 0.00067 |
| 3.41 | 0.99968 | 0.00032 | 0.99935 | 0.00065 |
| 3.42 | 0.99969 | 0.00031 | 0.99937 | 0.00063 |
| 3.43 | 0.99970 | 0.00030 | 0.99940 | 0.00060 |
| 3.44 | 0.99971 | 0.00029 | 0.99942 | 0.00058 |
| 3.45 | 0.99972 | 0.00028 | 0.99944 | 0.00056 |
| 3.46 | 0.99973 | 0.00027 | 0.99946 | 0.00054 |
| 3.47 | 0.99974 | 0.00026 | 0.99948 | 0.00052 |
| 3.48 | 0.99975 | 0.00025 | 0.99950 | 0.00050 |
| 3.49 | 0.99976 | 0.00024 | 0.99952 | 0.00048 |
| 3.50 | 0.99977 | 0.00023 | 0.99953 | 0.00047 |
| 3.51 | 0.99978 | 0.00022 | 0.99955 | 0.00045 |
| 3.52 | 0.99978 | 0.00022 | 0.99957 | 0.00043 |
| 3.53 | 0.99979 | 0.00021 | 0.99958 | 0.00042 |
| 3.54 | 0.99980 | 0.00020 | 0.99960 | 0.00040 |
| 3.55 | 0.99981 | 0.00019 | 0.99961 | 0.00039 |
| 3.56 | 0.99981 | 0.00019 | 0.99963 | 0.00037 |
| 3.57 | 0.99982 | 0.00018 | 0.99964 | 0.00036 |
| 3.58 | 0.99983 | 0.00017 | 0.99966 | 0.00034 |
| 3.59 | 0.99983 | 0.00017 | 0.99967 | 0.00033 |
| 3.60 | 0.99984 | 0.00016 | 0.99968 | 0.00032 |
| 3.80 | 0.99993 | 0.00007 | 0.99986 | 0.00014 |
| 3.82 | 0.99993 | 0.00007 | 0.99987 | 0.00013 |
| 3.84 | 0.99994 | 0.00006 | 0.99988 | 0.00012 |
| 3.86 | 0.99994 | 0.00006 | 0.99989 | 0.00011 |
| 3.88 | 0.99995 | 0.00005 | 0.99990 | 0.00010 |
| 3.90 | 0.99995 | 0.00005 | 0.99990 | 0.00010 |
| 3.92 | 0.99996 | 0.00004 | 0.99991 | 0.00009 |
| 3.94 | 0.99996 | 0.00004 | 0.99992 | 0.00008 |
| 3.96 | 0.99996 | 0.00004 | 0.99993 | 0.00007 |
| 3.98 | 0.99997 | 0.00003 | 0.99993 | 0.00007 |
| 4.00 | 0.99997 | 0.00003 | 0.99994 | 0.00006 |
| 4.02 | 0.99997 | 0.00003 | 0.99994 | 0.00006 |
| 4.04 | 0.99997 | 0.00003 | 0.99995 | 0.00005 |
| 4.06 | 0.99998 | 0.00002 | 0.99995 | 0.00005 |
| 4.08 | 0.99998 | 0.00002 | 0.99995 | 0.00005 |
| 4.10 | 0.99998 | 0.00002 | 0.99996 | 0.00004 |
| 4.12 | 0.99998 | 0.00002 | 0.99996 | 0.00004 |
| 4.14 | 0.99998 | 0.00002 | 0.99997 | 0.00003 |
| 4.16 | 0.99998 | 0.00002 | 0.99997 | 0.00003 |
| 4.18 | 0.99999 | 0.00001 | 0.99997 | 0.00003 |
| 4.20 | 0.99999 | 0.00001 | 0.99997 | 0.00003 |

| z | $P(Z < z)$ | $P(Z > z)$ | $P(-z < Z < z)$ | $P(Z < -z \text{ or } Z > z)$ |
|------|------------|------------|-----------------|-------------------------------|
| 4.22 | 0.99999 | 0.00001 | 0.99998 | 0.00002 |
| 4.24 | 0.99999 | 0.00001 | 0.99998 | 0.00002 |
| 4.26 | 0.99999 | 0.00001 | 0.99998 | 0.00002 |
| 4.28 | 0.99999 | 0.00001 | 0.99998 | 0.00002 |
| 4.30 | 0.99999 | 0.00001 | 0.99998 | 0.00002 |
| 4.32 | 0.99999 | 0.00001 | 0.99998 | 0.00002 |
| 4.34 | 0.99999 | 0.00001 | 0.99999 | 0.00001 |
| 4.36 | 0.99999 | 0.00001 | 0.99999 | 0.00001 |
| 4.38 | 0.99999 | 0.00001 | 0.99999 | 0.00001 |
| 4.40 | 0.99999 | 0.00001 | 0.99999 | 0.00001 |
| 4.42 | 1.00000 | 0.00000 | 0.99999 | 0.00001 |
| 4.44 | 1.00000 | 0.00000 | 0.99999 | 0.00001 |
| 4.46 | 1.00000 | 0.00000 | 0.99999 | 0.00001 |
| 4.48 | 1.00000 | 0.00000 | 0.99999 | 0.00001 |
| 4.50 | 1.00000 | 0.00000 | 0.99999 | 0.00001 |
| 4.52 | 1.00000 | 0.00000 | 0.99999 | 0.00001 |
| 4.54 | 1.00000 | 0.00000 | 0.99999 | 0.00001 |
| 4.56 | 1.00000 | 0.00000 | 0.99999 | 0.00001 |
| 4.58 | 1.00000 | 0.00000 | 1.00000 | 0.00000 |
| 4.60 | 1.00000 | 0.00000 | 1.00000 | 0.00000 |

Appendix 2

Percentiles of t distributions

| Degrees of freedom (df) | Area in the symmetric central region $P(-t < T < t)$ | | | | |
|----------------------------|--|-------|-------|-------|-------|
| | Area to the left of t : $P(T < t)$ | | | | |
| | 0.80 | 0.90 | 0.95 | 0.975 | 0.99 |
| 1 | 3.078 | 6.314 | 12.71 | 63.66 | 636.6 |
| 2 | 1.886 | 2.920 | 4.303 | 9.925 | 31.60 |
| 3 | 1.638 | 2.353 | 3.182 | 5.841 | 12.92 |
| 4 | 1.533 | 2.132 | 2.776 | 4.604 | 8.610 |
| 5 | 1.476 | 2.015 | 2.571 | 4.032 | 6.869 |
| 6 | 1.440 | 1.943 | 2.447 | 3.707 | 5.959 |
| 7 | 1.415 | 1.895 | 2.365 | 3.499 | 5.408 |
| 8 | 1.397 | 1.860 | 2.306 | 3.355 | 5.041 |
| 9 | 1.383 | 1.833 | 2.262 | 3.250 | 4.781 |
| 10 | 1.372 | 1.812 | 2.228 | 3.169 | 4.587 |
| 11 | 1.363 | 1.796 | 2.201 | 3.106 | 4.437 |
| 12 | 1.356 | 1.782 | 2.179 | 3.055 | 4.318 |
| 13 | 1.350 | 1.771 | 2.160 | 3.012 | 4.221 |
| 14 | 1.345 | 1.761 | 2.145 | 2.977 | 4.140 |
| 15 | 1.341 | 1.753 | 2.131 | 2.947 | 4.073 |
| 16 | 1.337 | 1.746 | 2.120 | 2.921 | 4.015 |
| 17 | 1.333 | 1.740 | 2.110 | 2.898 | 3.965 |
| 18 | 1.330 | 1.734 | 2.101 | 2.878 | 3.922 |
| 19 | 1.328 | 1.729 | 2.093 | 2.861 | 3.883 |
| 20 | 1.325 | 1.725 | 2.086 | 2.845 | 3.850 |
| 21 | 1.323 | 1.721 | 2.080 | 2.831 | 3.819 |
| 22 | 1.321 | 1.717 | 2.074 | 2.819 | 3.792 |
| 23 | 1.319 | 1.714 | 2.069 | 2.807 | 3.768 |
| 24 | 1.318 | 1.711 | 2.064 | 2.797 | 3.745 |
| 25 | 1.316 | 1.708 | 2.060 | 2.787 | 3.725 |
| 26 | 1.315 | 1.706 | 2.056 | 2.779 | 3.707 |
| 27 | 1.314 | 1.703 | 2.052 | 2.771 | 3.690 |
| 28 | 1.313 | 1.701 | 2.048 | 2.763 | 3.674 |
| 29 | 1.311 | 1.699 | 2.045 | 2.756 | 3.659 |
| 30 | 1.310 | 1.697 | 2.042 | 2.750 | 3.646 |
| 31 | 1.309 | 1.696 | 2.040 | 2.744 | 3.633 |
| 32 | 1.309 | 1.694 | 2.037 | 2.738 | 3.622 |
| 33 | 1.308 | 1.692 | 2.035 | 2.733 | 3.611 |
| 34 | 1.307 | 1.691 | 2.032 | 2.728 | 3.601 |
| 35 | 1.306 | 1.690 | 2.030 | 2.724 | 3.591 |

| Degrees of freedom (df) | Area in the symmetric central region $P(-t < T < t)$ | | | | |
|----------------------------|--|-------|-------|-------|-------|
| | Area to the left of t : $P(T < t)$ | | | | |
| | 0.80 | 0.90 | 0.95 | 0.975 | 0.99 |
| 36 | 1.306 | 1.688 | 2.028 | 2.719 | 3.582 |
| 37 | 1.305 | 1.687 | 2.026 | 2.715 | 3.574 |
| 38 | 1.304 | 1.686 | 2.024 | 2.712 | 3.566 |
| 39 | 1.304 | 1.685 | 2.023 | 2.708 | 3.558 |
| 40 | 1.303 | 1.684 | 2.021 | 2.704 | 3.551 |
| 45 | 1.301 | 1.679 | 2.014 | 2.690 | 3.520 |
| 50 | 1.299 | 1.676 | 2.009 | 2.678 | 3.496 |
| 60 | 1.296 | 1.671 | 2.000 | 2.660 | 3.460 |
| 70 | 1.294 | 1.667 | 1.994 | 2.648 | 3.435 |
| 80 | 1.292 | 1.664 | 1.990 | 2.639 | 3.416 |
| 90 | 1.291 | 1.662 | 1.987 | 2.632 | 3.402 |
| 100 | 1.290 | 1.660 | 1.984 | 2.626 | 3.390 |
| 120 | 1.289 | 1.658 | 1.980 | 2.617 | 3.373 |
| 140 | 1.288 | 1.656 | 1.977 | 2.611 | 3.361 |
| 160 | 1.287 | 1.654 | 1.975 | 2.60 | 3.352 |
| 180 | 1.286 | 1.653 | 1.973 | 2.603 | 3.345 |
| 200 | 1.286 | 1.653 | 1.972 | 2.601 | 3.340 |
| 220 | 1.285 | 1.652 | 1.971 | 2.598 | 3.335 |
| 240 | 1.285 | 1.651 | 1.970 | 2.596 | 3.332 |
| 260 | 1.285 | 1.651 | 1.969 | 2.595 | 3.328 |
| 280 | 1.285 | 1.650 | 1.968 | 2.594 | 3.326 |
| 300 | 1.284 | 1.650 | 1.968 | 2.592 | 3.323 |

Appendix 3

Percentiles of χ^2 distributions

| Degrees of freedom (df) | Area to the left of X^2 : $P[X < X^2]$ | | | |
|----------------------------|--|--------|--------|--------|
| | 0.90 | 0.95 | 0.99 | 0.999 |
| 1 | 2.706 | 3.841 | 6.635 | 10.828 |
| 2 | 4.605 | 5.991 | 9.210 | 13.816 |
| 3 | 6.251 | 7.815 | 11.345 | 16.266 |
| 4 | 7.779 | 9.488 | 13.277 | 18.467 |
| 5 | 9.236 | 11.070 | 15.086 | 20.515 |
| 6 | 10.645 | 12.592 | 16.812 | 22.458 |
| 7 | 12.017 | 14.067 | 18.475 | 24.322 |
| 8 | 13.362 | 15.507 | 20.090 | 26.124 |
| 9 | 14.684 | 16.919 | 21.666 | 27.877 |
| 10 | 15.987 | 18.307 | 23.209 | 29.588 |
| 11 | 17.275 | 19.675 | 24.725 | 31.264 |
| 12 | 18.549 | 21.026 | 26.217 | 32.909 |
| 13 | 19.812 | 22.362 | 27.688 | 34.528 |
| 14 | 21.064 | 23.685 | 29.141 | 36.123 |
| 15 | 22.307 | 24.996 | 30.578 | 37.697 |
| 16 | 23.542 | 26.296 | 32.000 | 39.252 |
| 17 | 24.769 | 27.587 | 33.409 | 40.790 |
| 18 | 25.989 | 28.869 | 34.805 | 42.312 |
| 19 | 27.204 | 30.144 | 36.191 | 43.820 |
| 20 | 28.412 | 31.410 | 37.566 | 45.315 |
| 21 | 29.615 | 32.671 | 38.932 | 46.797 |
| 22 | 30.813 | 33.924 | 40.289 | 48.268 |
| 23 | 32.007 | 35.172 | 41.638 | 49.728 |
| 24 | 33.196 | 36.415 | 42.980 | 51.179 |
| 25 | 34.382 | 37.652 | 44.314 | 52.620 |
| 26 | 35.563 | 38.885 | 45.642 | 54.052 |
| 27 | 36.741 | 40.113 | 46.963 | 55.476 |
| 28 | 37.916 | 41.337 | 48.278 | 56.892 |
| 29 | 39.087 | 42.557 | 49.588 | 58.301 |
| 30 | 40.256 | 43.773 | 50.892 | 59.703 |
| 35 | 46.059 | 49.802 | 57.342 | 66.619 |
| 40 | 51.805 | 55.758 | 63.691 | 73.402 |
| 45 | 57.505 | 61.656 | 69.957 | 80.077 |
| 50 | 63.167 | 67.505 | 76.154 | 86.661 |
| 55 | 68.796 | 73.311 | 82.292 | 93.168 |
| 60 | 74.397 | 79.082 | 88.379 | 99.607 |
| 70 | 85.527 | 90.531 | 100.43 | 112.32 |

| Degrees of freedom (df) | Area to the left of X^2 : $P(X < X^2)$ | | | |
|----------------------------|--|--------|--------|--------|
| | 0.90 | 0.95 | 0.99 | 0.999 |
| 80 | 96.578 | 101.88 | 112.33 | 124.84 |
| 90 | 107.57 | 113.15 | 124.12 | 137.21 |
| 100 | 118.50 | 124.34 | 135.81 | 149.45 |
| 110 | 129.39 | 135.48 | 147.41 | 161.58 |
| 120 | 140.23 | 146.57 | 158.95 | 173.62 |
| 130 | 151.05 | 157.61 | 170.42 | 185.57 |
| 140 | 161.83 | 168.61 | 181.84 | 197.45 |
| 150 | 172.58 | 179.58 | 193.21 | 209.26 |
| 160 | 183.31 | 190.52 | 204.53 | 221.02 |
| 170 | 194.02 | 201.42 | 215.81 | 232.72 |
| 180 | 204.70 | 212.30 | 227.06 | 244.37 |
| 190 | 215.37 | 223.16 | 238.27 | 255.98 |
| 200 | 226.02 | 233.99 | 249.45 | 267.54 |

Appendix 4

Percentiles of F distributions ($\alpha = 0.05$)

| (ddf) | Numerator degrees of freedom (ndf) | | | | | | | | |
|-------|------------------------------------|-------|-------|-------|-------|-------|-------|-------|-------|
| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 1 | 161.4 | 199.5 | 215.7 | 224.6 | 230.2 | 234.0 | 236.8 | 238.9 | 240.5 |
| 2 | 18.51 | 19.00 | 19.16 | 19.25 | 19.30 | 19.33 | 19.35 | 19.37 | 19.38 |
| 3 | 10.13 | 9.55 | 9.28 | 9.12 | 9.01 | 8.94 | 8.89 | 8.85 | 8.81 |
| 4 | 7.71 | 6.94 | 6.59 | 6.39 | 6.26 | 6.16 | 6.09 | 6.04 | 6.00 |
| 5 | 6.61 | 5.79 | 5.41 | 5.19 | 5.05 | 4.95 | 4.88 | 4.82 | 4.77 |
| 6 | 5.99 | 5.14 | 4.76 | 4.53 | 4.39 | 4.28 | 4.21 | 4.15 | 4.10 |
| 7 | 5.59 | 4.74 | 4.35 | 4.12 | 3.97 | 3.87 | 3.79 | 3.73 | 3.68 |
| 8 | 5.32 | 4.46 | 4.07 | 3.84 | 3.69 | 3.58 | 3.50 | 3.44 | 3.39 |
| 9 | 5.12 | 4.26 | 3.86 | 3.63 | 3.48 | 3.37 | 3.29 | 3.23 | 3.18 |
| 10 | 4.96 | 4.10 | 3.71 | 3.48 | 3.33 | 3.22 | 3.14 | 3.07 | 3.02 |
| 11 | 4.84 | 3.98 | 3.59 | 3.36 | 3.20 | 3.09 | 3.01 | 2.95 | 2.90 |
| 12 | 4.75 | 3.89 | 3.49 | 3.26 | 3.11 | 3.00 | 2.91 | 2.85 | 2.80 |
| 13 | 4.67 | 3.81 | 3.41 | 3.18 | 3.03 | 2.92 | 2.83 | 2.77 | 2.71 |
| 14 | 4.60 | 3.74 | 3.34 | 3.11 | 2.96 | 2.85 | 2.76 | 2.70 | 2.65 |
| 15 | 4.54 | 3.68 | 3.29 | 3.06 | 2.90 | 2.79 | 2.71 | 2.64 | 2.59 |
| 16 | 4.49 | 3.63 | 3.24 | 3.01 | 2.85 | 2.74 | 2.66 | 2.59 | 2.54 |
| 17 | 4.45 | 3.59 | 3.20 | 2.96 | 2.81 | 2.70 | 2.61 | 2.55 | 2.49 |
| 18 | 4.41 | 3.55 | 3.16 | 2.93 | 2.77 | 2.66 | 2.58 | 2.51 | 2.46 |
| 19 | 4.38 | 3.52 | 3.13 | 2.90 | 2.74 | 2.63 | 2.54 | 2.48 | 2.42 |
| 20 | 4.35 | 3.49 | 3.10 | 2.87 | 2.71 | 2.60 | 2.51 | 2.45 | 2.39 |
| 21 | 4.32 | 3.47 | 3.07 | 2.84 | 2.68 | 2.57 | 2.49 | 2.42 | 2.37 |
| 22 | 4.30 | 3.44 | 3.05 | 2.82 | 2.66 | 2.55 | 2.46 | 2.40 | 2.34 |
| 23 | 4.28 | 3.42 | 3.03 | 2.80 | 2.64 | 2.53 | 2.44 | 2.37 | 2.32 |
| 24 | 4.26 | 3.40 | 3.01 | 2.78 | 2.62 | 2.51 | 2.42 | 2.36 | 2.30 |
| 25 | 4.24 | 3.39 | 2.99 | 2.76 | 2.60 | 2.49 | 2.40 | 2.34 | 2.28 |
| 26 | 4.23 | 3.37 | 2.98 | 2.74 | 2.59 | 2.47 | 2.39 | 2.32 | 2.27 |
| 27 | 4.21 | 3.35 | 2.96 | 2.73 | 2.57 | 2.46 | 2.37 | 2.31 | 2.25 |
| 28 | 4.20 | 3.34 | 2.95 | 2.71 | 2.56 | 2.45 | 2.36 | 2.29 | 2.24 |
| 29 | 4.18 | 3.33 | 2.93 | 2.70 | 2.55 | 2.43 | 2.35 | 2.28 | 2.22 |
| 30 | 4.17 | 3.32 | 2.92 | 2.69 | 2.53 | 2.42 | 2.33 | 2.27 | 2.21 |
| 40 | 4.08 | 3.23 | 2.84 | 2.61 | 2.45 | 2.34 | 2.25 | 2.18 | 2.12 |
| 50 | 4.03 | 3.18 | 2.79 | 2.56 | 2.40 | 2.29 | 2.20 | 2.13 | 2.07 |
| 60 | 4.00 | 3.15 | 2.76 | 2.53 | 2.37 | 2.25 | 2.17 | 2.10 | 2.04 |
| 70 | 3.98 | 3.13 | 2.74 | 2.50 | 2.35 | 2.23 | 2.14 | 2.07 | 2.02 |
| 80 | 3.96 | 3.11 | 2.72 | 2.49 | 2.33 | 2.21 | 2.13 | 2.06 | 2.00 |
| 90 | 3.95 | 3.10 | 2.71 | 2.47 | 2.32 | 2.20 | 2.11 | 2.04 | 1.99 |
| 100 | 3.94 | 3.09 | 2.70 | 2.46 | 2.31 | 2.19 | 2.10 | 2.03 | 1.97 |
| 110 | 3.93 | 3.08 | 2.69 | 2.45 | 2.30 | 2.18 | 2.09 | 2.02 | 1.97 |
| 120 | 3.92 | 3.07 | 2.68 | 2.45 | 2.29 | 2.18 | 2.09 | 2.02 | 1.96 |

| (ddf) | Numerator degrees of freedom (ndf) | | | | | | | | | | |
|-------|------------------------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| | 10 | 12 | 15 | 20 | 25 | 30 | 40 | 60 | 80 | 100 | 120 |
| 1 | 241.9 | 243.9 | 245.9 | 248.0 | 249.3 | 250.1 | 251.1 | 252.2 | 252.7 | 253.0 | 253.3 |
| 2 | 19.40 | 19.41 | 19.43 | 19.45 | 19.46 | 19.46 | 19.47 | 19.48 | 19.48 | 19.49 | 19.49 |
| 3 | 8.79 | 8.74 | 8.70 | 8.66 | 8.63 | 8.62 | 8.59 | 8.57 | 8.56 | 8.55 | 8.55 |
| 4 | 5.96 | 5.91 | 5.86 | 5.80 | 5.77 | 5.75 | 5.72 | 5.69 | 5.67 | 5.66 | 5.66 |
| 5 | 4.74 | 4.68 | 4.62 | 4.56 | 4.52 | 4.50 | 4.46 | 4.43 | 4.41 | 4.41 | 4.40 |
| 6 | 4.06 | 4.00 | 3.94 | 3.87 | 3.83 | 3.81 | 3.77 | 3.74 | 3.72 | 3.71 | 3.70 |
| 7 | 3.64 | 3.57 | 3.51 | 3.44 | 3.40 | 3.38 | 3.34 | 3.30 | 3.29 | 3.27 | 3.27 |
| 8 | 3.35 | 3.28 | 3.22 | 3.15 | 3.11 | 3.08 | 3.04 | 3.01 | 2.99 | 2.97 | 2.97 |
| 9 | 3.14 | 3.07 | 3.01 | 2.94 | 2.89 | 2.86 | 2.83 | 2.79 | 2.77 | 2.76 | 2.75 |
| 10 | 2.98 | 2.91 | 2.85 | 2.77 | 2.73 | 2.70 | 2.66 | 2.62 | 2.60 | 2.59 | 2.58 |
| 11 | 2.85 | 2.79 | 2.72 | 2.65 | 2.60 | 2.57 | 2.53 | 2.49 | 2.47 | 2.46 | 2.45 |
| 12 | 2.75 | 2.69 | 2.62 | 2.54 | 2.50 | 2.47 | 2.43 | 2.38 | 2.36 | 2.35 | 2.34 |
| 13 | 2.67 | 2.60 | 2.53 | 2.46 | 2.41 | 2.38 | 2.34 | 2.30 | 2.27 | 2.26 | 2.25 |
| 14 | 2.60 | 2.53 | 2.46 | 2.39 | 2.34 | 2.31 | 2.27 | 2.22 | 2.20 | 2.19 | 2.18 |
| 15 | 2.54 | 2.48 | 2.40 | 2.33 | 2.28 | 2.25 | 2.20 | 2.16 | 2.14 | 2.12 | 2.11 |
| 16 | 2.49 | 2.42 | 2.35 | 2.28 | 2.23 | 2.19 | 2.15 | 2.11 | 2.08 | 2.07 | 2.06 |
| 17 | 2.45 | 2.38 | 2.31 | 2.23 | 2.18 | 2.15 | 2.10 | 2.06 | 2.03 | 2.02 | 2.01 |
| 18 | 2.41 | 2.34 | 2.27 | 2.19 | 2.14 | 2.11 | 2.06 | 2.02 | 1.99 | 1.98 | 1.97 |
| 19 | 2.38 | 2.31 | 2.23 | 2.16 | 2.11 | 2.07 | 2.03 | 1.98 | 1.96 | 1.94 | 1.93 |
| 20 | 2.35 | 2.28 | 2.20 | 2.12 | 2.07 | 2.04 | 1.99 | 1.95 | 1.92 | 1.91 | 1.90 |
| 21 | 2.32 | 2.25 | 2.18 | 2.10 | 2.05 | 2.01 | 1.96 | 1.92 | 1.89 | 1.88 | 1.87 |
| 22 | 2.30 | 2.23 | 2.15 | 2.07 | 2.02 | 1.98 | 1.94 | 1.89 | 1.86 | 1.85 | 1.84 |
| 23 | 2.27 | 2.20 | 2.13 | 2.05 | 2.00 | 1.96 | 1.91 | 1.86 | 1.84 | 1.82 | 1.81 |
| 24 | 2.25 | 2.18 | 2.11 | 2.03 | 1.97 | 1.94 | 1.89 | 1.84 | 1.82 | 1.80 | 1.79 |
| 25 | 2.24 | 2.16 | 2.09 | 2.01 | 1.96 | 1.92 | 1.87 | 1.82 | 1.80 | 1.78 | 1.77 |
| 26 | 2.22 | 2.15 | 2.07 | 1.99 | 1.94 | 1.90 | 1.85 | 1.80 | 1.78 | 1.76 | 1.75 |
| 27 | 2.20 | 2.13 | 2.06 | 1.97 | 1.92 | 1.88 | 1.84 | 1.79 | 1.76 | 1.74 | 1.73 |
| 28 | 2.19 | 2.12 | 2.04 | 1.96 | 1.91 | 1.87 | 1.82 | 1.77 | 1.74 | 1.73 | 1.71 |
| 29 | 2.18 | 2.10 | 2.03 | 1.94 | 1.89 | 1.85 | 1.81 | 1.75 | 1.73 | 1.71 | 1.70 |
| 30 | 2.16 | 2.09 | 2.01 | 1.93 | 1.88 | 1.84 | 1.79 | 1.74 | 1.71 | 1.70 | 1.68 |
| 40 | 2.08 | 2.00 | 1.92 | 1.84 | 1.78 | 1.74 | 1.69 | 1.64 | 1.61 | 1.59 | 1.58 |
| 50 | 2.03 | 1.95 | 1.87 | 1.78 | 1.73 | 1.69 | 1.63 | 1.58 | 1.54 | 1.52 | 1.51 |
| 60 | 1.99 | 1.92 | 1.84 | 1.75 | 1.69 | 1.65 | 1.59 | 1.53 | 1.50 | 1.48 | 1.47 |
| 70 | 1.97 | 1.89 | 1.81 | 1.72 | 1.66 | 1.62 | 1.57 | 1.50 | 1.47 | 1.45 | 1.44 |
| 80 | 1.95 | 1.88 | 1.79 | 1.70 | 1.64 | 1.60 | 1.54 | 1.48 | 1.45 | 1.43 | 1.41 |
| 90 | 1.94 | 1.86 | 1.78 | 1.69 | 1.63 | 1.59 | 1.53 | 1.46 | 1.43 | 1.41 | 1.39 |
| 100 | 1.93 | 1.85 | 1.77 | 1.68 | 1.62 | 1.57 | 1.52 | 1.45 | 1.41 | 1.39 | 1.38 |
| 110 | 1.92 | 1.84 | 1.76 | 1.67 | 1.61 | 1.56 | 1.50 | 1.44 | 1.40 | 1.38 | 1.36 |
| 120 | 1.91 | 1.83 | 1.75 | 1.66 | 1.60 | 1.55 | 1.50 | 1.43 | 1.39 | 1.37 | 1.35 |

Appendix 5

Values of q for Tukey's HSD test ($\alpha = 0.05$)

| v | 2 | 3 | α | 4 | 5 | 6 |
|-----|---------|---------|----------|---------|---------|---------|
| 4 | 3.92649 | 5.04024 | | 5.75706 | 6.28702 | 6.70644 |
| 5 | 3.63535 | 4.60166 | | 5.21848 | 5.67312 | 6.03290 |
| 6 | 3.46046 | 4.33902 | | 4.89559 | 5.30494 | 5.62855 |
| 7 | 3.34392 | 4.16483 | | 4.68124 | 5.06007 | 5.35909 |
| 8 | 3.26115 | 4.04101 | | 4.52880 | 4.88575 | 5.16723 |
| 9 | 3.19906 | 3.94850 | | 4.41490 | 4.75541 | 5.02352 |
| 10 | 3.15106 | 3.87676 | | 4.32658 | 4.65429 | 4.91202 |
| 11 | 3.11265 | 3.81952 | | 4.25609 | 4.57356 | 4.82295 |
| 12 | 3.08132 | 3.77278 | | 4.19852 | 4.50760 | 4.75015 |
| 13 | 3.05529 | 3.73414 | | 4.15087 | 4.45291 | 4.68970 |
| 14 | 3.03319 | 3.70139 | | 4.11051 | 4.40661 | 4.63854 |
| 15 | 3.01432 | 3.67338 | | 4.07597 | 4.36699 | 4.59474 |
| 16 | 2.99800 | 3.64914 | | 4.04609 | 4.33269 | 4.55681 |
| 17 | 2.98373 | 3.62796 | | 4.01999 | 4.30271 | 4.52365 |
| 18 | 2.97115 | 3.60930 | | 3.99698 | 4.27629 | 4.49442 |
| 19 | 2.95998 | 3.59274 | | 3.97655 | 4.25283 | 4.46846 |
| 20 | 2.95000 | 3.57794 | | 3.95829 | 4.23186 | 4.44524 |
| 21 | 2.94102 | 3.56463 | | 3.94188 | 4.21300 | 4.42436 |
| 22 | 2.93290 | 3.55259 | | 3.92704 | 4.19594 | 4.40547 |
| 23 | 2.92553 | 3.54167 | | 3.91356 | 4.18045 | 4.38831 |
| 24 | 2.91880 | 3.53170 | | 3.90126 | 4.16632 | 4.37265 |
| 25 | 2.91263 | 3.52257 | | 3.89000 | 4.15337 | 4.35831 |
| 26 | 2.90697 | 3.51417 | | 3.87964 | 4.14146 | 4.34511 |
| 27 | 2.90174 | 3.50643 | | 3.87009 | 4.13047 | 4.33294 |
| 28 | 2.89690 | 3.49918 | | 3.86125 | 4.12030 | 4.32167 |
| 29 | 2.89240 | 3.49263 | | 3.85304 | 4.11087 | 4.31121 |
| 30 | 2.88822 | 3.48651 | | 3.84540 | 4.10208 | 4.30147 |
| 31 | 2.88432 | 3.48065 | | 3.83828 | 4.09389 | 4.29238 |
| 32 | 2.88068 | 3.47525 | | 3.83162 | 4.08622 | 4.28389 |
| 33 | 2.87726 | 3.47019 | | 3.82537 | 4.07904 | 4.27592 |
| 34 | 2.87405 | 3.46544 | | 3.81951 | 4.07230 | 4.26844 |
| 35 | 2.87103 | 3.46097 | | 3.81400 | 4.06595 | 4.26141 |
| 36 | 2.86818 | 3.45676 | | 3.80880 | 4.05997 | 4.25477 |
| 37 | 2.86550 | 3.45278 | | 3.80389 | 4.05432 | 4.24851 |
| 38 | 2.86296 | 3.44902 | | 3.79925 | 4.04898 | 4.24258 |
| 39 | 2.86055 | 3.44546 | | 3.79486 | 4.04392 | 4.23697 |
| 40 | 2.85827 | 3.44208 | | 3.79069 | 4.03913 | 4.23165 |
| 41 | 2.85610 | 3.43888 | | 3.78673 | 4.03457 | 4.22659 |

| v | 2 | 3 | α | 4 | 5 | 6 |
|-----|---------|---------|----------|---------|---------|---|
| 42 | 2.85404 | 3.43582 | 3.78296 | 4.03024 | 4.22179 | |
| 43 | 2.85208 | 3.43292 | 3.77938 | 4.02611 | 4.21721 | |
| 44 | 2.85020 | 3.43015 | 3.77596 | 4.02217 | 4.21284 | |
| 45 | 2.84842 | 3.42751 | 3.77270 | 4.01842 | 4.20868 | |
| 46 | 2.84671 | 3.42499 | 3.76958 | 4.01483 | 4.20469 | |
| 47 | 2.84508 | 3.42257 | 3.76660 | 4.01140 | 4.20089 | |
| 48 | 2.84352 | 3.42026 | 3.76375 | 4.00812 | 4.19724 | |
| 49 | 2.84203 | 3.41805 | 3.76102 | 4.00497 | 4.19375 | |
| 50 | 2.84059 | 3.41592 | 3.75839 | 4.00195 | 4.19040 | |
| 51 | 2.83921 | 3.41389 | 3.75588 | 3.99906 | 4.18719 | |
| 52 | 2.83789 | 3.41193 | 3.75346 | 3.99627 | 4.18410 | |
| 53 | 2.83662 | 3.41005 | 3.75104 | 3.99360 | 4.18113 | |
| 54 | 2.83540 | 3.40824 | 3.74886 | 3.99103 | 4.17827 | |
| 55 | 2.83422 | 3.40649 | 3.74677 | 3.98855 | 4.17552 | |
| 56 | 2.83308 | 3.40482 | 3.74475 | 3.98616 | 4.17287 | |
| 57 | 2.83199 | 3.40320 | 3.74268 | 3.98386 | 4.17031 | |
| 58 | 2.83093 | 3.40163 | 3.74075 | 3.98164 | 4.16785 | |
| 59 | 2.82992 | 3.40013 | 3.73889 | 3.97949 | 4.16547 | |
| 60 | 2.82893 | 3.39867 | 3.73709 | 3.97742 | 4.16317 | |
| 61 | 2.82798 | 3.39726 | 3.73535 | 3.97542 | 4.16094 | |
| 62 | 2.82706 | 3.39590 | 3.73367 | 3.97348 | 4.15879 | |
| 63 | 2.82617 | 3.39458 | 3.73204 | 3.97161 | 4.15671 | |
| 64 | 2.82531 | 3.39331 | 3.73047 | 3.96979 | 4.15470 | |
| 65 | 2.82448 | 3.39207 | 3.72894 | 3.96804 | 4.15275 | |
| 66 | 2.82367 | 3.39088 | 3.72746 | 3.96633 | 4.15085 | |
| 67 | 2.82288 | 3.38971 | 3.72603 | 3.96468 | 4.14902 | |
| 68 | 2.82212 | 3.38859 | 3.72464 | 3.96308 | 4.14724 | |
| 69 | 2.82138 | 3.38750 | 3.72329 | 3.96152 | 4.14552 | |
| 70 | 2.82067 | 3.38644 | 3.72198 | 3.96001 | 4.14384 | |
| 71 | 2.81997 | 3.38540 | 3.72071 | 3.95855 | 4.14221 | |
| 72 | 2.81929 | 3.38440 | 3.71947 | 3.95712 | 4.14063 | |
| 73 | 2.81864 | 3.38343 | 3.71827 | 3.95574 | 4.13909 | |
| 74 | 2.81800 | 3.38248 | 3.71710 | 3.95439 | 4.13759 | |
| 75 | 2.81738 | 3.38156 | 3.71596 | 3.95308 | 4.13614 | |
| 76 | 2.81665 | 3.38067 | 3.71485 | 3.95181 | 4.13472 | |
| 77 | 2.81606 | 3.37979 | 3.71377 | 3.95056 | 4.13334 | |
| 78 | 2.81548 | 3.37894 | 3.71273 | 3.94935 | 4.13200 | |
| 79 | 2.81492 | 3.37812 | 3.71170 | 3.94818 | 4.13069 | |
| 80 | 2.81437 | 3.37731 | 3.71071 | 3.94703 | 4.12941 | |
| 81 | 2.81384 | 3.37652 | 3.70973 | 3.94591 | 4.12817 | |
| 82 | 2.81332 | 3.37575 | 3.70879 | 3.94481 | 4.12696 | |
| 83 | 2.81281 | 3.37501 | 3.70786 | 3.94375 | 4.12577 | |
| 84 | 2.81232 | 3.37428 | 3.70696 | 3.94271 | 4.12462 | |
| 85 | 2.81184 | 3.37356 | 3.70608 | 3.94169 | 4.12349 | |
| 86 | 2.81136 | 3.37287 | 3.70522 | 3.94070 | 4.12239 | |
| 87 | 2.81090 | 3.37219 | 3.70438 | 3.93974 | 4.12132 | |
| 88 | 2.81045 | 3.37152 | 3.70356 | 3.93879 | 4.12027 | |
| 89 | 2.81001 | 3.37087 | 3.70276 | 3.93778 | 4.11924 | |

| v | 2 | 3 | α | 4 | 5 | 6 |
|-----|---------|---------|----------|---------|---------|---------|
| 90 | 2.80958 | 3.37024 | | 3.70197 | 3.93691 | 4.11824 |
| 91 | 2.80916 | 3.36962 | | 3.70121 | 3.93607 | 4.11725 |
| 92 | 2.80875 | 3.36901 | | 3.70046 | 3.93524 | 4.11630 |
| 93 | 2.80835 | 3.36842 | | 3.69972 | 3.93443 | 4.11536 |
| 94 | 2.80795 | 3.36784 | | 3.69901 | 3.93363 | 4.11444 |
| 95 | 2.80757 | 3.36727 | | 3.69830 | 3.93274 | 4.11354 |
| 96 | 2.80719 | 3.36671 | | 3.69762 | 3.93194 | 4.11266 |
| 97 | 2.80682 | 3.36617 | | 3.69694 | 3.93117 | 4.11180 |
| 98 | 2.80646 | 3.36564 | | 3.69628 | 3.93041 | 4.11095 |
| 99 | 2.80611 | 3.36511 | | 3.69564 | 3.92967 | 4.11013 |
| 100 | 2.80576 | 3.36460 | | 3.69501 | 3.92894 | 4.10932 |
| 101 | 2.80542 | 3.36410 | | 3.69439 | 3.92822 | 4.10853 |
| 102 | 2.80509 | 3.36361 | | 3.69378 | 3.92752 | 4.10775 |
| 103 | 2.80476 | 3.36313 | | 3.69318 | 3.92684 | 4.10699 |
| 104 | 2.80444 | 3.36266 | | 3.69260 | 3.92616 | 4.10624 |
| 105 | 2.80412 | 3.36219 | | 3.69203 | 3.92550 | 4.10550 |
| 106 | 2.80382 | 3.36174 | | 3.69147 | 3.92486 | 4.10478 |
| 107 | 2.80351 | 3.36129 | | 3.69092 | 3.92422 | 4.10408 |
| 108 | 2.80322 | 3.36085 | | 3.69038 | 3.92360 | 4.10339 |
| 109 | 2.80293 | 3.36043 | | 3.68984 | 3.92299 | 4.10271 |
| 110 | 2.80264 | 3.36000 | | 3.68932 | 3.92239 | 4.10204 |
| 111 | 2.80236 | 3.35959 | | 3.68881 | 3.92180 | 4.10139 |
| 112 | 2.80208 | 3.35918 | | 3.68831 | 3.92122 | 4.10074 |
| 113 | 2.80181 | 3.35878 | | 3.68782 | 3.92065 | 4.10011 |
| 114 | 2.80155 | 3.35839 | | 3.68733 | 3.92009 | 4.09949 |
| 115 | 2.80129 | 3.35801 | | 3.68686 | 3.91954 | 4.09888 |
| 116 | 2.80103 | 3.35763 | | 3.68639 | 3.91900 | 4.09828 |
| 117 | 2.80078 | 3.35726 | | 3.68593 | 3.91847 | 4.09769 |
| 118 | 2.80053 | 3.35689 | | 3.68548 | 3.91795 | 4.09711 |
| 119 | 2.80028 | 3.35653 | | 3.68503 | 3.91744 | 4.09655 |
| 120 | 2.80004 | 3.35618 | | 3.68460 | 3.91694 | 4.09599 |
| 121 | 2.79981 | 3.35583 | | 3.68417 | 3.91644 | 4.09544 |
| 122 | 2.79958 | 3.35549 | | 3.68375 | 3.91596 | 4.09490 |
| 123 | 2.79935 | 3.35516 | | 3.68333 | 3.91548 | 4.09436 |
| 124 | 2.79913 | 3.35482 | | 3.68292 | 3.91501 | 4.09384 |
| 125 | 2.79890 | 3.35450 | | 3.68252 | 3.91454 | 4.09333 |
| 126 | 2.79869 | 3.35418 | | 3.68213 | 3.91409 | 4.09282 |
| 127 | 2.79847 | 3.35387 | | 3.68174 | 3.91364 | 4.09232 |
| 128 | 2.79826 | 3.35356 | | 3.68135 | 3.91320 | 4.09183 |
| 129 | 2.79806 | 3.35325 | | 3.68098 | 3.91276 | 4.09135 |
| 130 | 2.79785 | 3.35295 | | 3.68061 | 3.91234 | 4.09087 |
| 131 | 2.79765 | 3.35265 | | 3.68024 | 3.91192 | 4.09040 |
| 132 | 2.79745 | 3.35236 | | 3.67988 | 3.91150 | 4.08994 |
| 133 | 2.79726 | 3.35208 | | 3.67953 | 3.91109 | 4.08949 |
| 134 | 2.79707 | 3.35179 | | 3.67918 | 3.91069 | 4.08904 |
| 135 | 2.79688 | 3.35152 | | 3.67883 | 3.91029 | 4.08860 |
| 136 | 2.79669 | 3.35124 | | 3.67849 | 3.90990 | 4.08817 |
| 137 | 2.79651 | 3.35097 | | 3.67816 | 3.90952 | 4.08774 |

| v | 2 | 3 | α | 4 | 5 | 6 |
|-----|---------|---------|----------|---------|---------|---------|
| 138 | 2.79633 | 3.35071 | | 3.67783 | 3.90914 | 4.08723 |
| 139 | 2.79615 | 3.35045 | | 3.67751 | 3.90877 | 4.08683 |
| 140 | 2.79598 | 3.35019 | | 3.67719 | 3.90840 | 4.08644 |
| 141 | 2.79580 | 3.34993 | | 3.67687 | 3.90804 | 4.08606 |
| 142 | 2.79563 | 3.34968 | | 3.67656 | 3.90768 | 4.08562 |
| 143 | 2.79547 | 3.34943 | | 3.67626 | 3.90732 | 4.08538 |
| 144 | 2.79530 | 3.34919 | | 3.67596 | 3.90698 | 4.08495 |
| 145 | 2.79514 | 3.34895 | | 3.67566 | 3.90663 | 4.08459 |
| 146 | 2.79498 | 3.34871 | | 3.67537 | 3.90630 | 4.08423 |
| 147 | 2.79482 | 3.34848 | | 3.67508 | 3.90596 | 4.08388 |
| 148 | 2.79466 | 3.34825 | | 3.67479 | 3.90563 | 4.08342 |
| 149 | 2.79451 | 3.34802 | | 3.67451 | 3.90531 | 4.08306 |
| 150 | 2.79435 | 3.34780 | | 3.67423 | 3.90499 | 4.08271 |

Review exercise solutions by chapter

Chapter 5

- 1.
- a nominal
 - b ratio
 - c ratio
 - d ratio
 - e ratio
 - f ordinal

3.

- a 63
- b 53
- c 72

Chapter 6

- 1.
- a $100/200 = 0.5$
 - b $30/200 = 0.15$
 - c $45/200 = 0.225$
 - d $30/45 = 0.67$

3.

- a 0.00135
- b 0.5
- c 0.05
- d 0.00003

9.

- a $t < -1.833$ or $t > 1.833$
- b $t < -3.250$ or $t > 3.250$
- c $t < -2.045$ or $t > 2.045$
- d $t < -3.659$ or $t > 3.659$

10.

- a not reject
- b reject
- c reject
- d not reject

Chapter 8

2.

- a $(0.04, 0.21)$
- b $(0.08, 0.16)$

3.

- a $(0.10, 0.22)$
- b $(0.08, 0.24)$
- c $Z = 0.74$ therefore we would be 54% confident.

4.

- a $(0.005, 0.15)$
- b $(-0.01, 0.16)$
- c $(-0.04, 0.19)$

Chapter 9

2.

- a $(-0.745, 1.425)$
- b $(-0.963, 1.643)$
- c $(-1.405, 2.085)$

3.

- a The difference between groups is not statistically significant.

- b The difference between groups is statistically significant and the treatment appears to increase SBP.
- c The difference between groups is statistically significant and the treatment appears to lower SBP.

Chapter 10

3.

- a not rejected
- b rejected
- c rejected
- d rejected
- e not rejected
- f not rejected
- g rejected
- h not rejected

4.

- a 0.119
- b 0.008
- c 0.001
- d 0.317

5.

a

| | Placebo | Test |
|---------------|---------|------|
| Responder | 117 | 152 |
| Non-responder | 385 | 346 |
| | 502 | 498 |

- b $H_0: p_1 - p_2 = 0$
 $H_A: p_1 - p_2 \neq 0$
- c Chi-square test, Fisher's exact test, or z approximation
- d Yes, there is sufficient evidence to reject the null hypothesis ($\alpha = 0.05$). Using the chi-square test the assumptions are that the two groups are independent; responses are mutually exclusive; and the expected cell counts are at least 5 in >80% of the cells. The value of the chi-square test statistic is 6.62.
- e The odds ratio = $\frac{(152)(385)}{(117)(346)} = 1.45$

Participants exposed to the test treatment are 1.45 times more likely to respond than participants in the placebo group.

Chapter 11

1.

- a $H_0: \mu_{TEST} - \mu_{PLACEBO} = 0$
 $H_A: \mu_{TEST} - \mu_{PLACEBO} \neq 0$
- b $t < -2.0423$ or $t > 2.042$
- c Independent samples; outcome approximately normally distributed; equal unknown variance
- d -2.26
- e Do not reject H_0 since $-2.042 < -0.68 < 2.042$. The mean pain scores are not significantly different between the two groups.

2.

- a SS error = 238.67896
MS Drug = 49.947295
MS Error = 7.95597
 $F = 6.28$
- b 3
- c $H_0: \mu_1 = \mu_2 = \mu_3$
 $H_A: \text{at least one pair of population means are unequal}$
- d 33
- e $F > 3.32$
- f Reject H_0 since $6.28 > 3.32$. At least one pair of population means is unequal.

3.

- a $H_0: \mu_p = \mu_L = \mu_M = \mu_H$
 $H_A: \text{at least one pair of population means are unequal}$
- b Each group represents a simple random sample from relevant populations; observations are independent; outcome is approximately normally distributed; the variance is equal across the populations
- c Placebo vs. low; placebo vs. medium; placebo vs. high; low vs. medium; low vs. high; medium vs. high
- d To control the overall Type I error
- e $MSD_T = 3.68639\sqrt{\frac{20}{30}} = 3.01$

Chapter 12

4.

a 80% power: 64/group
90% power: 86/group

b 80% power: 143/group
90% power: 191/group

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