## 17

## Chemical Equilibrium

CHAPTER

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## REVERSIBLE REACTIONS

Not all chemical reactions proceed to completion. In most reactions two or more substances react to form products which themselves react to give back the original substances. Thus A and B may react to form C and D which react together to reform A and $B$.

$$
\begin{array}{lll}
\mathrm{A}+\mathrm{B} & \longrightarrow \mathrm{C}+\mathrm{D} & \text { (Forward reaction) } \\
\mathrm{A}+\mathrm{B} & \mathrm{C}+\mathrm{D} & \text { (Reverse reaction) }
\end{array}
$$

$A$ reaction which can go in the forward and backward direction simultaneously is called a Reversible reaction. Such a reaction is represented by writing a pair of arrows between the reactants and products.

$$
\mathrm{A}+\mathrm{B} \rightleftharpoons \mathrm{C}+\mathrm{D}
$$

The arrow pointing right indicates the forward reaction, while that pointing left shows the reverse reaction.
Some Examples of Reversible Reactions
A few common examples of reversible reactions are listed below:

$$
2 \mathrm{NO}_{2}(g) \rightleftharpoons \mathrm{N}_{2} \mathrm{O}_{4}(g)
$$

## AN EQUILIBRIUM ANOLOGY

Nuts and Bolts Representation of Chemical Equilibrium


A "nuts and bolts" representation of chemical equilibrium for a reversible reaction. Initially (a) there are 100 nuts and 100 bolts in the beakers represented in the figure by 10 of each. The concentration is 100 bolts per beaker for both nuts and bolts. As time passes (b) concentrations of reactants decrease and concentrations of products - assembled units - increase. Equilibrium is established ( $c$ ) when concentrations stop changing. For this equilibrium, there are 40 nuts per beaker, 40 bolts per beaker, and 60 assembled units per beaker. The rate of the forward reaction (assembling units) is equal to the rate of the reverse reaction (taking the units apart).

$$
\begin{aligned}
\mathrm{H}_{2}(\mathrm{~g})+\mathrm{I}_{2}(\mathrm{~g}) & \rightleftharpoons 2 \mathrm{HI}(\mathrm{~g}) \\
\mathrm{CH}_{3} \mathrm{COOH}(\mathrm{l})+\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}(\mathrm{l}) & \rightleftharpoons \mathrm{CH}_{3} \mathrm{COOC}_{2} \mathrm{H}_{5}(\mathrm{l})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \\
\mathrm{PCl}_{5}(\mathrm{~s}) & \rightleftharpoons \mathrm{PCl}_{3}(\mathrm{~s})+\mathrm{Cl}_{2}(\mathrm{~g}) \\
\mathrm{CaCO}_{3}(\mathrm{~s}) & \rightleftharpoons \mathrm{CaO}(\mathrm{~s})+\mathrm{CO}_{2}(\mathrm{~g})
\end{aligned}
$$

## NATURE OF CHEMICAL EQUILIBRIUM : ITS DEFINITION

Let us consider the reaction

$$
\mathrm{A}+\mathrm{B} \rightleftharpoons \mathrm{C}+\mathrm{D}
$$

If we start with $A$ and $B$ in a closed vessel, the forward reaction proceeds to form $C$ and $D$. The concentrations of A and B decrease and those of C and D increase continuously. As a result the rate of forward reaction also decreases and the rate of the reverse reaction increases. Eventually, the rate of the two opposing reactions equals and the system attains a state of equilibrium. Thus Chemical equilibrium may be defined as: the state of a reversible reaction when the two opposing reactions occur at the same rate and the concentrations of reactants and products do not change with time.

Furthermore, the true equilibrium of a reaction can be attained from both sides. Thus the equilibrium concentrations of the reactants and products are the same whether we start with A and B , or C and D .


Figure 17.1
At equilibrium the forward reaction rate equals the reverse reaction rate.

## Chemical Equilibrium is Dynamic Equilibrium

We have shown above that as the reaction $\mathrm{A}+\mathrm{B} \rightleftharpoons \mathrm{C}+\mathrm{D}$ attains equilibrium, the concentrations of $A$ and $B$, as also of $C$ and $D$ remain constant with time. Apparently it appears that the equilibrium is dead. But it is not so. The equilibrium is dynamic. Actually, the forward and the reverse reactions are taking place at equilibrium but the concentrations remain unchanged.


Figure 17.2
Molecules of $A$ and $B$ colliding to give $C$ and $D$, and those of $C$ and $D$ colliding to give $A$ and $B$.

The dynamic nature of chemical equilibrium can be easily understood on the basis of the kinetic molecular model. The molecules of A and B in the equilibrium mixture collide with each other to form C and D . Likewise C and D collide to give back A and B . The collisions of molecules in a closed system is a ceaseless phenomenon. Therefore collisions of A and B giving C and D (Forward reaction) and collisions of C and D giving back A and B (reverse reaction) continue to occur even at equilibrium, while concentrations remain unchanged.

## CHARACTERISTICS OF CHEMICAL EQUILIBRIUM

Before we take up the mathematical study of chemical equilibria, let us understand the chemical characteristics of chemical equilibrium.

## (1) Constancy of concentrations

When a chemical equilibrium is established in a closed vessel at constant temperature, concentrations of the various species in the reaction mixture become constant.

The reaction mixture at equilibrium is called Equilibrium mixture.
The concentrations at equilibrium are called Equilibrium concentrations. The equilibrium concentrations are represented by square brackets with subscript eq or eqm, []$_{e q}$. Thus $[\mathrm{A}]_{e q}$ denotes the equilibrium concentration of substance A in moles per litre. In modern practice the subscript eq is not used.
(2) Equilibrium can be initiated from either side

The state of equilibrium of a reversible reaction can be approached whether we start with reactants or products, for example, the equilibrium

$$
\mathrm{H}_{2}(\mathrm{~g})+\mathrm{I}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{HI}(\mathrm{~g})
$$

is established if we start the reaction with $\mathrm{H}_{2}$ and $\mathrm{I}_{2}$, or 2 HI .
Fig. 17.3. Shows whether we start with 1 mole of $\mathrm{I}_{2}$ and 1 mole of $\mathrm{H}_{2}$, or with 2 moles of HI in a vessel of the same volume, the same mixture of $\mathrm{H}_{2}, \mathrm{I}_{2}$ and HI is obtained.


Figure 17.3
The left graph shows how equilibrium is attained for start with $\mathrm{H}_{2}$ and $\mathrm{I}_{2}$. The right graph depicts the attainment of equilibrium for start with 2 HI . Equilibrium concentrations in both cases are the same.

## (3) Equilibrium cannot be Attained in an Open Vessel

The equilibrium can be established only if the reaction vessel is closed and no part of the reactants or products is allowed to escape out. In an open vessel, the gaseous reactants and/or products may escape into the atmosphere leaving behind no possibility of attaining equilibrium.

However, the equilibrium can be attained when all the reactants and products are in the same phase i.e., ethanol and ethanoic acid.


Figure 17.4
A chemical equilibrium between $\mathrm{H}_{2}, \mathrm{I}_{2}$ and H .

## (4) A catalyst cannot change the equilibrium point

When a catalyst is added to a system in equilibrium, it speeds up the rate of both the forward and the reverse reaction to an equal extent. Therefore a catalyst cannot change the equilibrium point except that it is achieved earlier. This enhances the rate of the reaction.

The rapid increase of the rate of an equilibrium reaction on the addition of a catalyst is illustrated in Fig. 17.5.
(5) Value of Equilibrium Constant does not depend upon the initial concentration of reactants

It has been found that equilibrium constant must be the same when the concentrations of reacting species are varied over a wide range.


Figure 17.5
The vertical part of the curve indicates rapid increase of rate of reaction on addition of catalyst.
(6) At Equilibrium $\Delta G=\mathbf{0}$

At equilibrium the Gibbs free energy $(G)$ is minimum and any change taking place at equilibrium proceeds without change in free energy i.e. $\Delta \mathrm{G}=0$.

## LAW OF MASS ACTION

Two Norwegian chemists, Guldberg and Waage, studied experimentally a large number of equilibrium reactions. In 1864, they postulated a generalisation called the Law of Mass action. It states that : the rate of a chemical reaction is proportional to the active masses of the reactants.

By the term 'active mass' is meant the molar concentration i.e., number of moles per litre. It is expressed by enclosing the formula of the substance in square brackets. Thus a gas mixture containing 1 g of hydrogen $\left(\mathrm{H}_{2}\right)$ and 127 g of iodine $\left(\mathrm{I}_{2}\right)$ per litre has the concentrations

$$
\left[\mathrm{H}_{2}\right]=0.5 \text { and }\left[\mathrm{I}_{2}\right]=0.5
$$

## Explanation of the Law of Mass Action Based on the Molecular Collision Theory

We assume that a chemical reaction occurs as a result of the collisions between the reacting molecules. Although some of these collisions are ineffective, the chemical change produced is proportional to the number of collisions actually taking place. Thus at a fixed temperature the rate of a reaction is determined by the number of collisions between the reactant molecules present in unit volume.

Let us consider four boxes of one cubic centimetre volume; containing different number of reacting molecules A and B (Fig 17.6). They undergo collisions to form the products C and D, the rate of reaction being governed by the number of possible collisions between them.


Figure 17.6
Possible collisions between molecules of the reactants $A$ and $B$.
In the first box there is one molecule of A and one molecule of B , and the possibilities of collision at any instant is $1 \times 1=1$. In the second box, the number of molecules of $A$ and $B$ are two each and the possibilities of collisions are $2 \times 2=4$. In the third box, there are two molecules of A and three molecules of $B$, and the number of possibilities of collisions between $A$ and $B$ are increased to $3 \times 2=6$. In the fourth box, we have three molecules of each of $A$ and $B$ and the total number of collisions between them is $3 \times 3=9$. Thus in general, we can say that the possibilities of collisions between the reacting molecules A and B are equal to the product of the number of molecules of each species per unit volume. Since the rate of reaction is determined by molecular impacts, it is proportional to moles per unit volume i.e., molar concentration. Thus we can write

$$
\begin{aligned}
\text { Rate of reaction } & \propto[\mathrm{A}][\mathrm{B}] \\
& =k[\mathrm{~A}][\mathrm{B}]
\end{aligned}
$$

In a reaction, $\mathrm{A}+\mathrm{B}+\mathrm{C} \longrightarrow$ the number of collisions between $\mathrm{A}, \mathrm{B}$ and $C$ depends on the concentration of each reactant (Fig. 17.7). Therefore,

$$
\text { Rate of reaction } \propto[\mathrm{A}][\mathrm{B}][\mathrm{C}]=k[\mathrm{~A}][\mathrm{B}][\mathrm{C}]
$$

From the above considerations, it stands proved that the rate of a reaction is proportional to the molar concentrations of the reactants.


Figure 17.7

## EQUILIBRIUM CONSTANT : EQUILIBRIUM LAW

Let us consider a general reaction

$$
\mathrm{A}+\mathrm{B} \rightleftharpoons \mathrm{C}+\mathrm{D}
$$

and let $[A],[B],[C]$ and $[D]$ represent the molar concentrations of $A, B, C$ and $D$ at the equilibrium point. According to the Law of Mass action.

$$
\begin{aligned}
& \text { Rate of forward reaction } \propto[\mathrm{A}][\mathrm{B}]=k_{1}[\mathrm{~A}][\mathrm{B}] \\
& \text { Rate of reverse reaction } \propto[\mathrm{C}][\mathrm{D}]=k_{2}[\mathrm{C}][\mathrm{D}]
\end{aligned}
$$

where $k_{1}$ and $k_{2}$ are rate constants for the forward and reverse reactions.
At equilibrium, rate of forward reaction $=$ rate of reverse reaction.
Therefore,
or

$$
\begin{align*}
k_{1}[\mathrm{~A}][\mathrm{B}] & =k_{2}[\mathrm{C}][\mathrm{D}] \\
\frac{k_{1}}{k_{2}} & =\frac{[\mathrm{C}][\mathrm{D}]}{[\mathrm{A}][\mathrm{B}]} \tag{1}
\end{align*}
$$

At any specific temperature $k_{1} / k_{2}$ is constant since both $k_{1}$ and $k_{2}$ are constants. The ratio $k_{1} / k_{2}$ is called Equilibrium constant and is represented by the symbol $K_{c}$, or simply $k$. The subscript ' $c$ ' indicates that the value is in terms of concentrations of reactants and products. The equation (1) may be written as

$$
\underset{\mathrm{c}}{\text { Equilibrium }} \text { constant } \quad k_{\mathrm{c}}=\frac{[\mathrm{C}][\mathrm{D}]}{[\mathrm{A}][\mathrm{B}]} \text { Product concentrations }
$$

This equation is known as the Equilibrium constant expression or Equilibrium law.

Consider the reaction



Figure 17.8

Here, the forward reaction is dependent on the collisions of each of two A molecules. Therefore, for writing the equilibrium expression, each molecule is regarded as a separate entity i.e.,

$$
\mathrm{A}+\mathrm{A} \rightleftharpoons \mathrm{C}+\mathrm{D}
$$

Then the equilibrium constant expression is

$$
k_{\mathrm{c}}=\frac{[\mathrm{C}][\mathrm{D}]}{[\mathrm{A}][\mathrm{A}]}=\frac{[\mathrm{C}][\mathrm{D}]}{[\mathrm{A}]^{2}} \quad \begin{aligned}
& \text { Power equal to } \\
& \text { coefficent of } \mathrm{A}
\end{aligned}
$$

As a general rule, if there are two or more molecules of the same substance in the chemical equation, its concentration is raised to the power equal to the numerical coefficient of the substance in the equation.

## Equilibrium Constant Expression for a Reaction in General Terms

The general reaction may be written as

$$
a \mathrm{~A}+b \mathrm{~B} \rightleftharpoons c \mathrm{C}+d \mathrm{D}
$$

where $a, b, c$ and $d$ are numerical quotients of the substance, $\mathrm{A}, \mathrm{B}, \mathrm{C}$ and D respectively. The equilibrium constant expression is

$$
K_{c}=\frac{[\mathrm{C}]^{c}[\mathrm{D}]^{d}}{[\mathrm{~A}]^{a}[\mathrm{~B}]^{b}}
$$

where $K_{c}$ is the Equilibrium constant. The general definition of the equilibrium constant may thus be stated as : the product of the equilibrium concentrations of the products divided by the product of the equilibrium concentrations of the reactants, with each concentration term raised to a power equal to the coefficient of the substance in the balanced equation.

## How to Write the Equilibrium Constant Expression?

(1) Write the balanced chemical equation for the equilibrium reaction. By convention, the substances on the left of the equation are called the reactants and those on the right, the products.
(2) Write the product of concentrations of the 'products' and raise the concentrations of each substance to the power of its numerical quotient in the balanced equation.
(3) Write the product of concentrations of 'reactants' and raise the concentration of each substance to the power of its numerical quotient in the balanced equation.
(4) Write the equilibrium expression by placing the product concentrations in the numerator and reactant concentrations in the denominator. That is,

$$
K_{c}=\frac{\text { Product of concentrations of 'products' form Step (2) }}{\text { Product of concentrations of 'reactants' form Step (3) }}
$$

SOLVED PROBLEM 1. Give the equilibrium constant expression for the reaction

$$
\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \rightleftharpoons 2 \mathrm{NH}_{3}(g)
$$

SOLUTION
(1) The equation is already balanced. The numerical quotient of $\mathrm{H}_{2}$ is 3 and of $\mathrm{NH}_{3}$ is 2 .
(2) The concentration of the 'product' $\mathrm{NH}_{3}$ is $\left[\mathrm{NH}_{3}\right]^{2}$
(3) The product of concnentrations of the reactants is $\left[\mathrm{N}_{2}\right]\left[\mathrm{H}_{2}\right]^{3}$
(4) Therefore, the equilibrium constant expression is

$$
K_{c}=\frac{\left[\mathrm{NH}_{3}\right]^{2}}{\left[\mathrm{~N}_{2}\right]\left[\mathrm{H}_{2}\right]^{3}}
$$

SOLVED PROBLEM 2. Write the equilibrium constant expression for the reaction

$$
\mathrm{N}_{2} \mathrm{O}_{5}(\mathrm{~g}) \rightleftharpoons \mathrm{NO}_{2}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g})
$$

SOLUTION
(1) The equation as written is not balanced. Balancing yields

$$
2 \mathrm{~N}_{2} \mathrm{O}_{5} \rightleftharpoons 4 \mathrm{NO}_{2}(\mathrm{~g})+\mathrm{O}_{2}
$$

(2) The quotient of the product $\mathrm{NO}_{2}$ is 4 and of the reactant $\mathrm{N}_{2} \mathrm{O}_{5}$ it is 2 .
(3) The product of the concentrations of products is

$$
\left[\mathrm{NO}_{2}\right]^{4}\left[\mathrm{O}_{2}\right]
$$

(4) The concentration of the reactant is

$$
\left[\mathrm{N}_{2} \mathrm{O}_{5}\right]^{2}
$$

(5) The equilibrium constant expression can be written as

$$
K_{c}=\frac{\left[\mathrm{NO}_{2}\right]^{4}\left[\mathrm{O}_{2}\right]}{\left[\mathrm{N}_{2} \mathrm{O}_{5}\right]^{2}}
$$

SOLVED PROBLEM 3. What is the equilibrium constant expression of the reaction

$$
\mathrm{CH}_{4}(g)+\mathrm{H}_{2} \mathrm{O}(g) \rightleftharpoons \mathrm{CO}(g)+3 \mathrm{H}_{2}(g)
$$

SOLUTION
Write the product of concentrations of 'products' divided by the product of concentrations of 'reactants'. The concentration of $\mathrm{H}_{2}$ is to be raised by its quotient in the equation. Thus, the equilibrium constant expression is:

$$
K_{c}=\frac{[\mathrm{CO}]\left[\mathrm{H}_{2}\right]^{3}}{\left[\mathrm{CH}_{4}\right]\left[\mathrm{H}_{2} \mathrm{O}\right]}
$$

## EQUILIBRIUM CONSTANT EXPRESSION IN TERMS OF PARTIAL PRESSURES

When all the reactants and products are gases, we can also formulate the equilibrium constant expression in terms of partial pressure. The relationship between the partial pressure $(p)$ of any one gas in the equilibrium mixture and the molar concentration follows from the general ideal gas equation

$$
p V=n R T \text { or } \quad p=\left(\frac{n}{V}\right) R T
$$

The quantity $\frac{n}{V}$ is the number of moles of the gas per unit volume and is simply the molar concentration. Thus,

$$
p=(\text { Molar concentration }) \times R T
$$

i.e., the partial pressure of a gas in the equilibrium mixture is directly proportional to its molar concentration at a given temperature. Therefore, we can write the equilibrium constant expression in terms of partial pressure instead of molar concentrations. For a general reaction

$$
l \mathrm{~L}(\mathrm{~g})+m \mathrm{M}(\mathrm{~g}) \rightleftharpoons y \mathrm{Y}(\mathrm{~g})+\mathrm{zZ}(\mathrm{~g})
$$

the equilibrium law or the equilibrium constant may be written as

$$
K_{p}=\frac{\left(p_{\mathrm{Y}}\right)^{y}\left(p_{\mathrm{Z}}\right)^{z}}{\left(p_{\mathrm{L}}\right)^{l}\left(p_{\mathrm{M}}\right)^{m}}
$$

Here $K_{p}$ is the equilibrium constant, the subscript $p$ referring to partial pressure. Partial pressures are expressed in atmospheres.

SOLVED PROBLEM 1. Write the equilibrium constant expression for the synthesis of ammonia,

$$
\mathrm{N}_{2}(\mathrm{~g})+3 \mathrm{H}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{NH}_{3}(\mathrm{~g})
$$

SOLUTION

$$
K_{p}=\frac{\left(p_{\mathrm{NH}_{3}}\right)^{2}}{\left(p_{\mathrm{N}_{2}}\right)\left(p_{\mathrm{H}_{2}}\right)^{3}}
$$

SOLVED PROBLEM 2. Using partial pressures, write the equilibrium law for the reaction

$$
\mathrm{H}_{2}(\mathrm{~g})+\mathrm{I}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{HI}(\mathrm{~g})
$$

SOLUTION

$$
K_{p}=\frac{\left(p_{\mathrm{H}}\right)^{2}}{\left(p_{\mathrm{H}_{2}}\right)\left(p_{\mathrm{I}_{2}}\right)}
$$

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[ SOLVED PROBLEM 3. What is the expression $K_{p}$ for the reaction

$$
\mathrm{N}_{2} \mathrm{O}_{4}(g) \rightleftharpoons 2 \mathrm{NO}_{2}(g)
$$

SOLUTION
For $K_{p}$ we use the partial pressure in the equilibrium constant expression. Therefore,

$$
K_{p}=\frac{\left(p_{\mathrm{NO}_{2}}\right)^{2}}{\left(p_{\mathrm{N}_{2} \mathrm{O}_{4}}\right)}
$$

## HOW $K_{c}$ AND $K_{p}$ ARE RELATED?

Let us consider a general reaction

$$
j \mathrm{~A}+k \mathrm{~B} \rightleftharpoons l \mathrm{C}+m \mathrm{D}
$$

where all reactants and products are gases. We can write the equilibrium constant expression in terms of partial pressures as

$$
\begin{equation*}
K_{p}=\frac{\left(p_{C}\right)^{l}\left(p_{D}\right)^{m}}{\left(p_{A}\right)^{j}\left(p_{B}\right)^{k}} \tag{1}
\end{equation*}
$$

Assuming that all these gases constituting the equilibrium mixture obey the ideal gas equation, the partial pressure $(p)$ of a gas is

$$
p=\left(\frac{n}{V}\right) R T
$$

Where $\frac{n}{V}$ is the molar concentration. Thus the partial pressures of individual gases, A, B, C and D are:

$$
P_{\mathrm{A}}=[\mathrm{A}] R T ; p_{\mathrm{B}}=[\mathrm{B}] R T ; p_{C}=[\mathrm{C}] R T ; p_{\mathrm{D}}=[\mathrm{D}] R T
$$

Substituting these values in equation (1), we have

$$
\begin{array}{ll} 
& K_{p}=\frac{[\mathrm{C}]^{l}(R T)^{l}[\mathrm{D}]^{m}(R T)^{m}}{[\mathrm{~A}]^{j}(R T)^{j}[\mathrm{~B}]^{k}(R T)^{k}} \\
\text { or } \quad K_{p}=\frac{[\mathrm{C}]^{l}[\mathrm{D}]^{m}}{[\mathrm{~A}]^{j}[\mathrm{~B}]^{k}} \times \frac{(R T)^{l+m}}{(R T)^{j+k}} \\
\therefore \quad K_{p}=K_{c} \times(R T)^{(l+m)-(j+k)} \\
\therefore \quad K_{p}=K_{c} \times(R T)^{\Delta n}
\end{array}
$$

where $\Delta n=(l+m)-(j+k)$, the difference in the sums of the coefficients for the gaseous products and reactants.

From the expression (2) it is clear that when $\Delta n=0, K_{p}=K_{c}$.
SOLVED PROBLEM 1.At $500^{\circ} \mathrm{C}$, the reaction between $\mathrm{N}_{2}$ and $\mathrm{H}_{2}$ to form ammonia has $K_{c}=6.0 \times 10^{-2}$. What is the numerical value of $K_{p}$ for the reaction?

SOLUTION
Here, we will use the general expression

$$
K_{p}=K_{c}(R T)^{\Delta n}
$$

For the reaction $\quad \mathrm{N}_{2}+3 \mathrm{H}_{2} \rightleftharpoons 2 \mathrm{NH}_{3}$
we have $\quad \Delta n=$ (sum of quotients of products) - (sum of quotients of reactants)

$$
\begin{aligned}
& =2-4=-2 \\
K_{c} & =6.0 \times 10^{-2} \\
T & =500+273=773 \mathrm{~K} \\
R & =0.0821
\end{aligned}
$$

Substituting the value of $R, T, K_{c}$ and $\Delta n$ in the general expression, we have

$$
\begin{aligned}
K_{p} & =\left(6.0 \times 10^{-2}\right)[(0.0821) \times(773)]^{-2} \\
& =\mathbf{1 . 5} \times \mathbf{1 0}^{-5}
\end{aligned}
$$

SOLVED PROBLEM 2. The value of $K_{p}$ at $25^{\circ} \mathrm{C}$ for the reaction

$$
2 \mathrm{NO}(g)+\mathrm{Cl}_{2}(g) \rightleftharpoons 2 \mathrm{NOCl}(g)
$$

is $1.9 \times 10^{3} \mathrm{~atm}^{-1}$. Calculate the value of $K_{c}$ at the same temperature.
SOLUTION
We can write the general expression as

$$
K_{p}=K_{c}(R T)^{\Delta \mathrm{n}} \text { or } K_{c}=\frac{K_{p}}{(R T)^{\Delta n}}
$$

Here,

$$
\begin{aligned}
T & =25+273=298 \mathrm{~K} \\
R & =0.0821 \\
\Delta n & =2-(2+1)=-1 \\
K_{p} & =1.9 \times 10^{3}
\end{aligned}
$$

Substituting these values in the general expression

$$
\begin{aligned}
K_{c} & =\frac{1.9 \times 10^{3}}{(0.0821 \times 298)^{-1}} \\
& =4.6 \times \mathbf{1 0}^{4}
\end{aligned}
$$

## Calculation of $K_{c}$ from Experimental Information

To determine the value of $K_{c}$ of a reaction, write the balanced equation. Then write the equilibrium constant expression. Substitute in it the equilibrium concentrations of the reactants and products found experimentally. Thus calculate the value of $K_{c}$.

SOLVED PROBLEM 1. At equilibrium for the reaction

$$
2 \mathrm{SO}_{2}(g)+\mathrm{O}_{2}(g) \rightleftharpoons 2 \mathrm{SO}_{3}(g)
$$

the concentrations of reactants and products at $727^{\circ} \mathrm{C}$ were found to be : $\mathrm{SO}_{2}=0.27 \mathrm{~mol} \mathrm{~L}{ }^{-1}$; $\mathrm{O}_{2}=0.40 \mathrm{~mol} \mathrm{~L}^{-1}$; and $\mathrm{SO}_{3}=0.33 \mathrm{~mol} \mathrm{~L}^{-1}$. What is the value of the equilibrium constant, $K_{c \text {, }}$ at this temperature?

SOLUTION
Write the equilibrium constant expression for the reaction

$$
K_{c}=\frac{\left[\mathrm{SO}_{3}\right]^{2}}{\left[\mathrm{SO}_{2}\right]^{2}\left[\mathrm{O}_{2}\right]}
$$

We know that:

$$
\left[\mathrm{SO}_{3}\right]=0.33 \mathrm{~mol} \mathrm{~L}^{-1} ;\left[\mathrm{SO}_{2}\right]=0.27 \mathrm{~mol} \mathrm{~L}^{-1} ;\left[\mathrm{O}_{2}\right]=0.40 \mathrm{~mol} \mathrm{~L}^{-1}
$$

Substituting these values in the equilibrium constant expression, we have

$$
K_{c}=\frac{(0.33)^{2}}{(0.27)^{2} \times(0.40)}=3.7 \mathrm{~mol}^{-1} \text { or simply } 3.7
$$

SOLVED PROBLEM 2. Some nitrogen and hydrogen gases are pumped into an empty five-litre glass bulb at $500^{\circ} \mathrm{C}$. When equilibrium is established, 3.00 moles of $\mathrm{N}_{2}, 2.10$ moles of $\mathrm{H}_{2}$ and 0.298 mole of $\mathrm{NH}_{3}$ are found to be present. Find the value of $K_{c}$ for the reaction

$$
\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \rightleftharpoons 2 \mathrm{NH}_{3}(g)
$$

at $500^{\circ} \mathrm{C}$.

## SOLUTION

The equilibrium concentrations are obtained by dividing the number of moles of each reactant and product by the volume, 5.00 litres. Thus,

$$
\begin{aligned}
{\left[\mathrm{N}_{2}\right] } & =3.00 \mathrm{~mole} / 5.00 \mathrm{~L}=0.600 \mathrm{M} \\
{\left[\mathrm{H}_{2}\right] } & =2.10 \mathrm{~mole} / 5.00 \mathrm{~L}=0.420 \mathrm{M} \\
{\left[\mathrm{NH}_{3}\right] } & =0.298 \text { mole } / 5.00 \mathrm{~L}=0.0596 \mathrm{M}
\end{aligned}
$$

Substituting these concentrations (not number of moles) in the equilibrium constant expression, we get the value of $K_{c}$.

$$
K_{c}=\frac{\left[\mathrm{NH}_{3}\right]^{2}}{\left[\mathrm{~N}_{2}\right]\left[\mathrm{H}_{2}\right]^{3}}=\frac{(0.0596)^{2}}{(0.600)(0.420)^{3}}=0.080
$$

Thus, for the reaction of $\mathrm{H}_{2}$ and $\mathrm{N}_{2}$ to form $\mathrm{NH}_{3}$ at $500^{\circ} \mathrm{C}$, we can write

$$
K_{c}=\frac{\left[\mathrm{NH}_{3}\right]^{2}}{\left[\mathrm{~N}_{2}\right]\left[\mathrm{H}_{2}\right]^{3}}=\mathbf{0 . 0 8 0}
$$

SOLVED PROBLEM 3. Calculate the equilibrium constant at $25^{\circ} \mathrm{C}$ for the reaction

$$
2 \mathrm{NOCl}(g) \rightleftharpoons 2 \mathrm{NO}(g)+\mathrm{Cl}_{2}(g)
$$

In an experiment, 2.00 moles of NOCl were placed in a one-litre flask and the concentration of NO after equilibrium achieved was 0.66 mole/litre.

SOLUTION
Let us write the equilibrium constant expression for the balanced chemical equation.

$$
K_{c}=\frac{[\mathrm{NO}]^{2}\left[\mathrm{Cl}_{2}\right]}{[\mathrm{NOCl}]^{2}}
$$

Next we proceed to find the equilibrium concentrations of $\mathrm{NOCl}, \mathrm{NO}$ and $\mathrm{Cl}_{2}$. Since the volume of the reaction vessel is one litre, the moles of various reagents also represent their molar concentrations.

The initial amount of NOCl is 2.00 moles. Let us assume that $x$ moles of it have reacted to achieve the equilibrium. The moles of different reagents at equilibrium are indicated in the equation

| 2 NOCl | $2 \mathrm{NO}+\mathrm{Cl}_{2}$ |
| :--- | :---: |
| $(2-x)$ | $x \quad x / 2$ |

According to this equation, one mole of NOCl gives one mole of NO and half a mole of $\mathrm{Cl}_{2}$.
The experimental value of equilibrium concentration of NO is 0.66 mole/litre. Therefore, the
equilibrium concentration $\mathrm{Cl}_{2}$ is half of it i.e. 0.33 mole/litre. Since $x=0.66$, the equilibrium concentration of $\mathrm{NOCl}=(2-0.66)=1.34$. To find $K_{c}$, these values of equilibrium concentrations are substituted in the equilibrium constant expression.

$$
K_{c}=\frac{\left[\mathrm{NO}^{2}\left[\mathrm{Cl}_{2}\right]\right.}{[\mathrm{NOCl}]^{2}}=\frac{(0.66)^{2}(0.33)}{(1.34)^{2}}=\mathbf{0 . 0 8 0}
$$

SOLVED PROBLEM 4. At a certain temperature, 0.100 mole of $\mathrm{H}_{2}$ and 0.100 mole of $\mathrm{I}_{2}$ were placed in a one-litre flask. The purple colour of iodine vapour was used to monitor the reaction. After a time, the equilibrium

$$
\mathrm{H}_{2}+\mathrm{I}_{2} \rightleftharpoons 2 \mathrm{HI}
$$

was established and it was found that the concentration of $\mathrm{I}_{2}$ decreased to 0.020 mole/litre. Calculate the value of $K_{c}$ for the reaction at the given temperature.

SOLUTION
The equilibrium constant expression for the reaction

$$
\mathrm{H}_{2}+\mathrm{I}_{2} \rightleftharpoons 2 \mathrm{HI}
$$

is

$$
K_{c}=\frac{[\mathrm{HI}]^{2}}{\left[\mathrm{H}_{2}\right]\left[\mathrm{I}_{2}\right]}
$$

Let us proceed to find the equilibrium concentrations of the various species.
The initial moles of $\mathrm{H}_{2}, \mathrm{I}_{2}$ and HI present at equilibrium are

$$
\mathrm{H}_{2}+\mathrm{I}_{2} \rightleftharpoons 2 \mathrm{HI}
$$

moles at equilibrium : (0.100-x) (0.100-x) $2 x$
Since the volume of the reaction vessel is one litre, the moles at equilibrium also represent the equilibrium concentrations. Thus,
or

$$
\begin{aligned}
{\left[\mathrm{I}_{2}\right] } & =0.100-x=0.020 \text { (given) } \\
x & =0.100-0.020 \\
& =0.080
\end{aligned}
$$

Knowing the value of $x$, we can give the equilibrium concentrations of $\mathrm{H}_{2}, \mathrm{I}_{2}$ and HI .

$$
\begin{aligned}
{\left[\mathrm{H}_{2}\right] } & =0.100-x=0.100-0.080=0.020 \\
{\left[\mathrm{I}_{2}\right] } & =0.020 \text { (given) } \\
{[\mathrm{HI}] } & =2 x=0.160
\end{aligned}
$$

Substituting these values in the equilibrium constant expression, we get the value of $K_{c}$.

$$
K_{c}=\frac{[\mathrm{HI}]^{2}}{\left[\mathrm{H}_{2}\right]\left[\mathrm{I}_{2}\right]}=\frac{(0.160)^{2}}{0.02 \times 0.02}=\mathbf{6 4}
$$

SOLVED PROBLEM 5.13 .5 ml of HI are produced by the interaction of 8.1 ml of hydrogen and 9.3 ml of iodine vapour at $444^{\circ} \mathrm{C}$. Calculate the equilibrium constant at this temperature of the reaction.

$$
\mathrm{H}_{2}(\mathrm{~g})+\mathrm{I}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{HI}(\mathrm{~g})
$$

SOLUTION
The equilibrium constant expression for the reaction is

$$
K_{c}=\frac{[\mathrm{HI}]^{2}}{\left[\mathrm{H}_{2}\right]\left[\mathrm{I}_{2}\right]}
$$

Let us proceed to find the equilibrium concentrations.

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Since the number of moles in a gas under the same conditions of temperature and pressure are proportional to volumes, ml of a gas may be used instead of molar concentrations. Thus,

$$
\mathrm{H}_{2}+\mathrm{I}_{2} \rightleftharpoons 2 \mathrm{HI}
$$

Equilibrium volumes: $(8.1-x) \quad(9.3-x) \quad 2 x$
The experimental volume of $\mathrm{HI}=13.5 \mathrm{ml}$ (given)

$$
\begin{aligned}
\therefore & 2 x & =13.5 \mathrm{ml} \\
\text { or } & x & =6.75 \mathrm{ml}
\end{aligned}
$$

Thus, the equilibrium concentrations are:

$$
\begin{aligned}
{\left[\mathrm{H}_{2}\right] } & =(8.1-x)=8.1-6.75=1.35 \\
{\left[\mathrm{I}_{2}\right] } & =(9.3-x)=9.3-6.75=2.55 \\
{[\mathrm{HI}] } & =13.5
\end{aligned}
$$

Substituting these values in the equilibrium constant expression, we have

$$
K_{c}=\frac{[\mathrm{HI}]^{2}}{\left[\mathrm{H}_{2}\right]\left[\mathrm{I}_{2}\right]}=\frac{(13.5)^{2}}{1.35 \times 2.55}=\mathbf{5 2 . 9 4}
$$

## Calculation of Equilibrium Concentrations

SOLVED PROBLEM 1. One mole of $\mathrm{H}_{2}$ and one mole of $\mathrm{I}_{2}$ were heated in a 1 litre sealed glass box at $490^{\circ} \mathrm{C}$ till the equilibrium was reached. Assuming that the equilibrium constant is 45.9 , find the final concentrations of $\mathrm{H}_{2}, \mathrm{I}_{2}$ and HI .

SOLUTION
The equation for the reaction is

$$
\mathrm{H}_{2}+\mathrm{I}_{2} \rightleftharpoons 2 \mathrm{HI}
$$

If $x$ mole of $\mathrm{H}_{2}$ has reacted on attainment of equilibrium, the moles of components are

$$
\underset{(1-x)}{\mathrm{H}_{2}}+\underset{(1-x)}{\mathrm{I}_{2}} \rightleftharpoons \underset{2 \mathrm{x})}{\rightleftharpoons} \rightleftharpoons \begin{array}{r}
2 \mathrm{HI} \\
2
\end{array}
$$

Since the reaction vessel is a 1 litre box, the concentrations at equilibrium are the same as the moles. Thus,

$$
\begin{aligned}
{\left[\mathrm{H}_{2}\right] } & =1-x \\
{\left[\mathrm{I}_{2}\right] } & =1-x \\
{[\mathrm{HI}] } & =2 x
\end{aligned}
$$

Substituting the values in the equilibrium constant expression
or

$$
K=\frac{[\mathrm{HI}]^{2}}{\left[\mathrm{H}_{2}\right]\left[\mathrm{I}_{2}\right]}=\frac{(2 x)^{2}}{(1-x)(1-x)}=45.9
$$

$$
\frac{4 x^{2}}{1-2 x+x^{2}}=45.9
$$

or

$$
41.9 x^{2}-91.8 x+45.9=0
$$

Using the quadratic formula $x=0.79$. Hence the equilibrium concentrations are

$$
\begin{aligned}
{\left[\mathrm{H}_{2}\right] } & =1-0.79=0.21 \text { mole per litre } \\
{\left[\mathrm{I}_{2}\right] } & =1-0.79=0.21 \text { mole per litre } \\
{[\mathrm{HI}] } & =2 x=2(0.79)=\mathbf{1 . 5 8} \text { mole per litre }
\end{aligned}
$$

SOLVED PROBLEM 2. At a certain temperature, $K$ for the reaction $3 \mathrm{C}_{2} \mathrm{H}_{2}(\mathrm{~g}) \rightleftharpoons \mathrm{C}_{6} \mathrm{H}_{6}(\mathrm{~g})$ is 4 . If the equilibrium concentration of $\mathrm{C}_{2} \mathrm{H}_{2}$ is 0.5 mole/litre, what is the concentration of $\mathrm{C}_{6} \mathrm{H}_{6}$ ?

SOLUTION
The reaction can be written as

$$
3 \mathrm{C}_{2} \mathrm{H}_{2} \rightleftharpoons \mathrm{C}_{6} \mathrm{H}_{6}
$$

The equilibrium constant expression is

$$
K=\frac{\left[\mathrm{C}_{6} \mathrm{H}_{6}\right]}{\left[\mathrm{C}_{2} \mathrm{H}_{2}\right]^{3}}
$$

It is given that:

$$
\begin{aligned}
K & =4 \\
{\left[\mathrm{C}_{2} \mathrm{H}_{2}\right] } & =0.5 \mathrm{~mole} / \mathrm{litre}
\end{aligned}
$$

Substituting these values,

$$
\begin{aligned}
& 4 & =\frac{\left[\mathrm{C}_{6} \mathrm{H}_{6}\right]}{[0.5]^{3}} \\
\therefore & {\left[\mathrm{C}_{6} \mathrm{H}_{6}\right] } & =4 \times(0.5)^{3}=\mathbf{0 . 5} \text { moles/litre }
\end{aligned}
$$

SOLVED PROBLEM 3. For the reaction

$$
\mathrm{CO}_{2}(\mathrm{~g})+\mathrm{H}_{2}(\mathrm{~g}) \rightleftharpoons \mathrm{CO}(\mathrm{~g})+\mathrm{H}_{2} \mathrm{O}(\mathrm{~g})
$$

the value of $K$ at $552^{\circ} \mathrm{C}$ is 0.137 . If 5 moles of $\mathrm{CO}_{2}, 5.0$ moles of $\mathrm{H}_{2}, 1.0$ mole of CO and 1.0 mole of $\mathrm{H}_{2} \mathrm{O}$ are initially present, what are the actual concentrations of $\mathrm{CO}_{2}, \mathrm{H}_{2}, \mathrm{CO}$ and $\mathrm{H}_{2} \mathrm{O}$ at equilibrium?

SOLUTION
If $x$ moles of $\mathrm{CO}_{2}$ has reacted at equilibrium, $x$ mole of CO and $x$ mole of $\mathrm{H}_{2} \mathrm{O}$ will be produced. The moles at equilibrium due to the reaction will be

$$
\begin{array}{llll} 
& \mathrm{CO}_{2}+\mathrm{H}_{2} & \rightleftharpoons & \mathrm{CO}+\mathrm{H}_{2} \mathrm{O} \\
\text { Moles at equilibrium : } \\
5-x & 5-x & & x \quad x
\end{array}
$$

But 1 mole each of CO and $\mathrm{H}_{2} \mathrm{O}$ were present initially. Therefore the actual moles at equilibrium would be

$$
\begin{aligned}
\mathrm{CO}_{2} & =5-x \\
\mathrm{H}_{2} & =5-x \\
\mathrm{CO} & =1+x \\
\mathrm{H}_{2} \mathrm{O} & =1+x
\end{aligned}
$$

If $V$ litres be the volume of the reaction vessel, the concentration of the various species are:

$$
\begin{aligned}
{\left[\mathrm{CO}_{2}\right] } & =(5-x) / V \\
{\left[\mathrm{H}_{2}\right] } & =(5-x) / V \\
{[\mathrm{CO}] } & =(1+x) / V \\
{\left[\mathrm{H}_{2} \mathrm{O}\right] } & =(1+x) / V
\end{aligned}
$$

Substituting the values in the equilibrium constant expression, we have

$$
\begin{aligned}
K & =\frac{[\mathrm{CO}]\left[\mathrm{H}_{2} \mathrm{O}\right]}{\left[\mathrm{CO}_{2}\right]\left[\mathrm{H}_{2}\right]} \\
0.137 & =\frac{[(1+x) / V][(1+x) / V]}{[(5-x) / V][(5-x) / V]}=\frac{(1+x)^{2} V^{2}}{(5-x)^{2} V^{2}}
\end{aligned}
$$

or

$$
0.137=\frac{(1+x)^{2}}{(5-x)^{2}}=\frac{1+2 x+x^{2}}{25-10 x+x^{2}}
$$

$$
\begin{aligned}
& 0.137(25)-0.137(10) x+0.137 x^{2}=1+2 x+x^{2} \\
& 0.863 x^{2}+3.370 x-2.425=0
\end{aligned}
$$

Solving for $x$ using the quadratic formula

$$
x=0.62
$$

Thus the final equilibrium concentrations are:

$$
\begin{aligned}
{[\mathrm{CO}] } & =1+x=1+0.62=1.62 \mathrm{~mole}^{-1} \\
{\left[\mathrm{H}_{2} \mathrm{O}\right] } & =1+x=1+0.62=1.62 \mathrm{~mole}^{-1} \\
{\left[\mathrm{CO}_{2}\right] } & =5-x=5-0.62=4.38 \mathrm{~mole}^{-1} \\
{\left[\mathrm{H}_{2}\right] } & =5-x=5-0.62=4.38 \text { mole } \mathbf{1}^{-1}
\end{aligned}
$$

SOLVED PROBLEM 4. For the reaction $\mathrm{I}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{I}(\mathrm{g}), K=3.76 \times 10^{-5}$ at $727^{\circ} \mathrm{C}$. Let 1 mole of $\mathrm{I}_{2}$ be injected into a 2-litre glass box at $727^{\circ} \mathrm{C}$. What will be the concentrations of $\mathrm{I}_{2}$ and I when the equilibrium is attained?

SOLUTION
The balanced equation for the reaction is

$$
\mathrm{I}_{2} \rightleftharpoons 2 \mathrm{I}
$$

1 mole of $I_{2}$ is injected in a 2-litre box. Thus the initial concentration of $I_{2}$ is

$$
\frac{1 \text { mole }}{2 \text { litre }}=0.5 \mathrm{M}
$$

Let $x$ moles of $\mathrm{I}_{2}$ decompose at equilibrium. Then the moles of the two species are:

$$
\left.\begin{array}{rl}
\mathrm{I}_{2} & \rightleftharpoons 2 \mathrm{I} \\
0.5-x
\end{array}\right) 2 x
$$

Therefore the equilibrium concentrations are:

$$
\begin{aligned}
{\left[\mathrm{I}_{2}\right] } & =0.5-x \\
{[\mathrm{I}] } & =2 x
\end{aligned}
$$

$$
\text { and } \quad K=3.76 \times 10^{-5}
$$

Substituting the values in the equilibrium constant expression, we have

$$
\mathrm{K}=\frac{[\mathrm{I}]^{2}}{\left[\mathrm{I}_{2}\right]}=3.76 \times 10^{-5}
$$

or

$$
\frac{(2 x)^{2}}{(0.5-x)}=3.76 \times 10^{-5}
$$

Solving for $x$, using the quadratic equation formula,

$$
x=2.17 \times 10^{-3}
$$

Thus the concentrations of I and $\mathrm{I}_{2}$ at equilibrium are:

$$
\begin{aligned}
{[I] } & =2 x=\mathbf{4 . 3 4} \times \mathbf{1 0}^{-\mathbf{3}} \text { mole } \mathbf{1}^{\mathbf{- 1}} \\
{\left[\mathrm{I}_{2}\right] } & =0.5-x=\mathbf{0} .498 \text { mole }^{-1}
\end{aligned}
$$

## CALCULATIONS INVOLVING $\boldsymbol{K}_{\boldsymbol{p}}$

It may be noted that the value of $K_{p}$ depends on the units used to express pressures, which are usually atmospheres.

## Calculation of $K_{p}$

SOLVED PROBLEM 1. The reaction

$$
2 \mathrm{NO}(\mathrm{~g})+\mathrm{Cl}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{NOCl}(\mathrm{~g})
$$

was studied at $25^{\circ} \mathrm{C}$. The partial pressures at equilibrium were found to be

$$
\begin{aligned}
p_{\mathrm{NOCl}} & =1.2 \mathrm{~atm} \\
p_{\mathrm{NO}} & =5.0 \times 10^{-2} \mathrm{~atm} \\
P_{C l_{2}} & =3.0 \times 10^{-1} \mathrm{~atm}
\end{aligned}
$$

Calculate $K_{p}$ for the reaction at $25^{\circ} \mathrm{C}$.
SOLUTION
The equilibrium constant expression in terms of partial pressures is

$$
K_{p}=\frac{\left(p_{\mathrm{NOCl}}\right)^{2}}{\left(p_{\mathrm{NO}}\right)^{2}\left(p_{\mathrm{Cl}_{2}}\right)}
$$

Substituting the values of partial pressures

$$
K_{p}=\frac{(1.2)^{2}}{\left(5.0 \times 10^{-2}\right)^{2} \times\left(3.0 \times 10^{-1}\right)}=1.92 \times 10^{3}
$$

SOLVED PROBLEM 2. At $60^{\circ} \mathrm{C}$ and a total pressure of 1 atmosphere dinitrogen tetroxide, $\mathrm{N}_{2} \mathrm{O}_{4}$, is $50 \%$ dissociated into nitrogen dioxide, $\mathrm{NO}_{2}$.

$$
\mathrm{N}_{2} \mathrm{O}_{4}(g) \rightleftharpoons 2 \mathrm{NO}_{2}(g)
$$

Calculate the value of $K_{p}$ at this temperature.
SOLUTION
Let us have 1 mole of $\mathrm{N}_{2} \mathrm{O}_{4}$ to start with of which $x$ mole dissociates at equilibrium. Then the moles of $\mathrm{N}_{2} \mathrm{O}_{4}$ and $\mathrm{NO}_{2}$ at equilibrium are:

$$
\begin{aligned}
& \mathrm{N}_{2} \mathrm{O}_{4} \rightleftharpoons 2 \mathrm{NO}_{2} \\
& \text { moles at equilibrium : } \\
&(1-x) 2 x
\end{aligned}
$$

Since $\mathrm{N}_{2} \mathrm{O}_{4}$ is $50 \%$ dissociated, $x=0.5$ mole and the equilibrium mixture contains

$$
\begin{aligned}
\mathrm{NO}_{2} & =2 x=2 \times 0.5=1 \text { mole } \\
\mathrm{N}_{2} \mathrm{O}_{4} & =(1-x)=(1-0.5)=0.5 \text { mole }
\end{aligned}
$$

That is, the moles of $\mathrm{N}_{2} \mathrm{O}_{4}$ and $\mathrm{NO}_{2}$ are present in the ratio 1:2
$\therefore$ The partial pressure of $\mathrm{N}_{2} \mathrm{O}_{4}=\frac{1}{3}$ atm
The partial pressure of $\mathrm{NO}_{2}=\frac{2}{3}$ atm
Substituting these values in the equilibrium constant expression, we have

$$
K_{p}=\frac{\left(p_{\mathrm{NO}_{2}}\right)^{2}}{p_{\mathrm{N}_{2} \mathrm{O}_{4}}}=\frac{(2 / 3)^{2}}{1 / 3}=\frac{4}{3}=1.33
$$

## Calculation of Equilibrium Partial Pressures

SOLVED PROBLEM 1. At $727^{\circ} \mathrm{C}$ the equilibrium constant for the reaction

$$
2 \mathrm{SO}_{2}(g)+\mathrm{O}_{2}(g) \rightleftharpoons 2 \mathrm{SO}_{3}(g)
$$

is $K_{p}=3.50 \mathrm{~atm}^{-1}$. If the total pressure in the reaction flask is 1.00 atm , and the partial pressure of $\mathrm{O}_{2}$ at equilibrium is 0.10 atm , calculate the partial pressures of $\mathrm{SO}_{2}$ and $\mathrm{SO}_{3}$.

## SOLUTION

Let the partial pressure of $\mathrm{SO}_{2}=x \mathrm{~atm}$
Then the partial pressure of $\mathrm{SO}_{3}=1.00-p_{O_{2}}-x$

$$
\begin{aligned}
& =(0.90-x) \mathrm{atm} \\
\text { the partial pressure of } \mathrm{O}_{2} & =0.10 \mathrm{~atm}
\end{aligned}
$$

Substituting these values in the equilibrium constant expression, we have

$$
K_{p}=\frac{\left(p_{\mathrm{SO}_{3}}\right)^{2}}{\left(p_{\mathrm{SO}_{2}}\right)^{2}\left(p_{\mathrm{O}_{2}}\right)}=\frac{(0.90-x)^{2}}{x^{2} \times 0.1}=3.5 \mathrm{~atm}^{-1}
$$

Taking the square root, we have

$$
\frac{0.9-x}{x}=(0.35)^{\frac{1}{2}}
$$

or

$$
x=0.57
$$

$$
\begin{aligned}
& p_{\mathrm{SO}_{2}}=\mathbf{0 . 5 7} \mathrm{atm} \\
& p_{\mathrm{SO}_{3}}=\mathbf{0} .33 \mathrm{~atm}
\end{aligned}
$$

## Calculation of Degree of Dissociation

Case 1. By determining equilibrium concentrations. The equilibrium constant $(K)$ for the combination reaction is first calculated using equilibrium concentrations. The equilibrium law is then applied to the reverse (dissociation) reaction when the equilibrium constant is $1 / K$.

SOLVED PROBLEM 1.25 ml of $\mathrm{H}_{2}$ and 18 ml of $\mathrm{I}_{2}$ vapour were heated in a sealed glass bulb at $465^{\circ} \mathrm{C}$ when at equilibrium 30.8 ml of HI was formed. Calculate the degree of dissociation of pure HI at $465^{\circ} \mathrm{C}$.

## SOLUTION

## Step 1. Calculation of $K$

The combination of $\mathrm{H}_{2}$ and $\mathrm{I}_{2}$ to form HI can be written as

$$
\mathrm{H}_{2}+\mathrm{I}_{2} \rightleftharpoons 2 \mathrm{HI}
$$

ml at equilibrium: $(a-x) \quad(b-x) \quad 2 x$
At equilibrium, HI formed is $2 x \mathrm{ml}$

$$
\text { or } \quad \begin{aligned}
2 x & =30.8 \text { (given) } \\
x & =15.4
\end{aligned}
$$

$\therefore$ Concentrations at equilibrium are:

$$
\begin{aligned}
{\left[\mathrm{H}_{2}\right] } & =(a-x)=25-15.4=9.6 \text { mole } 1^{-1} \\
{\left[\mathrm{I}_{2}\right] } & =(b-x)=18-15.4=2.6 \text { mole }^{-1} \\
{[\mathrm{HI}] } & =30.8 \text { mole } 1^{-1}
\end{aligned}
$$

Substituting the values in the equilibrium constant expression

$$
K=\frac{[\mathrm{HI}]^{2}}{\left[\mathrm{H}_{2}\right]\left[\mathrm{I}_{2}\right]}=\frac{30.8 \times 30.8}{9.6 \times 2.6}=38
$$

Step 2. Calculation of Degree of dissociation, $x$
If we inject one ml of HI in a sealed glass bulb at $465^{\circ} \mathrm{C}, x \mathrm{ml}$ of it will decompose at equilibrium, where $x$ represents the degree of dissociation.
$\begin{array}{llll} & 2 \mathrm{HI} & \rightleftharpoons \mathrm{H}_{2}+ & \mathrm{I}_{2} \\ \mathrm{ml} \text { at equilibrium: } & 1-x & x / 2 \quad x / 2\end{array}$
Substituting the values in the equilibrium constant expression

$$
K^{\prime}=\frac{[x / 2]^{2}}{(1-x)^{2}}=\frac{x^{2}}{4(1-x)^{2}}
$$

Since $\quad K^{\prime}=1 / K$, we have

Hence

$$
\frac{x^{2}}{4(1-x)^{2}}=\frac{1}{38}
$$

Thus the degree of dissociation of pure HI at $465^{\circ} \mathrm{C}$ is $\mathbf{0 . 2 4 5}$.
SOLVED PROBLEM 2. For the reaction $\mathrm{PCl}_{5} \rightleftharpoons \mathrm{PCl}_{3}+\mathrm{Cl}_{2}, K=33.3$ at 760 K .1 .00 g of $\mathrm{PCl}_{5}$ is injected into a 500 ml evacuated flask and allowed to come to equilibrium. What per cent of the $\mathrm{PCl}_{5}$ will dissociate at equilibrium? Molecular mass of $\mathrm{PCl}_{5}=208.235$.

SOLUTION

$$
\begin{aligned}
\text { Initial moles of } \mathrm{PCl}_{5} & =\frac{\text { grams (mass) }}{\text { mol.mass }}=\frac{1}{208.235}=0.0048 \text { mole } \\
\text { Initial concentration of } \mathrm{PCl}_{5} & =\frac{0.0048 \text { mole }}{0.5 \text { litre }}=0.0096 \mathrm{~mol} \mathrm{l}^{-1}
\end{aligned}
$$

At equilibrium if $x$ mole of $\mathrm{PCl}_{5}$ is dissociated, the equilibrium concentrations are:

$$
\begin{array}{cc}
\mathrm{PCl}_{5} \\
0.0096-x & \rightleftharpoons \mathrm{PCl}_{3} \\
x
\end{array}+\underset{x}{\mathrm{Cl}_{2}}
$$

Substituting values in the equilibrium constant expression,

$$
\begin{aligned}
& \frac{\left[\mathrm{PCl}_{3}\right]\left[\mathrm{Cl}_{2}\right]}{\left[\mathrm{PCl}_{5}\right]}=33.3 \\
& \frac{(x)(x)}{(0.0096-x)}=33.3
\end{aligned}
$$

Solving for $x$ using the quadratic equation obtained by you, we have

$$
x=9.597 \times 10^{-3}
$$

$\therefore$ The initial concentration of $\mathrm{PCl}_{5}=0.0096 \mathrm{~mol} \mathrm{l}^{-1}$
The final concentration of $\mathrm{PCl}_{5}=0.0096-x$

$$
\begin{aligned}
& =0.0096-9.597 \times 10^{-3} \\
& =3 \times 10^{-6} \mathrm{moll}^{-1}
\end{aligned}
$$

Thus the amount of $\mathrm{PCl}_{5}$ dissociated at equilibrium is

$$
100 \times \frac{0.0096-3 \times 10^{-6}}{0.0096}=\mathbf{9 9 . 9 \%}
$$

Case 2. By density measurements. This method is used for the determination of the degree of dissociation of gases in which one molecule produces two or more molecules. For example, $\mathrm{PCl}_{5}$ dissociates to give two molecules $\mathrm{PCl}_{3}$ and $\mathrm{Cl}_{2}$.

$$
\mathrm{PCl}_{5} \rightleftharpoons \mathrm{PCl}_{3}+\mathrm{Cl}_{2}
$$

Thus at constant temperature and pressure the volume increases. The density at constant pressure then decreases. The degree of dissociation can be calculated from the difference between the density of the undissociated gas and that of the partially dissociated gas at equilibrium.

If we start with one mole of gas $\left(\mathrm{PCl}_{5}\right)$ and the degree of dissociation is $x$, we have

$$
\begin{array}{cccc} 
& \mathrm{PCl}_{5} & \rightleftharpoons \mathrm{PCl}_{3} & +\mathrm{Cl}_{2} \\
\text { moles at equilibrium : } \\
(1-x) & x & x
\end{array}
$$

Thus the total number of moles at equilibrium

$$
=(1-x)+x+x=1+x
$$

The density of an ideal gas at constant temperature and pressure is inversely proportional to the number of moles for a given weight.

Hence the ratio of density $\rho_{1}$ of the undissociated gas to the density $\rho_{2}$ of the dissociated gas at equilibrium is given as

$$
\frac{\rho_{1}}{\rho_{2}}=\frac{1+x}{1}
$$

whence

$$
\begin{aligned}
\rho_{1} & =\rho_{2}+x \rho_{2} \\
x & =\frac{\rho_{1}-\rho_{2}}{\rho_{2}}
\end{aligned}
$$

Substituting the values of $\rho_{1}$ and $\rho_{2}$ the value of $x$, the degree of dissociation, can be calculated.
SOLVED PROBLEM 1. When $\mathrm{PCl}_{5}$ is heated it gasifies and dissociates into $\mathrm{PCl}_{3}$ and $\mathrm{Cl}_{2}$. The density of the gas mixture at $200^{\circ} \mathrm{C}$ is 70.2 . Find the degree of dissociation of $\mathrm{PCl}_{5}$ at $200^{\circ} \mathrm{C}$.

SOLUTION
We will use the expression $\quad x=\frac{\rho_{1}-\rho_{2}}{\rho_{2}}$
where $\quad x=$ degree of dissociation

$$
\rho_{1}=\text { density of undissociated } \mathrm{PCl}_{5}
$$

$$
\rho_{2}=\text { density of gas mixture at equilibrium (partially dissociated) }
$$

The density $\left(\rho_{1}\right)$ of undissociated $\mathrm{PCl}_{5}$ would be

$$
\mathrm{VD}=\frac{\text { mol mass }}{2}=\frac{31+177.5}{2}=104.25
$$

Observed density $\rho_{2}=70.2$

$$
\therefore \quad x=\frac{\rho_{1}-\rho_{2}}{\rho_{2}}=\frac{104.25-70.2}{70.2}=\mathbf{0 . 4 8 5}
$$

SOLVED PROBLEM 2. At $90^{\circ} \mathrm{C}$ the vapour density of nitrogen tetroxide $\left(\mathrm{N}_{2} \mathrm{O}_{4}\right)$ is 24.8 . Calculate the percentage dissociation into $\mathrm{NO}_{2}$ molecules at this temperature.

SOLUTION
The dissociation of $\mathrm{N}_{2} \mathrm{O}_{4}$ can be represented by the equation

$$
\mathrm{N}_{2} \mathrm{O}_{4} \rightleftharpoons \mathrm{NO}_{2}+\mathrm{NO}_{2}
$$

Since the number of molecules on the two sides of the equation is different, we can calculate the degree of dissociation by using the expression

$$
x=\frac{\rho_{1}-\rho_{2}}{\rho_{2}}
$$

The density of undissociated $\mathrm{N}_{2} \mathrm{O}_{4}$ is given by

$$
\begin{aligned}
& \rho_{1} \\
& =\frac{\text { mol mass }}{2}=\frac{28+64}{2}=\frac{92}{2}=46 \\
\rho_{2} & =24.8 \text { (given) } \\
\therefore \quad x & =\frac{46-24.8}{24.8}=0.8547
\end{aligned}
$$

Hence, percentage dissociation $=100 \times x=\mathbf{8 5 . 4 7}$
Case 3. By molecular mass determination. Molecular masses are proportional at constant temperature and pressure to the gas densities. Therefore, we can substitute molecular masses for the densities in the expression

$$
\begin{aligned}
& x=\frac{\rho_{1}-\rho_{2}}{\rho_{2}} \\
& x=\frac{M_{1}-M_{2}}{M_{2}}
\end{aligned}
$$

where $M_{1}$ is the molecular mass of the undissociated gas and $M_{2}$ is the average molecular mass of the gases at the equilibrium.

SOLVED PROBLEM. 1.588 g of nitrogen tetroxide gives a total pressure of 1 atm when partially dissociated at equilibrium in a 500 ml glass vessel at $25^{\circ} \mathrm{C}$. What is the degree of dissociation at this temperature.

SOLUTION
$M_{1}$, molecular mass of undissociated $\mathrm{N}_{2} \mathrm{O}_{4}$ gas

$$
=14 \times 2+16 \times 4=92.0
$$

$M_{2}$, molecular mass of partially dissociated gas at equilibrium can be determined by using the general gas equation.
where

$$
P V=n R T
$$

$$
n=\frac{\text { mass of substance }}{M_{2}}=\frac{m}{M_{2}}
$$

or

$$
\begin{equation*}
P V=\frac{m}{M_{2}} R T \tag{1}
\end{equation*}
$$

Rearranging the expression (1), we have

$$
\begin{equation*}
M_{2}=\frac{R T}{P} \times \frac{m}{V} \tag{2}
\end{equation*}
$$

Here,

$$
\begin{aligned}
& R=0.082 ; T=273+25=298 \mathrm{~K} \\
& P=1 \mathrm{~atm} ; V=0.500 \text { litre } ; m=1.588 \mathrm{~g}
\end{aligned}
$$

Substituting the values in the expression (2)

Therefore,

$$
\begin{aligned}
M_{2} & =\frac{0.082 \times 298 \times 1.588}{(1 \mathrm{~atm})(0.500 \text { litre })}=77.68 \\
x & =\frac{M_{1}-M_{2}}{M_{2}}=\frac{92.0-77.68}{77.68} \\
& =\mathbf{0 . 1 8 4 6}
\end{aligned}
$$

## UNITS OF EQUILIBRIUM CONSTANT

In the equilibrium expression for a particular reaction, the concentrations are given in units of moles/litre or mol/L, and the partial pressure are given in atmospheres (atm). The units of $K_{c}$ and $K_{p}$, depend on the specific reaction.
(1) When the total number of moles of reactants and products are equal

In the equilibrium expression of these reactions, the concentration or pressure terms in the numerator and denominator exactly cancel out. Thus $K_{c}$ or $K_{p}$ for such a reaction is without units.

Taking example of the reaction

$$
\begin{aligned}
\mathrm{H}_{2}(g)+\mathrm{I}_{2}(g) & \rightleftharpoons 2 \mathrm{HI}(g) \\
K_{c} & =\frac{[\mathrm{HI}]^{2}}{\left[\mathrm{H}_{2}\right]\left[\mathrm{I}_{2}\right]}=\frac{(\mathrm{mol} / \mathrm{L})^{2}}{(\mathrm{~mol} / \mathrm{L})(\mathrm{mol} / \mathrm{L})} \quad \text { (No units) } \\
K_{p} & =\frac{\left(P_{\mathrm{HI}}\right)^{2}}{\left(P_{\mathrm{H}_{2}}\right)\left(P_{\mathrm{I}_{2}}\right)}=\frac{(\mathrm{atm})^{2}}{(\mathrm{~atm})(\mathrm{atm})} \quad \text { (No units) }
\end{aligned}
$$

(2) When the total number of moles of the reactants and products are unequal

In such reactions $K_{c}$ will have units ( $\mathrm{mol} /$ litre) ${ }^{n}$ and $K_{p}$ will have units (atm) $)^{n}$, where $n$ is equal to the total number of moles of products minus the total number of moles of reactants. Thus for the reaction

$$
\begin{aligned}
\mathrm{N}_{2} \mathrm{O}_{4}(g) & \rightleftharpoons 2 \mathrm{NO}_{2}(g) \\
K_{c} & =\frac{\left[\mathrm{NO}_{2}\right]^{2}}{\left[\mathrm{~N}_{2} \mathrm{O}_{4}\right]}=\frac{(\mathrm{mol} / \mathrm{L})^{2}}{(\mathrm{~mol} / \mathrm{L})}=\mathrm{mol} / \mathrm{L} \\
K_{p} & =\frac{\left(p_{\mathrm{NO}_{2}}\right)^{2}}{\left(P_{\mathrm{N}_{2} \mathrm{O}_{4}}\right)}=\frac{(\mathrm{atm})^{2}}{(\mathrm{~atm})}=\mathrm{atm}
\end{aligned}
$$

Thus units for $K_{c}$ are $\mathrm{mol} / \mathrm{L}$ and for $K_{p}$ units are atm. For the reaction

$$
\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \rightleftharpoons 2 \mathrm{NH}_{3}(g)
$$

the units for $K_{c}$ and $K_{p}$ may be found as follows

$$
\begin{aligned}
& K_{c}=\frac{\left[\mathrm{NH}_{3}\right]^{2}}{\left[\mathrm{~N}_{2}\right]\left[\mathrm{H}_{2}\right]^{3}}=\frac{(\mathrm{mol} / \mathrm{L})^{2}}{(\mathrm{~mol} / \mathrm{L})(\mathrm{mol} / \mathrm{L})^{3}}=\mathrm{mol}^{-2} \mathrm{~L}^{2} \\
& K_{p}=\frac{\left(p_{\mathrm{NH}_{3}}\right)^{2}}{\left(p_{\mathrm{N}_{2}}\right)\left(p_{\mathrm{H}_{2}}\right)^{3}}=\frac{(\mathrm{atm})^{2}}{(\mathrm{~atm})(\mathrm{atm})^{3}}=\mathrm{atm}^{-2}
\end{aligned}
$$

Thus units of $K_{c}$ are $\mathrm{mol}^{-2} \mathrm{~L}^{2}$ and units of $K_{p}$ are atm ${ }^{-2}$.
It may be noted, however, that the units are often omitted when equilibrium constants are listed in tables.
Thermodynamic Derivation of Law of Chemical Equilibrium
Let us consider a general reaction

$$
a \mathrm{~A}+b \mathrm{~B}+\ldots \rightleftharpoons c \mathrm{C}+d \mathrm{D}+\ldots
$$

The chemical potential of a substance in a mixture is related to its activity by the expression

$$
\begin{equation*}
\mu=\mu^{\circ}+R T \ln a \tag{i}
\end{equation*}
$$

where $\mu^{\circ}$ is the chemical potential of the pure substance in standard state of unit activity, $R$ is gas constant and $T$ the absolute temperature.

For $a$ mole of the substance A we can write using the equation (i)

$$
a \mu_{\mathrm{A}}=a\left(\mu^{\circ}+R T \ln a_{A}\right)
$$

and similarly

$$
\begin{aligned}
b \mu_{\mathrm{B}} & =b\left(\mu^{\circ}+R T \ln a_{B}\right) \\
c \mu_{c} & =c\left(\mu^{\circ}+R T \ln a_{c}\right) \\
d \mu_{D} & =d\left(\mu^{\circ}+R T \ln a_{D}\right)
\end{aligned}
$$

The change in free energy for the reaction is given by

$$
\Delta G=G_{\text {products }}-G_{\text {reactants }}
$$

On substitution we get

$$
\begin{align*}
& \Delta G=\left(c \mu_{c}+d \mu_{D}+\ldots\right)-\left(a \mu_{\mathrm{A}}+b \mu_{B}+\ldots\right) \\
&=\left[c\left\{\mu_{\mathrm{c}}^{\circ}+R T \ln a_{\mathrm{C}}\right\}+d\left\{\mu^{\circ}{ }_{D} R T \ln a_{\mathrm{D}}\right\}\right] \\
&-\left[a\left\{\mu_{a}^{\circ}+R T \ln a_{A}\right\}+b\left\{\mu_{B}^{\circ} R T \ln a_{B}\right\}\right] \\
&=\left[\left\{c \mu_{\mathrm{c}}^{\circ}+d \mu_{D_{D}}^{\circ}+\ldots\right\}-\left\{a \mu_{A}^{\circ}+b \mu_{B}^{\circ}+\ldots \ldots . .\right\}\right]+R T \ln \frac{a_{C}^{c} \times a_{D}^{d} \times \ldots}{a_{A}^{a} \times a_{B}^{b} \times \ldots} \\
& \Delta G=\Delta G^{\circ}+R T \ln \frac{a_{C}^{c} \times a_{D}^{d} \times \ldots}{a_{A}^{a} \times a_{B}^{b} \times \ldots} \tag{ii}
\end{align*}
$$

where $\Delta G^{\circ}$ is the difference in free energy of the reaction when all reactants and products are in their standard state. It is given by

$$
\Delta \mathrm{G}^{\circ}=\left\{c \mu_{c}^{\circ}+d \mu_{D}^{\circ}+\ldots\right\}-\left\{a \mu_{\mathrm{A}}^{\circ}+b \mu_{B}^{\circ}+\ldots\right\}
$$

In equation (ii) the factor A given by

$$
\frac{a_{C}{ }^{c} \times{a_{D}}^{d} \times \ldots}{a_{A}^{a} \times{a_{B}}^{b} \times \ldots}
$$

stands for the reaction quotient of activities of the product and reactants. It may be denoted by $J$. The equation (ii) becomes

$$
\begin{equation*}
\Delta G=\Delta \mathrm{G}^{\circ}+R T \ln J \tag{iii}
\end{equation*}
$$

The equation (iii) is called van't Hoff reaction isotherm
For the reaction at equilibrium

$$
\Delta G=0
$$

therefore,

$$
\Delta G^{\circ}=-R T \ln J
$$

or

$$
\Delta G=-R T \ln \frac{a_{C}^{c} \times a_{D}^{d} \times \ldots}{a_{A}^{a} \times a_{B}^{b} \times \ldots}
$$

As $\Delta G^{\circ}$ is the free energy of the reaction in the standard state and is constant at a given temperature.

Also, the gas constant $R$ and $T$ are constant, the factor

$$
\frac{a_{C}^{c} \times a_{D}^{d} \times \ldots}{a_{A}^{a} \times a_{B}^{b} \times \ldots}
$$

is a constant i.e.

$$
\frac{a_{C}^{c} \times a_{D}^{d} \times \ldots}{a_{A}^{a} \times a_{B}^{b} \times \ldots}=a \text { constant }=K
$$

It is nothing but the law of chemical equilibrium. Therefore, from equation (iii) we have
or

$$
\begin{align*}
& \Delta G^{\circ}=-R T \ln K  \tag{iv}\\
& \Delta G^{\circ}=-2.303 R T \log K \tag{v}
\end{align*}
$$

The equation (iv) is also called van't Hoff Isotherm. It may be used to calculate the change in free energy of a reaction in the standard $\left(\Delta G^{\circ}\right)$ from the equilibrium constant and vice-versa.

The sign of $\Delta G^{\circ}$ indicates whether the forward or reverse reaction is spontaneous. Considering the equation (iv), we can have three possibilities depending on the sign of $\Delta G^{\circ}$ for the reaction.
(1) If $\Delta G^{\circ}$ is negative, $\log K$ must be positive and the reaction proceeds spontaneously in the forward reaction.
(2) If $\boldsymbol{\Delta} \boldsymbol{G}^{\circ}$ is positive, $\log K$ must be negative and $K$ is less than one. The reverse reaction is then spontaneous.
(3) If $\boldsymbol{\Delta} \boldsymbol{G}^{\circ}=\mathbf{0}, \log K=0$ and $K=1$. The reaction is at equilibrium.

## Meaning of the Magnitude of the Free Energy Change

If $\Delta G^{\circ}$ is a large negative number, $K$ will be much greater than one and the forward reaction will proceed nearly to completion. On the other hand if $\Delta G^{\circ}$ is a large positive number, $K$ will be a small fraction. Then the reverse reaction will proceed almost to completion.

SOLVED PROBLEM 1. Calculate $K$ for reaction which has $\Delta G^{\circ}$ value -20 kcal at $25^{\circ} \mathrm{C}$.
SOLUTION
We know that

$$
\begin{equation*}
\Delta G^{\circ}=-2.303 R T \log K \tag{a}
\end{equation*}
$$

where $\Delta G^{\circ}$ is standard free energy; $R$ is gas constant; $T$ is absolute temperature; and $K$ is equilibrium constant. It must be remembered that the same units of $\Delta G^{\circ}, R$ and $T$ are to be used in a given problem.

If $\Delta G^{\circ}$ is given in calories

$$
\begin{aligned}
R & =1.99 \\
T & =25+273=298 \mathrm{~K}
\end{aligned}
$$

The value of $K$ from expression (a) may be calculated as

$$
\begin{aligned}
-\log K & =\frac{-\Delta G^{\circ}}{(2.303)(1.99)(298)} \\
& =\frac{(20,000)}{1365.75}=14.7
\end{aligned}
$$

Taking antilogs,

$$
\log K=0.7+14.0
$$

$$
K=5 \times 10^{14}
$$

SOLVED PROBLEM 2. The standard free energy change for the reaction

$$
\mathrm{N}_{2}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{NO}(\mathrm{~g})
$$

is +173.1 kJ . Calculate $K_{p}$ for the reaction at $25^{\circ} \mathrm{C}$.
SOLUTION
Here, we will use the expression

$$
\begin{aligned}
\Delta G^{\circ} & =-2.303 R T \log K_{p} \\
\log K_{p} & =-\frac{\Delta G^{\circ}}{2.303 R T}
\end{aligned}
$$

or
Substituting the values

$$
\log K_{p}=\frac{1.73 \times 10^{5}}{(2.303)(8.314)(298)}
$$

Taking antilogs

$$
\begin{aligned}
K_{p} & =10^{0.66} \times 10^{-31} \\
& =4.6 \times \mathbf{1 0}^{-31}
\end{aligned}
$$

SOLVED PROBLEM 3. The equilibrium constant, $K_{p}$ for the reaction

$$
\mathrm{C}_{2} \mathrm{H}_{4}(\mathrm{~g})+\mathrm{H}_{2}(\mathrm{~g}) \rightleftharpoons \mathrm{C}_{2} \mathrm{H}_{6}(g)
$$

is $5.04 \times 10^{17} \mathrm{~atm}^{-1}$ at $25^{\circ} \mathrm{C}$. Calculate $\Delta G^{\circ}$.
SOLUTION

$$
\begin{equation*}
\Delta G^{\circ}=-2.303 R T \log K_{p} \tag{a}
\end{equation*}
$$

Here, $\quad R=8.314 ; T=25+273=298 \mathrm{~K} ; K_{p}=5.04 \times 10^{17} \mathrm{~atm}^{-1}$
Substituting the values in the expression (a)

$$
\begin{aligned}
\Delta G^{\circ} & =-2.303(8.314)(298) \log \left(5.04 \times 10^{17}\right) \\
& =-5706 \times \log \left(5.04 \times 10^{17}\right) \\
& =-5706 \times(17.702) \\
& =-1.010 \times 10^{5} \mathrm{~J} \\
\Delta G^{\circ} & =-101 \mathbf{~ k J}
\end{aligned}
$$

Thus
Temperature Dependence of Equilibrium Constant (van't Hoff's Equation)
There is appreciable change in the value of equilibrium constant with change in temperature. It can be determined thermodynamically using the relation

$$
\begin{equation*}
\Delta G^{\circ}=-R T \ln \mathrm{~K}_{p} \tag{i}
\end{equation*}
$$

where $\Delta G^{\circ}$ is the change in standard free energy of the reaction.
Differentiating equation (i) w.r.t. at constant pressure $P$, we get

$$
\left(\frac{\delta\left(\Delta G^{\circ}\right)}{\delta T}\right)_{p}=-R \ln K_{p}-R T\left(\frac{\delta \ln K_{p}}{\delta T}\right)_{p}
$$

Multiplying both sides by $T$, we get

$$
T\left(\frac{\delta\left(\Delta G^{\circ}\right)}{\delta T}\right)_{p}=-R T \ln K_{p}-R T^{2}\left(\frac{\delta \ln K_{p}}{\delta T}\right)_{p}
$$

From equation (i) we get

$$
\begin{equation*}
T\left(\frac{\delta\left(\Delta G^{\circ}\right)}{\delta T}\right)_{p}=\Delta G^{\circ}-R T^{2}\left(\frac{\delta\left(\ln K_{p}\right)}{\delta T}\right)_{p} \tag{ii}
\end{equation*}
$$

We know that Gibb’s Helmholtz equation for a reaction in the standard state can be written as

$$
\Delta G^{\circ}=\Delta H^{\circ}+T\left(\frac{\delta\left(\Delta G^{\circ}\right)}{\delta T}\right)_{p}
$$

or

$$
\begin{equation*}
T\left(\frac{\delta(\Delta G)}{\delta T}\right)_{p}=\Delta G^{\circ}-\Delta H^{\circ} \tag{iii}
\end{equation*}
$$

Comparing (ii) and (iii) we get

$$
\Delta G^{\circ}=R T^{2}\left(\frac{\delta\left(\ln K_{p}\right)}{\delta T}\right)_{p}
$$

or

$$
\begin{equation*}
\frac{\Delta H^{\circ}}{R T^{2}}=\frac{\delta\left(\ln K_{p}\right)}{\delta T} \tag{iv}
\end{equation*}
$$

This equation is known as van't Hoff equation, where $\Delta H^{\circ}$ is the enthalpy change of the reaction at constant pressure when all reactants and products are in their standard state. It has been found that the enthalpy change does not vary much with change in partial pressures of the reactants or products.

Therefore, $\Delta H^{\circ}$ may be replaced by $\Delta H$. The equation (iv) becomes

$$
\begin{equation*}
\frac{\Delta H}{R T^{2}}=\frac{d\left(\ln K_{p}\right)}{d T} \tag{v}
\end{equation*}
$$

Integrating equation $(v)$ we get
or

$$
\begin{align*}
\ln K_{p} & =-\frac{\Delta H}{R T}+C \\
\log K_{p} & =-\frac{\Delta H}{2.303 R T}+C \tag{vi}
\end{align*}
$$

where $C$ is a constant of integration. When a graph of $\log K_{p}$ against $1 / T$ is plotted we get straight line having slope equal to $-\frac{\Delta H}{2.303 R}$ (Fig 17.9).


Figure 17.9
Graph between $\log K p$ and IIT.
From the graph it is clear that
(a) For exothermic reaction $\Delta H$ is negative and $K_{p}$ decreases with increase in temperature
(b) For endothermic reaction $\Delta H$ is positive and $K_{p}$ increases with increase in temperature.

Integrating equation $(v)$ within the limits $K_{p 2}$ at temperature $T_{2}$ and $K_{p 1}$ at temperature $T_{1}$
or

$$
\int_{K_{p 1}}^{K_{p 2}} d \ln K_{p}=\int_{T_{1}}^{T_{2}} \frac{\Delta H}{R T^{2}} d T
$$

$$
\ln \frac{K_{p 2}}{K_{p 1}}=-\frac{\Delta H}{R}\left[\frac{1}{T_{2}}-\frac{1}{T_{1}}\right]
$$

$$
=\frac{\Delta H}{R}\left[\frac{1}{T_{1}}-\frac{1}{T_{2}}\right]
$$

$$
\text { In } \frac{K_{p 2}}{K_{p 1}}=\frac{\Delta H}{R}\left[\frac{T_{2}-T_{1}}{T_{1} T_{2}}\right]
$$

or

$$
\log =\frac{K_{p 2}}{K_{p 1}}=\frac{\Delta H}{2.303 R}\left[\frac{T_{2}-T_{1}}{T_{1} T_{2}}\right]
$$

From this equation the heat of reaction can be determined if the values of equilibrium constant $K_{p 2}$ and $K_{p 1}$ at temperature $T_{2}$ and $T_{1}$ are known and vice-versa.

## van't Hoff Equation in Terms of $\boldsymbol{K}$

We know that equilibrium constant in terms of partial pressure $\left(K_{p}\right)$ and in terms of concentration $\left(K_{c}\right)$ are related to each other by the relation

$$
K_{p}=K_{c}(\mathrm{RT})^{\Delta n}
$$

Taking logarithms we get

$$
\ln K_{p}=\ln K_{c}+\Delta n \ln R T
$$

Differentiating w.r.t. temperature, we get
or

$$
\begin{aligned}
& \frac{d\left(\ln K_{p}\right)}{d T}=\frac{d\left(\ln K_{c}\right)}{d T}+\frac{\Delta n}{T} \\
& \frac{d\left(\ln K_{c}\right)}{d T}=\frac{d\left(\ln K_{P}\right)}{d T}-\frac{\Delta n}{T}
\end{aligned}
$$

From equation ( $v$ ) we have

$$
\begin{aligned}
\frac{d\left(\ln K_{c}\right)}{d T} & =\frac{\Delta H}{R T^{2}}-\frac{\Delta n}{T} \\
& =\frac{\Delta H}{R T^{2}}-\frac{\Delta n R T}{T R T}
\end{aligned}
$$

or

$$
\frac{d\left(\ln K_{c}\right)}{d T}=\frac{\Delta H-\Delta n R T}{R T^{2}}
$$

But we know

$$
\begin{array}{rlrl}
\Delta H & =\Delta E+\Delta n R T \\
\therefore & \frac{d\left(\ln K_{c}\right)}{d T} & =\frac{\Delta E}{R T^{2}}
\end{array}
$$

where $\Delta E$ is the heat of the reaction at constant volume.
SOLVED PROBLEM 1. The partial pressure of $\mathrm{CO}_{2}$ in the reaction

$$
\mathrm{CaCO}_{3}(\mathrm{~s}) \rightleftharpoons \mathrm{CaO}(\mathrm{~s})+\mathrm{CO}_{2}(\mathrm{~g})
$$

is 0.773 mm at $500^{\circ} \mathrm{C}$. Calculate $K_{p}$ at $600^{\circ} \mathrm{C}$ for the above reaction. $\Delta H$ of the reaction is 43.2 kcal per mole and does not change in the given range of temperatures.

SOLUTION

Given

$$
\begin{gathered}
\mathrm{CaCO}_{3}(\mathrm{~s}) \rightleftharpoons \mathrm{CaO}(\mathrm{~s})+\mathrm{CO}_{2}(\mathrm{~g}) \\
K_{\mathrm{p}}=P_{\mathrm{CO}_{2}}
\end{gathered}
$$

$$
K_{p 1}=0.773 \mathrm{~mm} \text { at } 500^{\circ} \mathrm{C}
$$

$$
\Delta H=43.2 \mathrm{kcal} \mathrm{~mol}^{-1}
$$

$$
=43200 \mathrm{cal} \mathrm{~mol}^{-1}
$$

using the relation

$$
T_{2}=873 \mathrm{~K} ; K_{p 2}=?
$$

$$
\log \frac{K_{p 2}}{K_{p 1}}=\frac{\Delta H}{2.303 R}\left[\frac{T_{2}-T_{1}}{T_{1} T_{2}}\right]
$$

Substituting the values we get

$$
\begin{aligned}
\log \frac{K_{p 2}}{K_{p 1}} & =\frac{43200}{2.303 \times 1.987}\left[\frac{873-773}{873 \times 773}\right] \\
K_{p 2} & =12.06 \mathrm{~mm}
\end{aligned}
$$

$\therefore \quad$ Equilibrium constant for the given reaction at $600^{\circ} \mathrm{C}$ is $\mathbf{1 2 . 0 6 ~ \mathbf { m m }}$
SOLVED PROBLEM 2. The value of $K_{\mathrm{p}}$ at 298 K for the reaction

$$
\frac{1}{2} \mathrm{~N}_{2}+\frac{3}{2} \mathrm{H}_{2} \rightleftharpoons \mathrm{NH}_{3}
$$

is found to be 826.0, partial pressures being measured in atmospheric units. Calculate $\Delta G^{\circ}$ at 298 K .
SOLUTION. We know

$$
\Delta G^{\circ}=-2.303 R T \log K_{p}
$$

Here

$$
\begin{aligned}
R & =1.987 \mathrm{cal} \mathrm{~mol}^{-1} \mathrm{~K}^{-1} ; T=298 \mathrm{~K} \\
K_{p} & =826 ; \Delta G^{\circ}=?
\end{aligned}
$$

Substituting the values we get

$$
\begin{aligned}
\Delta G^{\circ} & =-2.303 \times 1.987 \times 298 \times \log 826 \\
& =3977.78 \text { cal }
\end{aligned}
$$

SOLVED PROBLEM 3. The equilibrium constant $K_{\mathrm{p}}$ for the reaction

$$
2 \mathrm{NH}_{3}(\mathrm{~g}) \rightleftharpoons 3 \mathrm{H}_{2}(\mathrm{~g})+\mathrm{N}_{2}(\mathrm{~g})
$$

is $1.22 \times 10^{-3}$ at 298 K and 2.16 at 498 K . Calculate $\Delta H^{\circ}$ for the reaction.
SOLUTION. We know

$$
\log \frac{K_{p 2}}{K_{p 1}}=\frac{\Delta H^{\circ}}{2.303 R}\left[\frac{T_{2}-T_{1}}{T_{1} T_{2}}\right]
$$

Here

$$
\begin{aligned}
K_{p 2} & =2.16 ; K_{p 1}=1.22 \times 10^{-3} \\
T_{2} & =498 \mathrm{~K} ; T_{1}=298 \mathrm{~K} \\
R & =1.987 \mathrm{cal} \mathrm{~K}^{-1} \mathrm{~mol}^{-1}
\end{aligned}
$$

Substituting the values we get
or

$$
\begin{aligned}
& \log \frac{2.16}{1.22 \times 10^{-3}}=\frac{\Delta H^{\circ}}{2.303 \times 1.987}\left[\frac{498-298}{498 \times 298}\right] \\
& \log \frac{2.16}{1.22 \times 10^{-3}}=\frac{\Delta H^{\circ}}{2.303 \times 1.987} \frac{200}{498 \times 298}
\end{aligned}
$$

$$
\begin{aligned}
\Delta H^{\circ} & =11028.9 \text { cals } \\
& =\mathbf{1 1 . 0 2 8 9} \mathbf{k c a l s}
\end{aligned}
$$

## LIOUID SYSTEMS

The chemical equilibrium in which all the reactants and products are in the liquid phase, are referred to as the liquid equilibria. Like the gas- phase equilibria, the liquid equilibria are also called homogeneous equilibria. For example, alcohols and acids react to form esters and water.
Reaction between Acetic acid and Ethyl alcohol to form Ethyl acetate

$$
\mathrm{CH}_{3} \mathrm{COOH}(l)+\mathrm{C}_{2} \mathrm{H}_{2} \mathrm{OH}(l) \rightleftharpoons \mathrm{CH}_{3} \mathrm{COOC}_{2} \mathrm{H}_{5}(l)+\mathrm{H}_{2} \mathrm{O}(l)
$$

Let us start with $a$ moles of acetic acid and $b$ moles of alcohol. If $x$ moles of acetic acid react with
$x$ moles of ethyl alcohol, $x$ moles of ester and $x$ moles of water are produced when the equilibrium is established. Now the moles present at equilibrium are:

$$
\begin{aligned}
\mathrm{CH}_{3} \mathrm{COOH} & =(a-x) \text { moles } \\
\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH} & =(b-x) \text { moles } \\
\mathrm{CH}_{3} \mathrm{COOC}_{2} \mathrm{H}_{5} & =x \text { moles } \\
\mathrm{H}_{2} \mathrm{O} & =x \text { moles }
\end{aligned}
$$

If $V$ litre be the total volume of the equilibrium mixture, the concentrations of the various species are:

$$
\begin{aligned}
{\left[\mathrm{CH}_{3} \mathrm{COOH}\right] } & =\frac{a-x}{V} \\
{\left[\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}\right] } & =\frac{b-x}{V} \\
{\left[\mathrm{CH}_{3} \mathrm{COOC}_{2} \mathrm{H}_{5}\right] } & =\frac{x}{V} \\
{\left[\mathrm{H}_{2} \mathrm{O}\right] } & =\frac{x}{V}
\end{aligned}
$$

The equilibrium constant expression may be written as

$$
K=\frac{\frac{x}{V} \times \frac{x}{V}}{\frac{a-x}{V} \times \frac{b-x}{V}} \quad \text { or } \frac{x^{2}}{(a-x)(b-x)}
$$

It may be noted that the volume terms $V$ in the numerator and denominator cancel out. In liquid systems when there is a change in the number of moles as a result of the reaction, it is necessary to consider the volume $V$ while calculating the equilibrium constant $K$.

SOLVED PROBLEM 1. At $25^{\circ} \mathrm{C}$ one mole of acetic acid was allowed to react with one mole of ethyl alcohol until equilibrium was established. The equilibrium mixture was found to contain 0.333 mole of unused acid. Calculate the equilibrium constant of the reaction at the same temperature.

SOLUTION
The equation for the reaction is

$$
\mathrm{CH}_{3} \mathrm{COOH}(\mathrm{l})+\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}(\mathrm{l}) \rightleftharpoons \mathrm{CH}_{3} \mathrm{COOC}_{2} \mathrm{H}_{5}(\mathrm{l})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l})
$$

The moles of unused acid $=0.333$
$\therefore$ moles reacted at equilibrium $=1-0.333=0.666$
One mole of acid reacts with one mole of alcohol to form one mole of ester and one mole of water. Therefore, moles of the various species present at equilibrium are:

$$
\begin{aligned}
\mathrm{CH}_{3} \mathrm{COOH} & =0.333 & \mathrm{CH}_{3} \mathrm{COOC}_{2} \mathrm{H}_{5} & =0.666 \\
\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH} & =0.333 & \mathrm{H}_{2} \mathrm{O} & =0.666
\end{aligned}
$$

Since volume term $V$ cancels out, moles may be taken instead of concentrations and the equilibrium constant expression may be written as

$$
\begin{aligned}
K & =\frac{\left[\mathrm{CH}_{3} \mathrm{COOC}_{2} \mathrm{H}_{5}\right]\left[\mathrm{H}_{2} \mathrm{O}\right]}{\left[\mathrm{CH}_{3} \mathrm{COOH}\right]\left[\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}\right]} \\
& =\frac{0.666 \times 0.666}{0.333 \times 0.333}=4
\end{aligned}
$$

Thus $K$ for the reaction between acetic acid and ethyl alcohol at $25^{\circ} \mathrm{C}$ is 4 .

SOLVED PROBLEM 2. 2 moles of acetic acid and 3 moles of ethyl alcohol are allowed to come to equilibrium at 298 K . If the equilibrium constant of the reaction at this temperature is 4 , what is the equilibrium concentration of ethyl acetate?

## SOLUTION

Let $x$ mole of acetic acid react with $x$ mole of ethyl alcohol to form $x$ moles of ethyl acetate and $x$ mole of water at equilibrium. Thus moles at equilibrium are:


Since the volume terms cancel out in the equilibrium constant expression, we have
or

$$
K=\frac{\left[\mathrm{CH}_{3} \mathrm{COOC}_{2} \mathrm{H}_{5}\right]\left[\mathrm{H}_{2} \mathrm{O}\right]}{\left[\mathrm{CH}_{3} \mathrm{COOH}\right]\left[\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}\right]}=\frac{x \times x}{(2-x)(3-x)}=4
$$

$$
\frac{x^{2}}{(2-x)(3-x)}=4
$$

Rearranging gives

$$
3 x^{2}-20 x+24=0
$$

Solving this quadratic equation, we get

$$
x=1.57 \text { or } 5.09
$$

Both roots are positive of which only 1.57 is acceptable. Since 2 mole of acetic acid can yield only 2 moles of the ester, the value 5.09 is rejected. The equilibrium conc. of ethyl acetate is 1.57 mole.

## HETEROGENEOUS EOUILIBRIA

So far we have discussed chemical equilibria in which all reactants and products are either gases or liquids. Such equilibria in which the reactants and products are not all in the same phase, are called heterogeneous equilibria. The decomposition of calcium carbonate upon heating to form calcium oxide and carbon dioxide is an example of heterogeneous equilibrium. If the reaction is carried in a closed vessel, the following equilibrium is established.

$$
\mathrm{CaCO}_{3}(s) \rightleftharpoons \mathrm{CaO}(s)+\mathrm{CO}_{2}(g)
$$



Figure 17.10
When solid $\mathrm{CaCO}_{3}$ is heated in a closed vessel at $900^{\circ} \mathrm{C}$, equilibrium is established when the pressure of $\mathrm{CO}_{2}$ reaches 1.04 atm .

## Equilibrium Constant Expression

Straight forward application of Equilibrium law to the decomposition reaction of calcium carbonate leads to the equilibrium constant expression.

$$
K=\frac{\left[\mathrm{CO}_{2}\right][\mathrm{CaO}]}{\left[\mathrm{CaCO}_{3}\right]}
$$

But $\mathrm{CaCO}_{3}$ and CaO are pure solids. The concentration (moles per unit volume) of a pure solid (or liquid) is fixed and cannot vary. Thus the concentrations of pure solids or liquids are not included in the equilibrium constant expression.

Ignoring the concentrations of $\mathrm{CaCO}_{3}$ and CaO , the equilibrium constant expression for the decomposition of $\mathrm{CaCO}_{3}$ may be written as

$$
K_{c}=\left[\mathrm{CO}_{2}\right]
$$

In terms of partial pressures

$$
K_{p}=p_{c o_{2}}
$$

Similarly, the equilibrium constant expression for the decomposition of liquid water

$$
2 \mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightleftharpoons 2 \mathrm{H}_{2}(g)+\mathrm{O}_{2}(g)
$$

would be

$$
K=\frac{\left[\mathrm{H}_{2}\right]^{2}\left[\mathrm{O}_{2}\right]}{\left[\mathrm{H}_{2} \mathrm{O}\right]}
$$

Ignoring the concentration of liquid water, we have

$$
\begin{aligned}
& K_{c}=\left[\mathrm{H}_{2}\right]^{2}\left[\mathrm{O}_{2}\right] \\
& K_{p}=\left(p_{\mathrm{H}_{2}}\right)^{2}\left(p_{\mathrm{O}_{2}}\right)
\end{aligned}
$$

SOLVED PROBLEM 1. Write expressions for the equilibrium constants $K_{c}$ and $K_{p}$ for the equilibria:
(b)

$$
\begin{equation*}
\mathrm{NH}_{4} \mathrm{Cl}(\mathrm{~s}) \rightleftharpoons \mathrm{NH}_{3}(g)+\mathrm{HCl}(g) \tag{a}
\end{equation*}
$$

$$
\mathrm{PCl}_{5}(\mathrm{~s}) \rightleftharpoons \mathrm{PCl}_{3}(\mathrm{l})+\mathrm{Cl}_{2}(\mathrm{~g})
$$

(c)

$$
3 \mathrm{Fe}(\mathrm{~s})+4 \mathrm{H}_{2} \mathrm{O}(\mathrm{~g}) \rightleftharpoons \mathrm{Fe}_{3} \mathrm{O}_{4}(\mathrm{~s})+4 \mathrm{H}_{2}(\mathrm{~g})
$$

SOLUTION
Ignoring the solid and liquid species, the equilibrium constant expressions may be written as:

$$
\begin{align*}
& K_{c}=\left[\mathrm{NH}_{3}\right][\mathrm{HCl}]  \tag{a}\\
& K_{p}=\left(p_{\mathrm{NH}_{3}}\right)\left(p_{\mathrm{HCl}}\right)
\end{align*}
$$

(b)

$$
K_{c}=\left[\mathrm{Cl}_{2}\right]
$$

$$
K_{p}=p_{\mathrm{Cl}_{2}}
$$

(c)

$$
\begin{aligned}
& K_{c}=\frac{\left[\mathrm{H}_{2}\right]^{4}}{\left[\mathrm{H}_{2} \mathrm{O}\right]^{4}} \\
& K_{p}=\frac{\left(p_{\mathrm{H}_{2}}\right)^{4}}{\left(p_{\mathrm{H}_{2} \mathrm{O}}\right)^{4}}
\end{aligned}
$$

SOLVED PROBLEM 2. Carbon dioxide upon heating with carbon at high temperature is reduced to carbon monoxide:

$$
\mathrm{CO}_{2}(\mathrm{~g})+\mathrm{C}(\mathrm{~s}) \rightleftharpoons 2 \mathrm{CO}(\mathrm{~g})
$$

$K_{p}$ for the reaction is 1.90 atm .
In a particular experiment the total pressure at equilibrium was found to be 2.00 atm . What were the partial pressures of CO and $\mathrm{CO}_{2}$ ?

SOLUTION
Ignoring solid carbon, the equilibrium constant expression can be written as

$$
K_{p}=\frac{\left(p_{\mathrm{CO}}\right)^{2}}{p_{\mathrm{CO}_{2}}}
$$

If the partial pressure of CO is $x \mathrm{~atm}$, partial pressure of $\mathrm{CO}_{2}$ is $(2.00-x)$
Substituting the values,

$$
\begin{aligned}
& \qquad K_{p}=\frac{x^{2}}{2.00-x}=1.90 \mathrm{~atm} \\
& \therefore \quad x^{2}+1.90 x-3.80=0 \\
& \text { Solving the quadratic equation, } x=1.22 \\
& \text { Hence } \quad \begin{array}{ll}
p_{\mathrm{CO}} & =x \mathrm{~atm}=1.22 \mathrm{~atm} \\
& p_{\mathrm{CO}_{2}}= \\
& =(2.00-x)=\mathbf{0 . 7 8} \mathbf{~ a t m}
\end{array}
\end{aligned}
$$

## LE CHATELIER'S PRINCIPLE

In 1884, the French Chemist Henry Le Chatelier proposed a general principle which applies to all systems in equilibrium. This important principle called the Le Chatelier's principle may be stated as : when a stress is applied on a system in equilibrium, the system tends to adjust itself so as to reduce the stress.

There are three ways in which the stress can be caused on a chemical equilibrium:
(1) Changing the concentration of a reactant or product.
(2) Changing the pressure (or volume) of the system.
(3) Changing the temperature.

Thus when applied to a chemical reaction in equilibrium, Le Chatelier's principle can be stated as: if a change in concentration, pressure or temperature is caused to a chemical reaction in equilibrium, the equilibrium will shift to the right or the left so as to minimise the change.

Now we proceed to illustrate the above statement by taking examples of each type of stress.

## EFFECT OF A CHANGE IN CONCENTRATION

We can restate Le Chatelier's principle for the special case of concentration changes: when concentration of any of the reactants or products is changed, the equilibrium shifts in a direction so as to reduce the change in concentration that was made.
Addition of an inert gas
Let us add an inert gas to an equilibrium mixture while the volume of the reaction vessel remains the same. The addition of the inert gas increases the total pressure but the partial pressures of the reactants and products are not changed. Thus the addition of an inert gas has no effect on the position of the equilibrium.

(a) At equilibrium

(b) Under stress

(c) New equilibrium


Figure 17.11
Illustratation of Le Chatelier's principle. (a) System at equilibrium with $10 \mathrm{H}_{2}, 5 \mathrm{~N}_{2}$, and $3 \mathrm{NH}_{3}$, for a total of 18 molecules. (b) The same molecules are forced into a smaller volume, creating a stress on the system. (c) Six $\mathrm{H}_{2}$ and $2 \mathrm{~N}_{2}$ have been converted to $4 \mathrm{NH}_{3}$. A new equilibrium has been established with $4 \mathrm{H}_{2}, 3 \mathrm{~N}_{2}$, and $7 \mathrm{NH}_{3}$, a total of 14 molecules. The stress is partially relieved by the reduction in the total number of molecules.

## Effect of change of concentration on Ammonia Synthesis reaction

Let us illustrate the effect of change of concentration on a system at equilibrium by taking example of the ammonia synthesis reaction:

$$
\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \rightleftharpoons 2 \mathrm{NH}_{3}(g)
$$

When $N_{2}$ (or $\mathrm{H}_{2}$ ) is added to the equilibrium already in existence (equilibrium I), the equilibrium will shift to the right so as to reduce the concentration of $N_{2}$ (Le Chatelier's principle). The concentration of $\mathrm{NH}_{3}$ at the equilibrium II is more than at equilibrium I. The results in a particular case after the addition of one mole/litre are given below.

$$
\begin{array}{ll}
\text { Equilibrium I } & \text { Equilibrium II } \\
{\left[\mathrm{N}_{2}\right]=0.399 \mathrm{M}} & \\
{\left[\mathrm{H}_{2}\right]=1.197 \mathrm{M}} & \frac{1 \text { mole/ } \mathrm{L}}{\text { of } \mathrm{N}_{2} \text { added }} \\
{\left[\mathrm{NH}_{3}\right]=0.202 \mathrm{M}} & \\
{\left[\mathrm{H}_{2}\right]=1.348 \mathrm{M}} \\
{\left[\mathrm{NH}_{3}\right]=0.304 \mathrm{M}} \\
\hline
\end{array}
$$

Obviously, the addition of $\mathrm{N}_{2}$ (a reactant) increases the concentration of $\mathrm{NH}_{3}$, while the concentration of $\mathrm{H}_{2}$ decreases. Thus to have a better yield of $\mathrm{NH}_{3}$, one of the reactants should be added in excess.

A change in the concentration of a reactant or product can be effected by the addition or removal of that species. Let us consider a general reaction

$$
\mathrm{A}+\mathrm{B} \rightleftharpoons \mathrm{C}
$$

When a reactant, say, A is added at equilibrium, its concentration is increased. The forward reaction alone occurs momentarily. According to Le Chatelier's principle, a new equilibrium will be
established so as to reduce the concentration of A. Thus the addition of A causes the equilibrium to shift to right. This increases the concentration (yield) of the product C.


Following the same line of argument, a decrease in the concentration of A by its removal from the equilibrium mixture, will be undone by shift to the equilibrium position to the left. This reduces the concentration (yield) of the product C .

## Effect of a change in pressure

To predict the effect of a change of pressure, Le Chatelier's principle may be stated as : when pressure is increased on a gaseous equilibrium reaction, the equilibrium will shift in a direction which tends to decrease the pressure.

The pressure of a gaseous reaction at equilibrium is determined by the total number of molecules it contains. If the forward reaction proceeds by the reduction of molecules, it will be accompanied by a decrease of pressure of the system and vice versa.

Let us consider a reaction,

$$
\mathrm{A}+\mathrm{B} \rightleftharpoons \mathrm{C}
$$

The combination of $A$ and $B$ produces a decrease of number of molecules while the decomposition of C into A and B results in the increase of molecules. Therefore, by the increase of pressure on the equilibrium it will shift to right and give more C. A decrease in pressure will cause the opposite effect. The equilibrium will shift to the left when C will decompose to form more of A and B .


The reactions in which the number of product molecules is equal to the number of reactant molecules,

$$
\text { e.g., } \quad \mathrm{H}_{2}(g)+\mathrm{I}_{2}(g) \rightleftharpoons 2 \mathrm{HI}
$$

are unaffected by pressure changes. In such a case the system is unable to undo the increase or decrease of pressure.

In light of the above discussion, we can state a general rule to predict the effect of pressure changes on chemical equilibria.

The increase of pressure on a chemical equilibrium shifts it in that direction in which the number of molecules decreases and vice-versa. This rule is illustrated by the examples listed in Table 17.1.

## TABLE 17.1. EFFECT OF PRESSURE ON VARIOUS GASEOUS EQUILIBRIA

System Pressure increased Pressure decreased

| (1) $\mathrm{N}_{2} \mathrm{O}_{4} \rightleftharpoons 2 \mathrm{NO}_{2}$ | - | $\longrightarrow$ |
| :---: | :---: | :---: |
| (2) $\mathrm{PCl}_{5} \rightleftharpoons \mathrm{PCl}_{3}+\mathrm{Cl}_{2}$ | $\longleftarrow$ | $\xrightarrow{ }$ |
| (3) $2 \mathrm{SO}_{2}+\mathrm{O}_{2} \rightleftharpoons 2 \mathrm{SO}_{3}$ | $\longrightarrow$ | $\longleftarrow$ |
| (4) $\mathrm{N}_{2}+3 \mathrm{H}_{2} \rightleftharpoons 2 \mathrm{NH}_{3}$ | $\rightarrow$ | $\longleftarrow$ |
| (5) $\mathrm{H}_{2}+\mathrm{I}_{2} \rightleftharpoons 2 \mathrm{HI}$ | No effect | No effe |
| (6) $\mathrm{N}_{2}+\mathrm{O}_{2} \rightleftharpoons 2 \mathrm{NO}$ | No effect | No effe |

## EFFECT OF CHANGE OF TEMPERATURE

Chemical reactions consist of two opposing reactions. If the forward reaction proceeds by the evolution of heat (exothermic), the reverse reaction occurs by the absorption of heat (endothermic). Both these reactions take place at the same time and equilibrium exists between the two. If temperature of a reaction is raised, heat is added to the system. The equilibrium shifts in a direction in which heat is absorbed in an attempt to lower the temperature. Thus the effect of temperature on an equilibrium reaction can be easily predicted by the following version of the Le Chatelier's principle.

When temperature of a reaction is increased, the equilibrium shifts in a direction in which heat is absorbed.

Let us consider an exothermic reaction

$$
\mathrm{A}+\mathrm{B} \rightleftharpoons \mathrm{C}+\text { heat }
$$

When the temperature of the system is increased, heat is supplied to it from outside. According to Le Chatelier's principle, the equilibrium will shift to the left which involves the absorption of heat. This would result in the increase of the concentration of the reactants A and B.


In an endothermic reaction

$$
\mathrm{X}+\mathrm{Y}+\text { heat } \rightleftharpoons \mathrm{Z}
$$

the increase of temperature will shift the equilibrium to the right as it involves the absorption of heat. This increases the concentration of the product Z .

In general, we can say that the increase of temperature favours the reverse change in an exothermic reaction and the forward change in an endothermic reaction.


## Formation of Ammonia from $\mathrm{N}_{2}$ and $\mathrm{H}_{2}$

The synthesis of ammonia from nitrogen and hydrogen is an exothermic reaction.

$$
\mathrm{N}_{2}+3 \mathrm{H}_{2} \rightleftharpoons 2 \mathrm{NH}_{3}+22.2 \mathrm{kcal}
$$

When the temperature of the system is raised, the equilibrium will shift from right-to-left which absorbs heat (Le Chatelier's principle) This results in the lower yield of ammonia. On the other hand, by lowering the temperature of the system, the equilibrium will shift to the right which evolves heat in an attempt to raise the temperature. This would increase the yield of ammonia. But with decreasing temperature, the rate of reaction is slowed down considerably and the equilibrium is reached slowly. Thus in the commercial production of ammonia, it is not feasible to use temperature much lower than $500^{\circ} \mathrm{C}$. At lower temperature, even in the presence of a catalyst, the reaction proceeds too slowly to be practical.

TABLE 17.2. THE DIRECTION OF EQUILIBRIUM SHIFT IN SOME REACTIONS ON INCREASE OF TEMPERATURE

| Reaction | Equilibrium Shift |
| :---: | :---: |
| $4 \mathrm{HCl}+\mathrm{O}_{2} \rightleftharpoons 2 \mathrm{H}_{2} \mathrm{O}+2 \mathrm{Cl}_{2}+284 \mathrm{kcal}$ |  |
| $\mathrm{H}_{2}+\mathrm{Cl}_{2} \rightleftharpoons 2 \mathrm{HCl}+44.2 \mathrm{kcal}$ |  |
| $\mathrm{CH}_{4}+2 \mathrm{O}_{2} \rightleftharpoons \mathrm{CO}_{2}+2 \mathrm{H}_{2} \mathrm{O}+212.8 \mathrm{kcal}$ | $\longleftarrow$ |
| $2 \mathrm{CO}_{2}+135.2 \mathrm{kcal} \rightleftharpoons 2 \mathrm{CO}+\mathrm{O}_{2}$ | $\longleftarrow$ |
| $\mathrm{~N}_{2} \mathrm{O}_{4}+14 \mathrm{kcal} \rightleftharpoons 2 \mathrm{NO}_{2}$ |  |
| $\mathrm{H}_{2}+\mathrm{I}_{2}+12.4 \mathrm{kcal} \rightleftharpoons 2 \mathrm{HI}$ | $\longrightarrow$ |

## CONDITIONS FOR MAXIMUM YIELD IN INDUSTRIAL PROCESSES

With the help of Le Chatelier's principle we can work out the optimum conditions for securing the maximum yield of products in industrial processes.

## Synthesis of Ammonia (Haber Process)

The manufacture of ammonia by Haber process is represented by the equation

$$
\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \rightleftharpoons 2 \mathrm{NH}_{3}(g)+22.0 \mathrm{kcal}
$$

A look at the equation provides the following information:
(a) the reaction is exothermic
(b) the reaction proceeds with a decrease in the number of moles.
(1) Low temperature. By applying Le Chatelier's principle, low temperature will shift the equilibrium to the right. This gives greater yield of ammonia. In actual practice a temperature of about $450^{\circ} \mathrm{C}$ is used when the percentage of ammonia in the equilibrium mixture is 15 .
(2) High pressure. High pressure on the reaction at equilibrium favours the shift of the equilibrium to the right. This is so because the forward reaction proceeds with a decrease in the number of moles. A pressure of about 200 atmospheres is applied in practice.
(3) Catalyst. As already stated, low temperature is necessary for higher yield of ammonia. But at relatively low temperatures, the rate of reaction is slow and the equilibrium is attained in a long time. To increase the rate of reaction and thus quicken the attainment of equilibrium, a catalyst is used. Finely divided iron containing molybdenum is employed in actual practice. Molybdenum acts as a promoter that increases the life and efficiency of the catalyst.
Pure $\mathrm{N}_{2}$ and $\mathrm{H}_{2}$ gases are used in the process. Any impurities in the gases would poison the catalyst and decrease its efficiency.


Figure 17.12
Synthesis of ammonia by Haber process.


Figure 17.13
Effect of temperature and pressure on the equilibrium $\mathrm{N}_{2}+3 \mathrm{H}_{2} \rightleftharpoons 2 \mathrm{NH}_{3}$. Increasing temperature decreases the percentage of $\mathrm{NH}_{3}$ at equilibrium. Increasing pressure increases the percentage of $\mathrm{NH}_{3}$ at equilibrium.

## Manufacture of Sulphuric acid (Contact Process)

The chief reaction used in the process is

$$
2 \mathrm{SO}_{2}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{SO}_{3}(\mathrm{~g})+42 \mathrm{kcal}
$$

Following information is revealed by the above equation:
(a) the reaction is exothermic.
(b) the reaction proceeds with a decrease in number of moles.

On the basis of Le Chatelier's principle, the conditions for the maximum yield can be worked out as below:
(1) Low temperature. Since the forward reaction is exothermic, the equilibrium will shift on the right at low temperature. An optimum temperature between $400-450^{\circ} \mathrm{C}$ is required for the maximum yield of sulphur trioxide.
(2) High pressure. Since the number of moles are decreased in the forward reaction, increase of pressure will shift the equilibrium to the right. Thus for maximum yield of $\mathrm{SO}_{3}, 2$ to 3 atmosphere pressure is used.
(3) Catalyst. At the low temperature used in the reaction, the rate of reaction is slow and the equilibrium is attained slowly. A catalyst is, therefore, used to speed up the establishment of the equilibrium. Vanadium pentoxide, $\mathrm{V}_{2} \mathrm{O}_{5}$, is commonly used and it has replaced the earlier catalyst platinum asbestos which was easily poisoned by the impurities present in the reacting gases. All the same, $\mathrm{SO}_{2}$ and $\mathrm{O}_{2}$ used for the manufacture of sulphuric acid must be pure and dry.

## Manufacture of Nitric acid (Birkeland-Eyde process)

Nitric acid is prepared on a large scale by making use of the reaction

$$
\mathrm{N}_{2}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{NO}(\mathrm{~g})-43.2 \mathrm{kcal}
$$

The equation tells us that:
(a) the reaction proceeds with no change in the number of moles.
(b) the reaction is endothermic and proceeds by absorption of heat.

The favourable conditions for the maximum yield of NO are:
(1) High temperature. Since the forward reaction is endothermic, increase of temperature will favour it (Le Chatelier's principle). Thus a high temperature of the order of $3000^{\circ} \mathrm{C}$ is employed to get high yield of nitric acid.
(2) No effect of pressure. Since the forward reaction involves no change in the number of moles, a change in pressure has no effect on the equilibrium.
(3) High concentration. The formation of nitric oxide is favoured by using high concentrations of the reactants i.e. $\mathrm{N}_{2}$ and $\mathrm{O}_{2}$.

## EXAMINATION QUESTIONS

1. Define or explain the following terms :
(a) Chemical equilibrium
(b) Law of mass action
(c) Equilibrium constant
(d) Heterogeneous equilibria
2. One mole of $\mathrm{PCl}_{5}$ is heated in a closed two-litre vessel. At equilibrium $40 \%$ of the $\mathrm{PCl}_{5}$ is dissociated. Calculate the equilibrium constant of the reaction.
Answer. 0.267
3. (a) Derive the law of mass action for the expression :
$n \mathrm{~A}+m \mathrm{~B} \rightleftharpoons p \mathrm{C}+q \mathrm{D}$
(b) The concentration equilibrium constant, $K_{c}$ for the reaction $\mathrm{N}_{2}+3 \mathrm{H}_{2} \rightleftharpoons 2 \mathrm{NH}_{3}$ at $400^{\circ} \mathrm{C}$ is 0.5 . Find the value of $K_{\mathrm{p}} .\left(R=0.0821\right.$ lit atm $\left.\mathrm{deg}^{-1} \mathrm{~mol}^{-1}\right)$
Answer. (b) 0.000164
4. (a) Why chemical equilibrium is called a dynamic equilibrium?
(b) In what direction the following equilibrium will be shifted if some chlorine gas is introduced into the system at equilibrium?
$\mathrm{COCl}_{2}(\mathrm{~g}) \rightleftharpoons \mathrm{CO}(\mathrm{g})+\mathrm{Cl}_{2}(\mathrm{~g})$
(c) Calculate the ratio of $K_{\mathrm{p}}$ to $K_{\mathrm{c}}$ at $27^{\circ} \mathrm{C}$ for the equilibrium reaction: $\mathrm{C}_{2} \mathrm{H}_{6}(\mathrm{~g}) \rightleftharpoons \mathrm{C}_{2} \mathrm{H}_{4}(\mathrm{~g})+\mathrm{H}_{2}(\mathrm{~g})$
Answer. (c) 24.63
5. For the reaction $\mathrm{CO}_{2}(\mathrm{~g})+\mathrm{H}_{2}(\mathrm{~g}) \rightleftharpoons \mathrm{CO}(\mathrm{g})+\mathrm{H}_{2} \mathrm{O}(\mathrm{g})$
the equilibrium constant at 1000 K is 0.53 .
(a) If a mixture at equilibrium in a $1 \mathrm{dm}^{3}$ vessel contains 0.25 mole of CO and 0.6 mole of $\mathrm{H}_{2}$, how many moles of $\mathrm{H}_{2} \mathrm{O}$ are there in the vessel?
(b) 5 moles of inert gas are added to the equilibrium mixture containing 1 mole of $\mathrm{H}_{2}$ and 1 mole of $\mathrm{CO}_{2}$ in $1 \mathrm{dm}^{3}$ vessel. Predict equilibrium concentration of $\mathrm{CO}_{2}$ and $\mathrm{H}_{2} \mathrm{O}$.
Answer. (a) 0.636 mole; (b) 0.4 mole; 0.4 mole
6. (a) What is standard free energy change? Derive a relationship between standard free energy change and equilibrium constant of a reaction at a given temperature.
(b) The equilibrium constant $K_{\mathrm{p}}$ for the reaction :
$\mathrm{N}_{2}(\mathrm{~g})+3 \mathrm{H}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{NH}_{3}(\mathrm{~g})$
is $1.64 \times 10^{-4}$ at 673 K and $0.144 \times 10^{-4}$ at 773 K . Calculate the mean heat of formation of ammonia from its elements in this temperature range.
Answer. (b) - 52.6174 kJ
7. (a) Derive thermodynamically the law of chemical equilibrium.
(b) For the reaction $\mathrm{N}_{2}(\mathrm{~g})+3 \mathrm{H}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{NH}_{3}(\mathrm{~g})$ $K_{\mathrm{p}}$ is $1.64 \times 10^{-4}$ at 673 K . Calculate
(i) $\Delta G$; (ii) $\Delta G$ when the partial pressure of $\mathrm{N}_{2}, \mathrm{H}_{2}$ and $\mathrm{NH}_{3}$ are $10 \mathrm{~atm}, 30 \mathrm{~atm}$ and 3 atm respectively;
(iii) Is the reaction spontaneous?

Answer.(b) (i) 48.775 kJ; (ii) 57.6979 kJ; (iii) No
8. (a) What is the thermodynamical equilibrium constant? Derive the expression showing the effect of temperature on chemical equilibrium.
(b) The equilibrium constant $K_{\mathrm{p}}$ for a reaction
$\mathrm{A}+\mathrm{B} \rightleftharpoons \mathrm{C}+\mathrm{D}$ is $10^{-12}$ at $327^{\circ} \mathrm{C}$ and $10^{-7}$ at $427^{\circ} \mathrm{C}$. Calculate the enthalpy of the reaction.
( $R=8.314 \mathrm{~J} \mathrm{~K}^{-1} \mathrm{~mol}^{-1}$ )
Answer. (b) 402.08998 kJ
9. (a) Describe homogenous and heterogeneous equilibria.
(b) For the dissociation of water :
$\mathrm{H}_{2} \mathrm{O}(\mathrm{g}) \rightleftharpoons \mathrm{H}_{2}(\mathrm{~g})+1 / 2 \mathrm{O}_{2}(\mathrm{~g})$
at 1773 K , the value of $K_{\mathrm{p}}$ is $1.87 \times 10^{-6} \mathrm{~atm}$. Assuming ideal behaviour of gases, calculate the value of $K_{c}$.
Answer. (b) $1.55 \times 10^{-7}$
10. Calculate $\Delta G^{\circ}$ and $K_{\mathrm{p}}$ for the following reaction at 298 K
$\mathrm{CO}(\mathrm{g})+\mathrm{H}_{2} \mathrm{O}(\mathrm{g}) \rightarrow \mathrm{CO}_{2}(\mathrm{~g})+\mathrm{H}_{2}(\mathrm{~g})$
Given that $\Delta G^{\circ}$ for $\mathrm{CO}(\mathrm{g}), \mathrm{CO}_{2}(\mathrm{~g})$ and $\mathrm{H}_{2} \mathrm{O}(\mathrm{g})$ are $-32.807,-97.26$ and $-54.64 \mathrm{cal} \mathrm{mol}^{-1}$ respectively.
Answer. $-9.813 \mathrm{kcal} ; 1.41 \times 10^{7}$

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11. Derive van't Hoff equation showing the variation of equilibrium constant $K$ with temperature. Also obtain its integrated form.
12. Derive a mathematical relation to calculate the temperature dependence of equilibrium constant of a chemical reaction.
13. Derive van't Hoff reaction isotherm for the reaction :
$a \mathrm{~A}+b \mathrm{~B}+\ldots . . \rightleftharpoons l \mathrm{~L}+m \mathrm{M}+\ldots \ldots .$.
14. Derive the relation between $K_{\mathrm{c}}$ and $K_{\mathrm{p}}$
15. Prove that $\Delta G^{\circ}=-R T \ln K_{\mathrm{p}}$
16. For a reaction $K_{\mathrm{p}}=K_{\mathrm{c}}$ : What do you infer from this?
17. What are the limitations of equation for chemical equilibrium?
(Himachal BSc, 2000)
18. What is the vapour density of $\mathrm{PCl}_{5}$ at $250^{\circ} \mathrm{C}$, if it has dissociated to the extent of $80 \%$ ?

Answer. 57.9
(Bundelkhand BSc, 2000)
19. Write a short note on "Le Chatelier's Principle".
(Purvanchal BSc, 2000)
20. (a) Define equilibrium constant and show that it can have two different values depending on how you express concentration. Derive relationship between these two values.
(b) Equilibrium constant of the reaction $\mathrm{H}_{2}+\mathrm{I}_{2} \rightleftharpoons 2 \mathrm{HI}$ is 64 at a certain temperature. If 12 g of hydrogen and 762 g of iodine be kept in a closed vessel at this temperature to attain equilibrium what weight of HI will be present in the vessel?
Answer. 847.8 g
(Purvanchal BSc, 2000)
21. Differentiate between the rate constant from equilibrium constant.
(Kathmandu BSc, 2001)
22. Deduce the law of mass action thermodynamically.
(Allahabad BSc, 2001)
23. (a) Discuss the law of chemical equilibrium for the synthesis of ammonia.
(b) What is Le Chatelier's principle? Discuss its applications.
(Purvanchal BSc, 2001)
24. The standard free energy change for the reaction :
$\mathrm{N}_{2}(\mathrm{~g})+3 \mathrm{H}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{NH}_{3}(\mathrm{~g})$
is $-33.2 \mathrm{~kJ} \mathrm{~mol}^{-1}$ at 298 K . Calculate the equilibrium constant. (Given $R=8.314 \mathrm{~J} \mathrm{~K}^{-1} \mathrm{~mol}^{-1}$ )
Answer. $6.60 \times 10^{5}$
(Nagpur BSc, 2002)
25. Give the thermodynamical derivation of law of chemical equilibrium for a general reaction :
$a \mathrm{~A}+b \mathrm{~B}+\ldots \ldots \rightleftharpoons l \mathrm{~L}+m \mathrm{M}+\ldots \ldots$.
(Mizoram BSc, 2002)
26. (a) State law of Mass Action. Does equilibrium reaction stop at equilibrium?
(b) Establish a relationship between $K_{\mathrm{p}}$ and $K_{\mathrm{c}}$.
(Punjabi BSc, 2002)
27. The equilibrium constants $K_{\mathrm{p}}$ for a reaction at $427^{\circ} \mathrm{C}$ and $447^{\circ} \mathrm{C}$ are $1 \times 10^{-12}$ and $5 \times 10^{-12}$ respectively. Considering $\Delta H^{\circ}$ to be constant in above temperature range, calculate $\Delta H^{\circ}$ for the reaction.
Answer. $12.78 \times 10^{4}$ J
(Allahabad BSc, 2002)
28. Derive the relationship between $K_{\mathrm{c}}$ and $K_{\mathrm{p}}$. Calculate $K_{\mathrm{c}}$ for the following reaction at 673 K :
$2 \mathrm{H}_{2} \mathrm{O}(\mathrm{g})+2 \mathrm{Cl}_{2}(\mathrm{~g}) \rightleftharpoons 4 \mathrm{HCl}(\mathrm{g})+\mathrm{O}_{2}(\mathrm{~g})$
(Given $K_{\mathrm{p}}=0.035 ; R=8.314 \mathrm{~J} \mathrm{~K}^{-1} \mathrm{~mol}^{-1}$ )
Answer. $6.25 \times 10^{-6}$
(Nagpur BSc, 2002)
29. Given $\Delta G^{\circ}$ for ionisation of acetic acid in aqueous solution is $27.18 \mathrm{~kJ} \mathrm{~mol}^{-1}$. Estimate the ionisation constant of acetic acid at 298 K .
Answer. $1.72 \times 10^{-5}$
(Guru Nanak Dev BSc, 2002)
30. What is the value of $K_{\mathrm{p}}: K_{\mathrm{c}}$ for the equilibrium
$\mathrm{N}_{2}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{NO}(\mathrm{g})$ at $27^{\circ} \mathrm{C}$ ?
Answer. 1
(Vidyasagar BSc, 2002)
31. (a) State and explain the law of mass action. Derive a relationship between $K_{\mathrm{p}}$ and $K_{\mathrm{c}}$ for the reaction:
$2 \mathrm{SO}_{2}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{SO}_{2}(\mathrm{~g})$
(b) Explain how equilibrium constant changes with temperature for exothermic and endothermic reaction.
(Arunachal BSc, 2002)
32. (a) Derive thermodynamical expression for chemical equilibrium.
(b) How are $K_{\mathrm{p}}, K_{\mathrm{c}}$ and $K_{\mathrm{a}}$ related?
(Arunachal BSc, 2002)
33. Consider the reaction :
$\mathrm{PCl}_{5}(\mathrm{~g}) \rightleftharpoons \mathrm{PCl}_{3}(\mathrm{~g})+\mathrm{Cl}_{2}(\mathrm{~g})$
How would the equilibrium be affected by
(i) the addition of $\mathrm{Cl}_{2}$
(ii) decrease in the volume of the container?
(Jamia Millia BSc, 2002)
34. (a) "Equilibrium constant is a measure of free energy change". Explain and establish a relation between them.
(b) Describe an experiment to establish that equilibrium constant of a reaction is constant at constant temperature.
(Kalyani BSc, 2003)
35. (a) Derive van't Hoff equations
(i) $\frac{d}{d t}\left(\log K_{\mathrm{p}}\right)=\frac{\Delta H^{0}}{R T^{2}}$
(ii) $\frac{d}{d t}\left(\log K_{\mathrm{c}}\right)=\frac{\Delta H^{0}}{R T^{2}}$
(b) Write expression for $K_{\mathrm{p}}$ and $K_{\mathrm{c}}$ for the following equilibrium : $\mathrm{N}_{2} \mathrm{O}_{4}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{NO}_{2}(\mathrm{~g})$
(Panjab BSc, 2003)
36. (a) Give van't Hoff's reaction isotherm for the reaction :
$2 \mathrm{~A}+3 \mathrm{~B} \rightleftharpoons 5 \mathrm{C}+4 \mathrm{~B}$
(b) Give the relationship between $K_{\mathrm{p}}$ and $K_{\mathrm{c}}$ for the reaction : $\mathrm{N}_{2}(\mathrm{~g})+3 \mathrm{H}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{NH}_{3}(\mathrm{~g})$
(Nagpur BSc, 2003)
37. (a) The dissociation of $\mathrm{N}_{2} \mathrm{O}_{4}$ is given by the equation :

$$
\mathrm{N}_{2} \mathrm{O}_{4}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{NO}_{2}(\mathrm{~g})
$$

If $\alpha$ is the degree of dissociation of $\mathrm{N}_{2} \mathrm{O}_{4}$ and P is the total pressure of the system, show that

$$
K_{\mathrm{p}}=\frac{4 \alpha^{2} P}{1-\alpha^{2}}
$$

(b) Calculate $K_{\mathrm{c}}$ and $K_{\mathrm{p}}$ for the reaction :
$\mathrm{N}_{2} \mathrm{O}_{4}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{NO}_{2}(\mathrm{~g})$
for which $K_{\mathrm{p}}=0.157 \mathrm{~atm}$ at $27^{\circ} \mathrm{C}$ and 1 atm pressure.
Answer. $6.38 \times 10^{-3} ; 0.157$
(Lucknow BSc, 2003)
38. For the reaction
$\mathrm{N}_{2}(\mathrm{~g})+3 \mathrm{H}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{NH}_{3}(\mathrm{~g})$
$K_{\mathrm{p}}=1.60 \times 10^{-4}$ at $400^{\circ} \mathrm{C}$. Calculate $\Delta G^{\circ}$ for the reaction.
Answer. 48.913 kJ
(Jamia Millia BSc, 2003)
39. The value of $K_{\mathrm{p}}$ for the water gas reaction is
$\mathrm{CO}+\mathrm{H}_{2} \mathrm{O} \rightleftharpoons \mathrm{CO}_{2}+\mathrm{H}_{2}$
is $1.06 \times 10^{5}$ at $25^{\circ} \mathrm{C}$. Calculate the standard state free energy change $\Delta G^{\circ}$ of the reaction at $25^{\circ} \mathrm{C}$. ( $R=8.314 \mathrm{~J} \mathrm{~K}^{-1} \mathrm{~mol}^{-1}$ )
Answer. 28.673 kJ
(Sambalpur BSc, 2003)
40. (a) Derive the following relationship.

$$
\frac{d \ln K_{\mathrm{p}}}{d T}=\frac{\Delta H^{\mathrm{o}}}{R T^{2}}
$$

(b) The equilibrium constant $K_{\mathrm{p}}$ for the reaction
$\mathrm{N}_{2}+3 \mathrm{H}_{2} \rightleftharpoons 2 \mathrm{NH}_{3}$
at $400^{\circ} \mathrm{C}$ is $1.64 \times 10^{-4}$. What will be the equilibrium constant at $500^{\circ} \mathrm{C}$ if the heat of the reaction in this temperature range is 10.18 kJ ?
Answer. $2.07 \times 10^{-4}$
(Delhi BSc, 2003)
41. (a) Deduce the equation of van't Hoff isochore for equilibrium constants $K_{\mathrm{p}_{1}}$ and $K_{\mathrm{p}_{2}}$
(b) The equilibrium constant for $K_{\mathrm{p}}$ for the reaction
$\mathrm{H}_{2}(\mathrm{~g})+\mathrm{S}(\mathrm{g}) \rightleftharpoons \mathrm{H}_{2} \mathrm{~S}(\mathrm{~g})$
is 20.2 atm at $945^{\circ} \mathrm{C}$ and 9.21 atm at $1065^{\circ} \mathrm{C}$. Calculate the heat of reaction.
Answer. 88.67 kJ
(Arunachal BSc (H), 2003)
42. (a) Derive the relation between the energy change and equilibrium constant.
(b) Calculate the free energy change $\left(\Delta G^{\circ}\right)$ associated with chemical reaction for which the equilibrium constant at 298 K is 0.01 . $\left(R=8.314 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}\right)$.
Answer. (b) 11411.68 J
(Kalyani BSc, 2004)
43. Calculate the equilibrium constant of the reaction $\mathrm{A}+\mathrm{B} \rightleftharpoons 2 \mathrm{C}$ from the data given below :

The reaction was started with 2.0 moles litre ${ }^{-1}$ of $A$ and 2.0 moles litre ${ }^{-1}$ of $B$ and the equilibrium concentration of C was found to be 0.32 mole litre ${ }^{-1}$.
Answer. 0.0302
(Burdwan BSc, 2004)
44. (a) Derive the relation between $K_{\mathrm{p}}$ and $K_{\mathrm{c}}$.
(b) On heating in a closed vessel $\mathrm{PCl}_{5}$ dissociates into $\mathrm{PCl}_{3}$ and $\mathrm{Cl}_{2}$. At $200^{\circ} \mathrm{C}$ the vapour density of the gaseous mixture is 75.5. Calculate the degree of dissociation of $\mathrm{PCl}_{5} .(\mathrm{P}=31, \mathrm{Cl}=35.5)$
Answer. (b) 0.3807
(Gulbarga BSc, 2004)
45. The value of $K_{c}$ for the following reaction at 1173 K is 0.28 .

$$
\mathrm{CS}_{2}(\mathrm{~g})+4 \mathrm{H}_{2}(\mathrm{~g}) \rightleftharpoons \mathrm{CH}_{4}(\mathrm{~g})+2 \mathrm{H}_{2} \mathrm{~S}(\mathrm{~g})
$$

Calculate the value of $K_{p}$ at this temperature.
Answer. $3 \times 10^{-5}$
(Nagpur BSc, 2005)
46. Alcohol and acetic acid were mixed in equimolar proportions in aqueous medium at room temperature. At equilibrium 50\% alcohol is converted into ester. Calculate how much ester will be formed if 2 moles of acetic acid and 1 mole of alcohol were mixed.
Answer. 0.67 mole
(Sri Venkateswara BSc, 2005)
47. A sample of $\mathrm{CaCO}_{3}(\mathrm{~s})$ is introduced into a sealed container of volume 0.500 litre and heated to 800 K until equilibrium is reached. The equilibrium constant for the reaction

$$
\mathrm{CaCO}_{3}(\mathrm{~g}) \rightleftharpoons \mathrm{CaO}(\mathrm{~g})+\mathrm{CO}_{2}(\mathrm{~g})
$$

is $3.9 \times 10^{-2}$ atm at this temperature. Calculate the mass of CaO present at equilibrium.
Answer. $2.97 \times 10^{-4} \mathrm{~mol}$ or 0.0166 g
(Delhi BSc, 2005)
48. At $25^{\circ} \mathrm{C}$ and 1 atm pressure the partial pressure in an equilibrium mixture of $\mathrm{N}_{2} \mathrm{O}_{4}$ and $\mathrm{NO}_{2}$ are 0.7 and 0.3 atm respectively. Calculate the partial pressures of these gases when they are in equilibrium at $25^{\circ} \mathrm{C}$ and a total pressure of 5 atm .
Answer. 4.47 atm and 0.53 atm
(Madras BSc, 2006)
49. At $27{ }^{\circ} \mathrm{C}$ and 1 atm pressure $\mathrm{N}_{2} \mathrm{O}_{4}$ is $20 \%$ dissociated in the $\mathrm{NO}_{2}$. Calculate the value of $K_{p}$ under these conditions.
Answer. 0.17 atm
(Bundelkhand BSc, 2006)
50. Calculate the value of $K_{c}$ for the following reaction

$$
\mathrm{N}_{2} \mathrm{O}_{4}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{NO}_{2}(\mathrm{~g})
$$

when $K_{p}$ is 0.113 atm at $25^{\circ} \mathrm{C}$.
Answer. $4.624 \times 10^{-3} \mathrm{~mol} \mathrm{lit}^{-1}$
(Mysore BSc, 2006)

## MULTIPLE CHOICE QUESTIONS

1. A chemical system is at equilibrium
(a) when the rate of the forward reaction becomes zero
(b) when the rates of the forward reaction and the reverse reaction are equal
(c) when all of the reactants have been used up
(d) when the rates of the forward reaction and the reverse reaction are both zero

Answer. (b)
2. Equilibrium reactions are characterised by
(a) going to completion
(b) being non-spontaneous
(c) the presence of both reactants and products in a definite proportion
(d) (a) and (b)

Answer. (c)
3. A dynamic equilibrium
(a) is when the rate of the forward reaction is equal to the rate of the reverse reaction
(b) is a form of static equilibrium
(c) only occurs in chemical equilibrium
(d) involves radioactivity

Answer. (a)
4. Which of the following represent equilibrium constants?
(a) weak acid or weak base dissociation constant
(b) $K_{\mathrm{c}}$ for a reaction
(c) concentration of a strong acid in water
(d) (a) and (b) represent equilibrium constants

Answer. (d)
5. If the equilibrium constant for a reaction is large, what can be said about the reaction?
(a) very little product is formed
(b) very little reactant remains at equilibrium
(c) the reaction goes to completion
(d) large quantities of reactants will remain at equilibrium

Answer. (b)
6. Which of the following will change the equilibrium constant for a reaction mixture?
(a) changing temperature
(b) adding an inert gas
(c) increasing pressure by decreasing volume
(d) all of these

Answer. (a)
7. A reaction is at equilibrium. What happens to the value of the equilibrium constant if an additional quantity of reactant is added to the reaction mixture?
(a) the equilibrium constant is shifted to favour production of more reactant
(b) the equilibrium constant is shifted to favour production of more product
(c) the equilibrium constant is increased
(d) the equilibrium constant stays the same

Answer. (d)
8. What effect does a catalyst have on the equilibrium position of a reaction?
(a) a catalyst favours the formation of products
(b) a catalyst favours the formation of reactants
(c) a catalyst does not change the equilibrium position of a reaction
(d) a catalyst may favour reactants or product formation, depending upon the direction in which the reaction is written
Answer. (c)
9. Which of the following can change the value of the equilibrium constant for a reaction
(a) changing the concentration of the reactants
(b) adding a catalyst
(c) changing the solvent
(d) removing the products as they are formed

Answer. (c)
10. Which of the following changes the value of $K$ ?
(a) adding reactant
(b) adding product
(c) changing temperature
(d) adding a catalyst

Answer. (c)
11. What is the expression for $K_{\text {eq }}$ for the reaction $2 \mathrm{~N}_{2} \mathrm{O}(\mathrm{g})+\mathrm{O}_{2}(\mathrm{~g}) \rightleftharpoons 4 \mathrm{NO}(\mathrm{g})$ ?
(a) $\frac{\left[\mathrm{N}_{2}\right]\left[\mathrm{O}_{2}\right]}{[\mathrm{NO}]}$
(b) $\frac{[\mathrm{NO}]^{4}}{\left[\mathrm{~N}_{2} \mathrm{O}\right]^{2}}$
(c) $\frac{\left[\mathrm{N}_{2} \mathrm{O}\right]^{2}\left[\mathrm{O}_{2}\right]}{[\mathrm{NO}]^{4}}$
(d) $\frac{[\mathrm{NO}]^{4}}{\left[\mathrm{~N}_{2} \mathrm{O}\right]^{2}\left[\mathrm{O}_{2}\right]}$

Answer. (d)
12. In writing equilibrium constant expressions, which of the following quantities can be used to represent the amount of reactants and products?
(a) concentrations
(b) partial pressures
(c) mole fractions
(d) (a) and (b) only

Answer. (d)
13. Which one of the following statements is incorrect?
(a) adding products shifts the equilibrium to the left
(b) adding reactants shifts the equilibrium to the right
(c) exothermic reactions shift the equilibrium to the left with increasing temperature
(d) adding a catalyst shifts the equilibrium to the right

Answer. (d)
14. For which of the following reactions is the value of $K_{\text {eq }}$ dependent on only one substance in the reaction?
(a) $\mathrm{C}(\mathrm{s})+\mathrm{CO}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{CO}(\mathrm{g})$
(b) $\mathrm{H}_{2}(\mathrm{~g})+\mathrm{Cl}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{HCl}(\mathrm{g})$
(c) $\mathrm{CaCO}_{3}(\mathrm{~s}) \rightleftharpoons \mathrm{CaO}(\mathrm{s})+\mathrm{CO}_{2}(\mathrm{~g})$
(d) $\mathrm{N}_{2} \mathrm{O}_{4}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{NO}_{2}(\mathrm{~g})$

Answer. (c)
15. Which one of the following is incorrect?
(a) equilibrium is dynamic, as some molecules are always reacting
(b) the equilibrium constant is just the ratio of forward to reverse rate constants
(c) at equilibrium the concentrations no longer change with time
(d) the equilibrium constant is not affected by temperature changes

Answer. (d)
16. Which of the following reactions goes to completion because a gas is evolved?
(a) $2 \mathrm{H}_{2}+\mathrm{O}_{2} \rightarrow 2 \mathrm{H}_{2} \mathrm{O}$
(b) $\mathrm{N}_{2}+3 \mathrm{H}_{2} \rightarrow 2 \mathrm{NH}_{3}$
(c) $2 \mathrm{CO}+\mathrm{O}_{2} \rightarrow 2 \mathrm{CO}_{2}$
(d) $\mathrm{Zn}+2 \mathrm{HCl} \rightarrow \mathrm{ZnCl}_{2}+\mathrm{H}_{2}$

Answer. (d)
17. A catalyst will increase the rate of a chemical reaction by
(a) shifting the equilibrium to the right
(b) lowering the activation energy
(c) shifting the equilibrium to the left
(d) increasing the activation energy Answer. (b)
18. The yield of $\mathrm{AB}(\mathrm{g})$
$\mathrm{A}(\mathrm{g})+\mathrm{B}(\mathrm{g}) \rightarrow \mathrm{AB}(\mathrm{g})+$ heat
would be increased by
(a) decreasing the pressure
(b) adding additional AB to the reaction mixture
(c) decreasing the temperature
(d) adding a non-reactive liquid to the reaction mixture

Answer. (c)
19. In which of the following reactions is $K_{\mathrm{eq}}$ independent of the pressure?
(a) $\mathrm{CaCO}_{3}(\mathrm{~s}) \rightleftharpoons \mathrm{CaO}(\mathrm{s})+\mathrm{CO}_{2}(\mathrm{~g})$
(b) $2 \mathrm{CO}(\mathrm{g})+\mathrm{O}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{CO}_{2}(\mathrm{~g})$
(c) $\mathrm{N}_{2}(\mathrm{~g})+3 \mathrm{H}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{NH}_{3}(\mathrm{~g})$
(d) none of these

Answer. (d)
20. The equilibrium constant for the reaction
$\mathrm{CO}(\mathrm{g})+\mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathrm{CO}_{2}(\mathrm{~g})$ (not balanced) may be expressed as
(a) $K=\frac{\left[\mathrm{CO}_{2}\right]}{[\mathrm{CO}]\left[\mathrm{O}_{2}\right]}$
(b) $K=\frac{[\mathrm{CO}]\left[\mathrm{O}_{2}\right]}{\left[\mathrm{CO}_{2}\right]}$
(c) $K=[\mathrm{CO}]^{2}\left[\mathrm{O}_{2}\right]\left[\mathrm{CO}_{2}\right]^{2}$
(d) $K=\frac{\left[\mathrm{CO}_{2}\right]^{2}}{[\mathrm{CO}]^{2}\left[\mathrm{O}_{2}\right]}$

Answer. (d)
21. $\mathrm{N}_{2}+3 \mathrm{H}_{2} \rightleftharpoons 2 \mathrm{NH}_{2} \uparrow$ + heat

In this reversible reaction, the equilibrium shifts to the right because of all the following factors except:
(a) adding heat
(b) adding reactant amounts
(c) formation of ammonia gas
(d) increasing pressure on reactants

Answer. (a)
22. Which statement is true for a liquid/gas mixture in equilibrium?
(a) the equilibrium constant is dependent on temperature
(b) the amount of the gas present at equilibrium is independent of pressure
(c) all interchange between the liquid and gas phases has ceased
(d) all of the above

Answer. (a)
23. Consider the following reversible reaction :
$\mathrm{N}_{2}+3 \mathrm{H}_{2} \rightleftharpoons 2 \mathrm{NH}_{3}$
Its equilibrium constant " $K$ " is expressed as :
(a) $\frac{\left[\mathrm{NH}_{3}\right]}{\left[\mathrm{N}_{2}\right]\left[\mathrm{H}_{2}\right]^{3}}$
(b) $\frac{\left[\mathrm{NH}_{3}\right]^{2}}{\left[\mathrm{~N}_{2}\right]^{3}\left[\mathrm{H}_{2}\right]}$
(c) $\frac{\left[\mathrm{NH}_{3}\right]}{\left[\mathrm{N}_{2}\right]\left[\mathrm{H}_{2}\right]}$
(d) $\left[\mathrm{N}_{2}\right]^{2}\left[\mathrm{H}_{2}\right]^{3}$

Answer. (b)
24. Why doesn't catalyst shift the equilibrium position?
(a) it speeds up both the forward and reverse reaction
(b) it is recoverable unchanged at the end of a reaction
(c) it increases the concentration of both the reactants and products equally
(d) it provides a surface site at which the reaction can occur

Answer. (a)
25. $\mathrm{H}_{2}+\mathrm{S} \rightleftharpoons \mathrm{H}_{2} \mathrm{~S}+$ energy

In this reversible reaction, select the factor that will shift the equilibrium to the right.
(a) adding heat
(b) adding $\mathrm{H}_{2} \mathrm{~S}$
(c) blocking hydrogen gas reaction
(d) removing hydrogen sulphide gas

Answer. (a)
26. The result of adding a small crystal of sodium chloride to a saturated solution of NaCl would be
(a) the same crystal would precipitate
(b) a larger amount of NaCl would precipitate
(c) the crystal would dissolve in solution
(d) the same amount of NaCl would precipitate

Answer. (d)
27. Consider the reaction below :
$2 \mathrm{SO}_{3}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{SO}_{2}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g}) \quad \Delta H^{\circ}=+198 \mathrm{~kJ}$
All of the following changes would shift the equilibrium to the left except one. Which one would not cause the equilibrium to shift to the left?
(a) removing some $\mathrm{SO}_{3}$
(b) adding some $\mathrm{SO}_{2}$
(c) decreasing the temperature
(d) adding a catalyst that speeds up the decomposition of $\mathrm{SO}_{3}$

Answer. (d)
28. Consider the reaction below :
$\mathrm{CO}(\mathrm{g})+\mathrm{H}_{2} \mathrm{O}(\mathrm{g}) \rightleftharpoons \mathrm{CO}_{2}(\mathrm{~g})+\mathrm{H}_{2}(\mathrm{~g}) \Delta H^{\circ}=-41 \mathrm{~kJ}$
All of the following changes would shift the equilibrium to the right except one. Which one would not cause the equilibrium to shift to the right?
(a) decreasing the container volume
(b) adding some CO
(c) removing some $\mathrm{CO}_{2}$
(d) decreasing the temperature

Answer. (a)
29. To an equilibrium mixture of $2 \mathrm{SO}_{2}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{SO}_{3}(\mathrm{~g})$, some helium, an inert gas, is added at constant volume. The addition of helium causes the total pressure to double. Which of the following is true?
(a) The concentrations of all three gases are unchanged
(b) $\left[\mathrm{SO}_{3}\right]$ increases
(c) The number of moles of $\mathrm{SO}_{3}$ increases
(d) $\left[\mathrm{SO}_{2}\right]$ increases

Answer. (a)
30. For the endothermic reaction $\mathrm{CaCO}_{3}(\mathrm{~s}) \rightarrow \mathrm{CaO}(\mathrm{s})+\mathrm{CO}_{2}(\mathrm{~g})$, which of the following actions would favour shifting the equilibrium position to form more $\mathrm{CO}_{2}$ gas?
(a) decreasing the system temperature
(b) both decreasing the system temperature and increasing the system pressure
(c) increasing the system pressure
(d) increasing the system temperature

Answer. (d)
31. Consider the following exothermic reaction :
$\mathrm{N}_{2}(\mathrm{~g})+3 \mathrm{H}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{NH}_{3}(\mathrm{~g})$
Which of the following changes would not increase the amount of $\mathrm{NH}_{3}$ produced from given quantities of $\mathrm{N}_{2}$ and $\mathrm{H}_{2}$ ?
(a) decrease in V
(b) increase in P
(c) remove some $\mathrm{NH}_{3}$ and re-establish equilibrium (d) increase in T Answer. (d)
32. The equilibrium expression, $k=\left[\mathrm{Ag}^{+}\right]\left[\mathrm{Cl}^{-}\right]$describes the reaction :
(a) $\mathrm{AgCl} \rightarrow \mathrm{Ag}^{+}+\mathrm{Cl}^{-}$
(b) $\mathrm{Ag}^{+}+\mathrm{Cl}^{-} \rightarrow \mathrm{AgCl}$
(c) $\mathrm{Ag}^{+}+\mathrm{Cl}^{-} \rightarrow \mathrm{Ag}+\mathrm{Cl}$
(d) $\mathrm{Ag}+\mathrm{Cl} \rightarrow \mathrm{Ag}^{+}+\mathrm{Cl}^{-}$

Answer. (a)
33. For which one of the following equilibrium equations will $K_{\mathrm{p}}$ equal $K_{\mathrm{c}}$ ?
(a) $\mathrm{PCl}_{5} \rightleftharpoons \mathrm{PCl}_{3}+\mathrm{Cl}_{2}$
(b) $\mathrm{COCl}_{2} \rightleftharpoons \mathrm{CO}+\mathrm{Cl}_{2}$
(c) $\mathrm{H}_{2}+\mathrm{I}_{2} \rightleftharpoons 2 \mathrm{HI}$
(d) $3 \mathrm{H}_{2}+\mathrm{N}_{2} \rightleftharpoons 2 \mathrm{NH}_{3}$

Answer. (c)
34. Which of the following shifts the equilibrium of the following reaction to the right?
$\mathrm{A}(\mathrm{g})+\mathrm{B}(\mathrm{g})+\mathrm{C}(\mathrm{g}) \rightleftharpoons \mathrm{A}(\mathrm{g})+\mathrm{BC}(\mathrm{g})$
(a) addition of more A
(b) removal of B
(c) increasing the pressure
(d) decreasing the temperature

Answer. (c)
35. In the reaction below, how could we cause the equilibrium to shift to the left?
$\mathrm{CH}_{4}(\mathrm{~g})+2 \mathrm{H}_{2} \mathrm{~S}(\mathrm{~g}) \rightleftharpoons \mathrm{CS}_{2}(\mathrm{~g})+4 \mathrm{H}_{2}(\mathrm{~g}) \quad \mathrm{K}=2.5 \times 10^{-3}$
(a) increasing the pressure by adding an inert gas at constant volume
(b) increasing the pressure by decreasing the volume
(c) increasing the volume by adding an inert gas at constant pressure
(d) increasing the pressure and the volume by adding an inert gas

Answer. (b)
36. The equilibrium expression, $K_{\mathrm{c}}=\left[\mathrm{CO}_{2}\right]$ represents the reaction :
(a) $\mathrm{C}(\mathrm{s})+\mathrm{O}_{2}(\mathrm{~g}) \rightleftharpoons \mathrm{CO}_{2}(\mathrm{~g})$
(b) $\mathrm{CO}(\mathrm{g})+1 / 2 \mathrm{O}_{2}(\mathrm{~g}) \rightleftharpoons \mathrm{CO}_{2}(\mathrm{~g})$
(c) $\mathrm{CaCO}_{3}(\mathrm{~s}) \rightleftharpoons \mathrm{CaO}(\mathrm{s})+\mathrm{CO}_{2}(\mathrm{~g})$
(d) $\mathrm{CaO}(\mathrm{s})+\mathrm{CO}_{2}(\mathrm{~g}) \rightleftharpoons \mathrm{CaCO}_{3}(\mathrm{~s})$

Answer. (c)
37. Which of the following statements dealing with equilibria is incorrect?
(a) catalysts have no effect on the value of the equilibrium constant
(b) the vapour pressure of liquid can be expressed as an equilibrium constant.
(c) at equilibrium in a reversible reaction, the rate of the forward reaction is equal to the rate of the reverse reaction
(d) $K_{\mathrm{p}}$ and $K_{\mathrm{c}}$ are numerically equal if a reversible reaction involves only gases Answer. (d)
38. Hydrogen molecules $\left(\mathrm{H}_{2}\right)$ can be dissociated into hydrogen atoms $(\mathrm{H})$. Which one of the following changes will not increase the number of atoms present at equilibrium?
(a) increasing the total pressure
(b) increasing the temperature
(c) adding H atoms
(d) increasing the volume of the container

Answer. (a)
39. Which of the following will increase the amount of $\mathrm{Fe}_{2} \mathrm{O}_{3}$ present at equilibrium in the reaction below?

$$
\mathrm{Fe}(\mathrm{~s})+3 \mathrm{H}_{2} \mathrm{O}(\mathrm{~g}) \rightleftharpoons \mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{~s})+3 \mathrm{H}_{2}(\mathrm{~g})
$$

(a) removing $\mathrm{H}_{2} \mathrm{O}(\mathrm{g})$
(b) adding Fe(s)
(c) removing $\mathrm{H}_{2}(\mathrm{~g})$
(d) cannot increase, since $\mathrm{Fe}_{2} \mathrm{O}_{3}$ is a solid

Answer. (c)
40. If a mixture where $\mathrm{Q}=\mathrm{K}$ is combined, what happens?
(a) nothing appears to happen, but forward and reverse reactions are continuing at the same rate
(b) the reaction shifts toward products
(c) the reaction shifts toward reactants
(d) nothing happens

Answer. (a)
41. For the reaction of hydrogen cyanide with water to form hydrogen ions and cyanide ions, the equilibrium constant at $25^{\circ} \mathrm{C}$ is $5 \times 10^{-10}$. What does this tell you about the position of the equilibrium and the rate of reaching equilibrium?
(a) the equilibrium lies toward reactants and the rate is slow
(b) the equilibrium lies toward products and you can tell nothing about the rate
(c) the equilibrium lies toward products and the rate is fast
(d) the equilibrium lies toward reactants and you can tell nothing about the rate

Answer. (d)
42. Equilibrium is established in the reversible reaction
$4 \mathrm{HCl}(\mathrm{g})+\mathrm{O}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{H}_{2} \mathrm{O}(\mathrm{g})+2 \mathrm{Cl}_{2}(\mathrm{~g}) \quad \Delta H^{\circ}=-114.4 \mathrm{~kJ}$
Which one of the following changes will not increase the amount of $\mathrm{Cl}_{2}$ present at equilibrium?
(a) removing $\mathrm{H}_{2} \mathrm{O}(\mathrm{g})$
(b) increasing the total gas pressure in the system
(c) decreasing the volume of the container
(d) raising the temperature

Answer. (d)
43. When solid $\mathrm{NH}_{4} \mathrm{HS}$ is placed in a closed flask at $28^{\circ} \mathrm{C}$, the solid dissociates according to the equation: $\mathrm{NH}_{4} \mathrm{HS}(\mathrm{s}) \rightleftharpoons \mathrm{NH}_{3}(\mathrm{~g})+\mathrm{H}_{2} \mathrm{~S}(\mathrm{~g})$
The total pressure of the equilibrium mixture is 0.766 atm . Determine $K_{\text {eq }}$ at this temperature.
(a) 0.147
(b) 0.766
(c) 0.587
(d) 0.383

Answer. (a)
44. Consider the reaction C (graphite) $+\mathrm{CO}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{CO}(\mathrm{g})$, which has the equilibrium constant $K_{\text {eq }}=3.7 \times 10^{-23}$ at $25^{\circ} \mathrm{C}$. What is the concentration of CO at equilibrium if we start with 0.22 g of $\mathrm{CO}_{2}$ per litre?
(a) $2.1 \times 10^{-12} \mathrm{M}$
(b) $3.7 \times 10^{-23} \mathrm{~atm}$
(c) $1.1 \times 10^{-12} \mathrm{M}$
(d) $2.9 \times 10^{-12} \mathrm{M}$

Answer. (a)
45. Which of the following reactions goes essentially to completion at equilibrium?
(a) $\mathrm{Br}_{2}(\mathrm{~g})+\mathrm{Cl}_{2}(\mathrm{~g})=2 \mathrm{BrCl}(\mathrm{g})$
$K_{\mathrm{c}}=7.0$
(b) $\mathrm{C}($ graphite $)+\mathrm{O}_{2}(\mathrm{~g})=\mathrm{CO}_{2}(\mathrm{~g})$
$K_{\mathrm{c}}=1.3 \times 10^{69}$
(c) $2 \mathrm{CH}_{4}(\mathrm{~g})=\mathrm{C}_{2} \mathrm{H}_{2}(\mathrm{~g})+3 \mathrm{H}_{2}(\mathrm{~g})$
$K_{\mathrm{c}}=0.154$
(d) $\mathrm{Br}_{2}(\mathrm{~g})=2 \operatorname{Br}(\mathrm{~g})$
$K_{\mathrm{c}}=4 \times 10^{-18}$

Answer. (b)
46. $K_{\mathrm{c}}$ for the equilibrium $2 \mathrm{CO}_{2}(\mathrm{~g})=2 \mathrm{CO}(\mathrm{g})+\mathrm{O}_{2}(\mathrm{~g})$ is $6.4 \times 10^{-7}$. What can be said about a mixture that contains $\left[\mathrm{CO}_{2}\right]=1.03 \times 10^{-1},[\mathrm{CO}]=2.4 \times 10^{-2}$ and $\left[\mathrm{O}_{2}\right]=1.18 \times 10^{-5}$ ?
(a) the mixture is at equilibrium
(b) the mixture will shift to generate more products
(c) the mixture will shift to generate more reactants
(d) because these are all gases, we need to know $K_{\mathrm{p}}$ in order to predict how this mixture will change Answer. (a)
47. For the equilibrium $\mathrm{N}_{2}(\mathrm{~g})+3 \mathrm{H}_{2}(\mathrm{~g})=2 \mathrm{NH}_{3}(\mathrm{~g})$, the value of $K_{\mathrm{c}}$ at $227^{\circ} \mathrm{C}$ is 152 . What is the value of $K_{\mathrm{p}}$ at $227^{\circ} \mathrm{C}$ ? Assume that pressures are measured in atmospheres.
(a) $9.03 \times 10^{-2}$
(b) 12.5
(c) 347
(d) $2.79 \times 10^{-4}$

Answer. (a)
48. Of the following equilibria, which one will shift to the left in response to a decrease in volume?
(a) $\mathrm{CO}_{2}(\mathrm{~g})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightleftharpoons \mathrm{H}_{2} \mathrm{CO}_{3}(\mathrm{aq})$
(b) $\mathrm{H}_{2}(\mathrm{~g})+\mathrm{Cl}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{HCl}(\mathrm{g})$
(c) $\mathrm{N}_{2}(\mathrm{~g})+3 \mathrm{H}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{NH}_{3}(\mathrm{~g})$
(d) $2 \mathrm{SO}_{3}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{SO}_{2}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g})$

Answer. (d)
49. Dinitrogen tetroxide undergoes the decomposition $\mathrm{N}_{2} \mathrm{O}_{4}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{NO}_{2}(\mathrm{~g})$ with $K_{\text {eq }}=5.85 \times 10^{-3}$ at $25^{\circ} \mathrm{C}$. If we begin with 0.100 atm dinitrogen tetroxide, what is the partial pressure of nitrogen dioxide at equilibrium?
(a) 0.200 atm
(b) 0.0050 atm
(c) 0.0228 atm
(d) 0.0750 atm

Answer. (c)
50. Calculate the equilibrium partial pressure of $\mathrm{PCl}_{3}$ in a 3.00 L vessel that was charged with 0.123 atm of $\mathrm{PCl}_{5}$.
$\mathrm{PCl}_{5}(\mathrm{~g}) \rightleftharpoons \mathrm{PCl}_{3}(\mathrm{~g})+\mathrm{Cl}_{2}(\mathrm{~g}) \quad\left(K_{\text {eq }}=0.0121\right)$
(a) 0.123 atm
(b) 0.0110 atm
(c) 0.0330 atm
(d) 0.0900 atm

Answer. c)
51. What is the solubility of AgCl in water if $K_{\mathrm{sp}}=1.6 \times 10^{-10}$ ?
(a) $1.6 \times 10^{-10}$
(b) $3.2 \times 10^{-10}$
(c) $1.3 \times 10^{-5}$
(d) $1.6 \times 10^{-5}$

Answer. (c)
52. For the following reaction at 500 K
$\mathrm{C}(\mathrm{s})+\mathrm{CO}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{CO}(\mathrm{g})$
the equilibrium mixture contained $\mathrm{CO}_{2}$ and CO at partial pressures of 7.6 atm and 3.2 atm respectively.
The value of the $K_{p}$ is
(a) 2.4 atm
(b) 18.1 atm
(c) .6 atm
(d) 1.0 atm

Answer. (b)
53. If the equilibrium concentrations found in the reaction $2 \mathrm{~A}(\mathrm{~g})+\mathrm{B}(\mathrm{g}) \rightleftharpoons \mathrm{C}(\mathrm{g})$ are $[\mathrm{A}]=2.4 \times 10^{-2} \mathrm{M}$, $[\mathrm{B}]=4.6 \times 10^{-3} \mathrm{M}$, and $[\mathrm{C}]=6.2 \times 10^{-3} \mathrm{M}$, calculate the value of $K_{\mathrm{c}}$.
(a) $2.3 \times 10^{3}$
(b) $1.8 \times 10^{-2}$
(c) $4.3 \times 10^{-4}$
(d) $5.8 \times 10^{2}$

Answer. (a)
54. Given the reaction $\mathrm{A}+\mathrm{B} \rightleftharpoons \mathrm{C}+\mathrm{D}$, find the equilibrium constant for this reaction if 0.7 moles of C are formed when 1 mole of A and 1 mole of B are initially present.
(a) 5.44
(b) 6.22
(c) 9.67
(d) 1.23

Answer. (a)
55. The $K_{\text {sp }}$ for $\mathrm{PbI}_{2}$ is $8.7 \times 10^{-9}$. What is the molar solubility of $\mathrm{PbI}_{2}$ ?
(a) $1.3 \times 10^{-3}$
(b) $8.7 \times 10^{-3}$
(c) $9.3 \times 10^{-5}$
(d) $1 \times 10^{-9}$

Answer. (a)
56. At a certain temperature, $K_{\text {eq }}$ for the reaction $3 \mathrm{C}_{2} \mathrm{H}_{2} \rightleftharpoons \mathrm{C}_{6} \mathrm{H}_{6}$ is 4 . If the equilibrium concentration of $\mathrm{C}_{2} \mathrm{H}_{2}$ is $0.5 \mathrm{~mole} / \mathrm{litre}$, what is the concentration of $\mathrm{C}_{6} \mathrm{H}_{6}$ ?
(a) 1.2 M
(b) 0.1 M
(c) 2.3 M
(d) 0.5 M

Answer. (d)

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57. For the reaction
$2 \mathrm{NO}(\mathrm{g})+\mathrm{Br}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{NOBr}(\mathrm{g}) \quad K_{\mathrm{c}}=1.32 \times 10^{-2}$ at 1000 K .
Determine the value of $K_{\mathrm{p}}$ that corresponds to this value of $K_{\mathrm{c}}$ at that temperature.
(a) 1.08
(b) 0.161
(c) $1.61 \times 10^{-4}$
(d) $2.39 \times 10^{-8}$

Answer. (c)
58. A chemist dissolves an excess of $\mathrm{BaSO}_{4}$ in pure water at $25^{\circ} \mathrm{C}$. If its $K_{\mathrm{sp}}=1 \times 10^{-10}$, what is the concentration of the barium in the water?
(a) $10^{-4} \mathrm{M}$
(b) $10^{-5} \mathrm{M}$
(c) $10^{-6} \mathrm{M}$
(d) $10^{-15} \mathrm{M}$

Answer. (d)
59. A reaction proceeds five times as fast at $60^{\circ} \mathrm{C}$ as it does at $30^{\circ} \mathrm{C}$. Estimate its energy of activation in $\mathrm{kcal} / \mathrm{mol}$.
(a) 1.61
(b) 13.4
(c) 10.8
(d) 11.6

Answer. (c)
60. The $K_{\text {sp }}$ of silver chromate $\left(\mathrm{Ag}_{2} \mathrm{CrO}_{4}\right)$ is $1.4 \times 10^{-12}$. What is the solubility in moles per litre of silver chromate?
(a) $7.0 \times 10^{-5} \mathrm{moles} /$ litre
(b) $3.5 \times 10^{-13} \mathrm{moles} / \mathrm{litre}$
(c) $6.2 \times 10^{-15} \mathrm{moles} / \mathrm{litre}$
(d) $1.0 \times 10^{-18} \mathrm{moles} / \mathrm{litre}$

Answer. (a)
61. At $25^{\circ} \mathrm{C}$, for $3 \mathrm{O}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{O}_{3}(\mathrm{~g}) \quad K_{\mathrm{c}}=2.9 \times 10^{-59}$.

If at equilibrium, the concentration of $\mathrm{O}_{2}$ is 0.040 M , what is the concentration of $\mathrm{O}_{3}$ ?
(a) $1.9 \times 10^{-63} \mathrm{M}$
(b) $4.3 \times 10^{-32} \mathrm{M}$
(c) $2.3 \times 10^{31} \mathrm{M}$
(d) $1.2 \times 10^{21} \mathrm{M}$

Answer. (b)
62. Equilibrium is established in a sealed 1.75 L vessel at $250^{\circ} \mathrm{C}$ in the reaction
$\mathrm{PCl}_{5}(\mathrm{~g}) \rightleftharpoons \mathrm{PCl}_{3}(\mathrm{~g})+\mathrm{Cl}_{2}(\mathrm{~g})$
The quantities found at equilibrium are $0.562 \mathrm{~g} \mathrm{PCl}_{5}, 1.950 \mathrm{~g} \mathrm{PCl}_{3}$, and $1.007 \mathrm{~g} \mathrm{Cl}_{2}$.
(a) $K_{\mathrm{c}}=3.49$
(b) $K_{\mathrm{c}}=0.0139$
(c) $K_{\mathrm{c}}=2.00$
(d) $K_{\mathrm{c}}=0.0427$

Answer. (d)
63. The equilibrium constant for the isomerization of butane at $25^{\circ} \mathrm{C}$ is $K_{\mathrm{c}}=7.94$.


If 5.00 g butane is introduced into a 12.5 L flask at $25^{\circ} \mathrm{C}$, what mass of isobutane will be present when equilibrium is reached?
(a) 4.44 g
(b) 0.00613 g
(c) 0.684 g
(d) 39.7 g

Answer. (a)
64. For the synthesis of phosgene at $395^{\circ} \mathrm{C}$
$\mathrm{CO}(\mathrm{g})+\mathrm{Cl}_{2}(\mathrm{~g}) \rightleftharpoons \mathrm{COCl}_{2}(\mathrm{~g}) \quad K_{\mathrm{c}}=1.2 \times 10^{3}$
If 0.700 mol CO and $0.500 \mathrm{~mol} \mathrm{Cl}_{2}$ are placed in a 8.05 L reaction vessel at $395^{\circ} \mathrm{C}$ and equilibrium is established, how many moles of $\mathrm{COCl}_{2}$ will be present?
(a) $0.090 \mathrm{~mol} \mathrm{COCl}_{2}$
(b) $0.060 \mathrm{~mol} \mathrm{COCl}{ }_{2}$
(c) $0.72 \mathrm{~mol} \mathrm{COCl}_{2}$
(d) $0.48 \mathrm{~mol} \mathrm{COCl}{ }_{2}$

Answer. (d)
65. For the reaction $\mathrm{N}_{2}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{NO}(\mathrm{g}), K_{\mathrm{c}}=4.08 \times 10^{-4}$ at 2000 K . What is the value of $K_{\mathrm{c}}$ at $2000 K$ for the reaction $\mathrm{NO}(\mathrm{g}) \rightleftharpoons 1 / 2 \mathrm{~N}_{2}(\mathrm{~g})+1 / 2 \mathrm{O}_{2}(\mathrm{~g})$ ?
(a) $6.01 \times 10^{6}$
(b) $2.45 \times 10^{3}$
(c) $2.02 \times 10^{-2}$
(d) 49.5

Answer. (d)
66. For the reaction
$\mathrm{CO}(\mathrm{g})+\mathrm{H}_{2} \mathrm{O}(\mathrm{g}) \rightleftharpoons \mathrm{CO}_{2}(\mathrm{~g})+\mathrm{H}_{2}(\mathrm{~g}) \quad K_{\mathrm{c}}=23.2$ at 600 K
If 0.250 mol each of CO and $\mathrm{H}_{2} \mathrm{O}$ are introduced into a reaction vessel and equilibrium is established, how many moles of CO will be present?
(a) 1.20 mol CO
(b) 0.043 mol CO
(c) 0.315 mol CO
(d) 0.207 mol CO

Answer. (b)
67. For the reaction
$\mathrm{C}(\mathrm{s})+2 \mathrm{H}_{2}(\mathrm{~g}) \rightleftharpoons \mathrm{CH}_{4}(\mathrm{~g}) \quad K_{\mathrm{p}}=0.0263$ at $1000^{\circ} \mathrm{C}$.
Calculate the pressure of $\mathrm{H}_{2}$ when $0.100 \mathrm{~mol} \mathrm{CH}_{4}$ and an excess of $\mathrm{C}(\mathrm{s})$ are brought to equilibrium at $1000^{\circ} \mathrm{C}$ in a 4.16 L reaction vessel.
(a) 3.29 atm
(b) 0.183 atm
(c) 2.28 atm
(d) 1.14 atm

Answer. (c)
68. For the reaction below, $K_{\mathrm{p}}=110$ at 800 K .
$\mathrm{CO}_{2}(\mathrm{~g})+\mathrm{C}(\mathrm{s}) \rightleftharpoons 2 \mathrm{CO}(\mathrm{g})$
Suppose we introduce $10.0 \mathrm{~atm} \mathrm{CO}_{2}$ into a 10.0 L flask at 800 K . What is the minimum number of grams of C we must add to allow the system to achieve equilibrium?
(a) 79 g C
(b) 1.8 g C
(c) 18.3 g C
(d) 14.2 g C

Answer. (d)
69. For the reaction below, $K_{p}=2.0$ at 1200 K . If we introduce $0.400 \mathrm{~mol} \mathrm{COF}_{2}$ into a 3.00 L flask at 1200 K , what is the partial pressure of $\mathrm{COF}_{2}$ at equilibrium?
$2 \mathrm{COF}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{CO}(\mathrm{g})+2 \mathrm{~F}_{2}(\mathrm{~g})$
(a) 6.1 atm
(b) 8.3
(c) 5.4
(d) 3.5 atm

Answer. (d).

